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Dynamical Coupling Between Ferromagnets Due to Spin Transfer Torque

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We use a combination of analytic calculations and numerical simulations to demonstrate that electrical current flowing through a magnetic bilayer induces dynamical coupling between the layers. The coupling originates from the dependence of the spin transfer torque exerted on the layers on the relative orientations of their magnetic moments. We demonstrate that such coupling modifies the behaviors of both layers, significantly affecting the the stability of the current-induced dynamical regimes and the efficiency of current-induced magnetic reversal.

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Current-induced spin transfer (ST) effect [1] is the most promising mechanism for manipulation of magnetic nanodevices, due to the simplicity of the implementation and potential power benefits. The main obstacle for viable applications of the effect is the large magnitude of the required current, which is too close to the limit of the physical stability of devices. A basic magnetoelectronic device consists of a magnetic bilayer $F_1/N/F_2$, where F_1 is a magnet needed to polarize the current, N is a metallic or insulating nonmagnetic spacer, and F_2 is a nanomagnet whose magnetic configuration can be changed by current via ST. The efficiency of spin transfer can be characterized by the zero-temperature threshold current I_c for the onset of current-induced magnetic dynamics of F_2 . In the framework of the widely accepted spin transfer torque (STT) model [2, 3],

$$I_c = eH_{eff}m_2\alpha/(\hbar g_2), \quad (1)$$

where e is the electron charge, H_{eff} is the effective magnetic field which includes the magnetic anisotropy of F_2 , α is the Gilbert damping parameter, and g_2 is a function of the relative orientations of the magnetic moments m_1 and m_2 of F_1 and F_2 , respectively, which depends predominantly on the spin polarizing properties of F_1 .

Several directions are pursued for reducing I_c . The function g_2 is proportional to the polarization $p = (I_\uparrow - I_\downarrow)/I$ of the current generated by F_1 [4]. Here, $I_\uparrow$ and $I_\downarrow$ are the spin-up and spin-down contributions to the current. Therefore, I_c can be reduced by enhancing the spin-polarizing properties of F_1 . However, the difference between the typical value $p \approx 0.7$ for the common F_1 such as $\text{Py}=\text{Ni}_{80}\text{Fe}_{20}$ and the largest possible $p = 1$ is small, limiting the room for improvement. Alternatively, I_c can be reduced by decreasing H_{eff} , which at small external field H is dominated by the anisotropy of F_2 . Simply reducing the magnetization M_2 of F_2 would decrease H_{eff} , but this would also compromise the stability of the magnetic configuration. Devices with perpendicular magnetic anisotropy can in principle overcome this limitation, but the potential advantages were offset by the reduced polarization and increased α [5]. Attempts to reduce m_2 while stabilizing F_2 with an antiferromagnet have encountered similar complications [6].

FIG. 1: Dynamics of two magnetic moments m_1 and m_2 due to the spin torques τ_1^{STT} and τ_2^{STT} exerted on the respective moments. (a) the signs of g_1 and g_2 are the same, (b) the signs of g_1 and g_2 are opposite.

Here, we discuss the previously unexplored mechanism affecting the efficiency of ST, involving simultaneous current-induced effects on both ferromagnets in a bilayer consisting of F_1 and F_2 . This mechanism couples the dynamics of the two magnets. We describe analytic results for a simple model system, and present realistic numerical calculations in macrospin approximation. Our results demonstrate that I_c can be either increased or reduced with respect to the value given in Eq. 1 by a suitable choice of F_1 and F_2 . Most importantly, we show that the dynamics of both magnets are *always excited simultaneously*, and thus both magnetic layers always participate in the current-induced behaviors.

Analytic Model. To introduce the idea of dynamical coupling of magnetic layers by STT and understand the consequences of such coupling, we consider an idealized system of two nanoscale magnets F_1 and F_2 represented by the magnetic moments m_1 and m_2 , whose magnitudes are fixed in the macrospin approximation. For simplicity, this model neglects the demagnetizing fields of the ferromagnets and their dipolar coupling. The dynamics of the magnetic moments in the presence of current $I > 0$ flowing from F_1 to F_2 can be described by two Landau-Lifshitz equations coupled by the STT term [2]

$$\frac{dm_{1,2}}{dt} = \gamma m_{1,2} \times [H - \alpha \frac{m_{1,2}}{|m_{1,2}|} + \frac{I g_{1,2}}{e S_{1,2}} \frac{m_1}{|m_1|} \times \frac{m_2}{|m_2|}], \quad (2)$$

where γ is the gyromagnetic ratio, and $S_{1,2} = m_{1,2}/(\gamma\hbar)$ are the spins of $F_{1,2}$. For simplicity, we assume the

