Design and development of a prototype of dual modality PET/optical breast cancer margin specification imager

Krishna Nandanavanam

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Design and development of a prototype of dual modality PET/optical breast cancer margin specification imager

Krishna Nandanavanam

Thesis submitted to the
College of Engineering and Mineral Resources at West Virginia University
in partial fulfillment of the requirements for the degree of

Master of Science
in
Mechanical Engineering

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Morgantown, West Virginia
2010

Keywords: Breast Cancer Imager, 3D Reconstruction, Image Processing
Abstract

Design and Development of a Prototype of Dual Modality PET/Optical Breast Cancer Margin Specification Imager

Krishna Nandanavanam

This thesis is an attempt to develop a prototype of a breast cancer imager to assess the margins of excised breast tissue. This device is proposed to be used to assure that the entire cancerous lesion has been removed by imaging the intensity of a radio labeled tracer and inspecting for a noncancerous margin in the volume of the tissue sample. The dual modality PET/optical breast cancer specification imager uses a pair of small PET detectors to measure the bioactivity of an excised sample of tissue. A co-registered optical image is taken to allow the surgeon to visually correlate the position of the lesion images obtained with the PET imager within the physical limits of the specimen, and to verify if margins are sufficient. This assists the surgeon in deciding if additional tissue removal is required. The hardware and software required to operate the optical modality was designed and developed as a part of this thesis. Various phantoms were tested and it was demonstrated that 3D reconstruction of volume can be calculated for objects with perfect convex surfaces and irregular convex surfaces of different sizes using the optical modality. By performing error analysis it was found out that the 3D surface can be reconstructed with an accuracy of ±1 mm. A calibration procedure was followed to merge the PET and optical volumes. Fusion of PET and optical volumes and margin evaluation of the merged volume was successful. It is proved that dual modality imager can be used for margin analysis and is potential enough for further research in this direction.
Dedication

To my beloved parents Sri Latha and Mohan Rao…
Acknowledgements

I take this opportunity to appreciate all the individuals who have been with me throughout this journey and have helped me to successfully complete my thesis. I am greatly thankful to Dr. Larry E. Banta for his constant support, guidance and being my research advisor. I am also grateful to Dr. Stanislaw Majewski for his financial support to the project and being my committee member. I extend my thanks to Dr. Sam Mukdadi for his valuable suggestions and for being on my committee. I thank my team Dr. Alexander Stolin and Pete Martone for their valuable suggestions.

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1 General Introduction

1.1 Introduction

Breast Conservation Therapy has become a much sought alternative to mastectomy in the treatment of smaller cancerous lesions as both the procedures are equally effective. Lumpectomy is a breast conserving technique where in the surgeon removes the cancerous tumor from the breast surrounded by healthy tissue. Major clinical trials have demonstrated similar survival rates for stage II breast cancer patients undergoing breast conservation therapy (lumpectomy followed by radiation therapy) and mastectomy (1). Also there is no increased risk of developing second malignancies in patients undergoing lumpectomies compared with mastectomy (2).

There have been huge advances in the technologies used for breast cancer imaging. Mammography has been the gold standard in identifying breast cancer due to the factors associated with performance, reliability and cost effectiveness. Mammogram uses X-rays to examine and is the most effective technology available for breast cancer diagnosis. Constant effort is being made to provide more information to the surgeon about the lesion localization, to decrease the intensity of radiation used in mammography; to improve the image quality and to develop techniques to interpret these images. Digital Mammography increases the sensitivity and optimizes the contrast between the malign and benign tissues. Digital Mammographic Imaging Screening Trials (DMIST) conclude that more accurate detection of cancer is possible with digital mammography for pre- or perimenopausal women under the age of 50 or women of any age with dense breasts. Patients are exposed to reduced doses of radiation in digital mammograms than film mammograms (3).

Computer-aided Detection (CAD) systems may be used to improve the accuracy of conventional and digital mammograms. Ultrasonography is an adjunct technology to mammography which can be used in improving the overall sensitivity of the system. This is painless and involves no radiation but the results obtained are not consistent in many cases as it depends mainly on the operator's skill(4). The usage