same α for both magnets, and neglect the dependence of $g_{1,2}$ on the relative orientations of m_1 and m_2 . The experimentally determined values of I_c are similar in both parallel (P) and antiparallel (AP) configurations of the magnetic moments, justifying the latter approximation [4]. In the limit $S_1 \gg S_2$, the last term in Eq. 2 for m_1 is negligible due to the large value of S_1 , resulting in a static solution for m_1 . The equation for m_2 then yields precession of m_2 at $I = I_{c0}$ determined by Eq. 1, consistent with the models for the dynamics of a single ferromagnet. At $I > I_{c0}$, the AP state becomes stable, and the solution for m_2 is a precessional reversal into this state.

We are interested in the solution of Eq. 2 for comparable values of S_1 and S_2 . As illustrated in Fig. 1, STT exerted on both layers can induce their simultaneous precession around the magnetic field H with cone angles θ_1 and θ_2 . A simple estimate shows that a stable configuration involves precession of m_1 and m_2 with the same polar angle (Fig. 1(a)). To demonstrate the stability of this configuration, we assume that m_1 lags behind m_2 by a small polar angle ϕ . The torque τ_{STT_1} exerted on m_1 then acquires an additional component in the polar direction, resulting in the increase of its angular frequency by $\Delta\omega_1 = \gamma I g_1 \sin(\theta_2) \sin(\phi) / [e S_1 \sin(\theta_1)]$. Similarly, a component of STT exerted on m_2 in the polar direction increases its angular frequency by $\Delta\omega_2 = \gamma I g_2 \sin(\theta_1) \sin(\phi) / [e S_2 \sin(\theta_2)]$. The stability of the coupled precession with respect to fluctuations of ϕ requires that $\Delta\omega_1 > \Delta\omega_2$, which is satisfied if $[\sin(\theta_1)/\sin(\theta_2)]^2 < S_2/S_1$. The derivation given below shows that the latter inequality usually holds, ensuring the stability of in-phase precession.

The stationary form of Eq. 2 for in-phase precession is

$$\begin{aligned} I g_1 \sin(\theta_2 - \theta_1) &= e S_1 \alpha H \sin(\theta_1) \\ I g_2 \sin(\theta_2 - \theta_1) &= e S_2 \alpha H \sin(\theta_2). \end{aligned} \quad (3)$$

The filtering properties of F_1 and F_2 are often similar, resulting in $g_1 \approx g_2$. Eqs. 3 then lead to

$$S_1 \sin(\theta_1) = S_2 \sin(\theta_2), \quad (4)$$

which satisfies the condition for the stability of in-phase precession, as discussed above. Eqs. 3 yield the current for the precession onset $I_c = I_{c0}/[1 - S_2/S_1]$. We emphasize three main consequences of Eqs. 3. Firstly, both moments *always precess simultaneously*. Secondly, the relation between the amplitudes of the dynamics of the two moments is determined by the ratio $A = S_2/S_1$. In particular, the dynamics of m_1 is negligible at $A \ll 1$. Precession of m_2 can then occur only at $I = I_c > 0$. Conversely, the dynamics of m_2 is negligible at $A \gg 1$, while precession of m_1 can occur at $I < 0$. Finally, I_c also depends on A . In particular, it diverges when the magnetic moments become equal ($A=1$).

To determine the nature of excitations and stability regimes for the magnets coupled by STT, we insert Eq. 4

FIG. 2: Stability diagram for the analytic model of two-layer system with varied $A = S_1/S_2$. (a) $g_1 = g_2$, bistable regions are hatched. (b) $g_1 = -g_2$, the region of stable precession is filled. For $A < 1$, I_{c0} is defined by Eq. 1. For $A > 1$, I_{c0} is defined by Eq. 1 with m_2 replaced by m_1 to emphasize the dominance of this layer's dynamics.

into the second of Eqs. 3, leading to

$$I = \frac{I_{c0}/A}{\sqrt{1/A^2 - 1 + \cos^2(\theta_2)} - \cos(\theta_2)}, \quad (5)$$

where $I_{c0} = \alpha H e S_2 / g_2$. Eq. 5 describes a monotonically decreasing function of θ , which implies that precession is unstable at any I . On the other hand, both $\theta_2 = 0$ and $\theta_2 = \pi$ are stable in the range $I'_c = \frac{P}{1+A} < I < \frac{P}{1-A} = I_c$, where I'_c is the current at which the AP state becomes stable. The resulting stability diagram is shown in Fig. 2(a), where the bistable regions are hatched.

As a consequence of the dynamical coupling due to STT, the value of I'_c is reduced by a factor of two at $A = 1$, while I_c diverges. It remains to be seen whether these coupling effects can be utilized to increase the efficiency of magnetoelectronic devices. Current-induced bistability in devices with $A \approx 1$ should generally result in telegraph-type noise due to thermally activated transitions between the two stable configurations. Such noise is detrimental to most applications. However, such configuration may be useful if small-amplitude current-induced dynamics is undesired. For $A < 1$, dynamical coupling also makes it impossible to induce dynamical states at $I < 0$. Similarly, dynamics cannot be induced at $I > 0$ for $A > 1$. We shall see below that this result also holds for a more realistic model. The fact that bipolar current-induced excitations were observed [8, 9] must indicate a significant breakdown of the macrospin approximation in these experiments.

Applications of magnetoelectronic devices in microwave generation require I_c to be minimized, and stable precession to be achieved over a significant range of I . We demonstrate below that I_c can be reduced by the current-induced coupling when g_1 and g_2 have opposite signs. This requires reversing the spin anisotropy of one of the ferromagnets, which can be accomplished by doping F_1 or F_2 with impurities providing appropriate spin-dependent scattering in their bulk, and/or by

choosing N that inverts the spin anisotropy of electron scattering at F/N interface [10]. For simplicity, we now assume that $g_1 = -g_2 < 0$. The torques exerted on the two magnets now result in the mutual attraction of the moments at $I < 0$, resulting in a stable collinear configuration at $I < 0$ for any A . Dynamical states are induced only by $I > 0$, regardless of the value of A . Fig. 1(b) shows that the relative precession phases of m_1 and m_2 are now shifted by 180° . Estimates similar to the ones presented above for $g_1, g_2 > 0$ show that this precessional configuration is stable.

Eq. 4 for the precession cone angles of the two moments still holds, but Eq. 5 is replaced with

$$I = \frac{I_{c0}/A}{\sqrt{1/A^2 - 1 + \cos^2(\theta_2)} + \cos(\theta_2)}. \quad (6)$$

The resulting stability diagram shown in Fig. 2(b) includes a region of stable coupled precession of the two magnets. At $A = 1$, the precession onset current is reduced by a factor of two, while the largest value of I at which the precession remains stable diverges.

Numerical Simulations. To determine whether the current-induced coupling remains robust in realistic systems, we solved Eqs. 2 numerically. We used the geometry and the magnetic properties typical for the spin-transfer devices, in which F_1 and F_2 are Py layers with $M = 800$ emu/cm³ and thicknesses t_1 and t_2 , patterned into an elliptical shape with dimensions 120×60 nm [1]. We used the material parameters known from the magnetotransport measurements [11]. The demagnetizing fields were taken into account. The dipolar coupling was neglected to eliminate its influence on the interpretation of current-induced behaviors. We included the dependencies of the spin transfer efficiencies g_1, g_2 on the configuration of the magnetic system to take into account the slight experimental asymmetry between the P→AP and AP→P reversals [4]. The equations were numerically integrated by the stochastic Heun method with a fixed time step set to 2 psec. To verify the convergence, the step size was decreased by a factor of two, which did not significantly affect the results. Random field approximation was used to model the thermal activation between different current-induced modes, with temperature set to 50 K. Damping parameter $\alpha = 0.03$ was used for both magnets [12].

The model was tested for three limiting cases: $t_1 \gg t_2$, $t_1 \ll t_2$, and $t_1 = t_2$. In the first case, STT induced the dynamics of only m_2 , and only at $I > 0$. Fig. 3(a) shows the normalized spectra of the component of m_2 along the hard in-plane axis for $A = 0.2$. The peaks correspond to several harmonics of the precession frequency. After the onset of small-angle precession at $I_c = 1.2$ mA, the frequency of precession decreases due to transition to large-angle clamshell precession trajectory. The transition to the out-of-plane precession at $I > 2.6$ mA results in the increase of precession frequency. These results

FIG. 3: (a)-(c) Normalized spectral intensity for the dynamics of the in-plane hard-axis component of m_2 , (a) $A = 0.2$, (b) $A = 0.67$, (c) $A = 1$ and $g_1 = -g_2$. Lighter colors correspond to higher intensity. The same scale is used in all three plots. (d) Time trace for the trajectories of m_1 (dark blue) and m_2 (light pink) for $A = 0.67$, $I = 15$ mA. x is the easy direction, y is the hard in-plane direction, and z is perpendicular to the film plane. The calculations were performed at $H = 1$ kOe along the easy axis, and a fixed $t_2 = 4$ nm.

are consistent with the published calculations for single layer dynamics, and are in overall agreement with the experiments [13]. Similar spectra were obtained for the dynamics of m_1 at $I < 0$, for $t_1 \ll t_2$. Calculations for $t_1 = t_2$ yielded identical spectra for m_1 and m_2 regardless of the sign of I , as expected for this symmetric geometry. Additionally, the calculations for $t_1 = t_2$ and $H = 0$ reproduced the sequential thermally activated flipping of m_1 and m_2 experimentally observed in symmetric magnetic nanopillars [14].

Current-induced coupling of the dynamics of two layers significantly affected the spectra at $0.4 < A \leq 1$, as illustrated in Fig. 3(b) for $A = 0.67$. The onset current for the magnetic dynamics is larger than in Fig. 3(a), in agreement with the results of the analytic model presented above. At $3 \text{ mA} < I < 6 \text{ mA}$, the data exhibit a broad incoherent excitation spectrum due to random transitions between different types of precession dynamics of m_2 . Specifically, the precession of m_2 alternates between the clamshell-type and the out-of-plane trajectories, depending on the relative phase with the elliptical precession of m_1 . The latter is not phase-coherent with m_2 . The formation of a sharp peak at $6 \text{ mA} < I < 12 \text{ mA}$ is associated with the complete transition to out-of plane precession of m_2 , resulting in nearly static deflection of m_1 towards m_2 . At $I > 12$ mA, the oscillations of m_1

become sufficiently large to disrupt the periodic precession of m_2 , resulting in increasingly chaotic dynamics of both. Fig. 3(b) shows the trajectories of m_1 and m_2 over a 0.5 nsec period at 15 mA. Despite nearly chaotic behavior of both moments, some parts of the trajectory of m_2 resemble clamshell and out-of-plane precession. The chaotic behaviors persisted in deterministic simulations at $T = 0$, eliminating thermal fluctuations as their cause. Based on the analysis of the trajectories, we believe that these behaviors are caused by a combination of large phase space associated with the dynamics of both magnets, and nonlinear nature of the large-amplitude magnetic dynamics.

At $A > 0.67$, the broad excitation band at small I and the out-of-plane precession peak gradually disappeared. At $A = 1$, only the $I > 12$ mA continuum remained, and similar features appeared at $I < -12$ mA. There were no excitations at $I < 0$ for all $A < 1$, in agreement with the analytic results described above. These results seem to be inconsistent with the intuitive picture, according to which $I > 0$ can induce the dynamics of m_2 , while $I < 0$ can induce the dynamics of m_1 even for $A < 1$ [15]. However, analysis of the magnetic trajectories shows that all oscillations of m_1 at $I < 0$ are efficiently suppressed by m_2 closely following m_1 , thus reducing STT exerted on both layers.

Calculations for $g_1 = -g_2$ showed that I_c is reduced in this case, in agreement with the analytic model. Fig. 3(c) shows spectra calculated for $A = 1$. $I_c = 0.75$ mA is slightly over half of the value I_{c0} obtained for $A \ll 1$. Therefore, reduction of the critical current for $g_1 = -g_2$ appears to be a robust feature of dynamical coupling. The spectra do not exhibit broadening and chaotic dynamics characteristic of the $g_1 = g_2$ data. The peaks in Fig. 3(c) abruptly terminate at $I = 3.8$ mA due to the formation of a static stable configuration with m_1 and m_2 oriented opposite to each other perpendicular to the film plane. Such static configuration is, however, not present for $A < 1$.

We have performed additional calculations without some of the simplifying assumptions of our model. In particular, we tested the effects of different magnetic damping in the two magnets and different magnetizations. We also checked the effect of the dipolar coupling between the layers. The modifications did not qualitatively change our conclusions regarding the effects of current-induced coupling, as long as the resonant frequencies of the two layers remained similar to each other.

In summary, we have analyzed the simultaneous effects of spin torque on both layers in a magnetic bilayer. We showed that the spin torque results in dynamical coupling between the layers, modifying their individual current-

induced dynamical properties. In particular, the onset of magnetic precession of both magnetic layers always occurs at the same current. In case of similar spin-transport anisotropy of both layers, the onset current for magnetic precession is increased, diverging for identical values of the moments of the two layers. Realistic numerical simulations show that coupling often leads to incoherent dynamical regimes associated with transitions between different dynamical states of the bilayer. However, for the opposite spin-transport anisotropy of the two layers, the onset current for the magnetic precession is decreased, and coherence is maintained even for the identical dimensions of the magnetic layers. This effect of dynamical coupling on the spin transfer efficiency can become useful for implementing devices with improved performance.

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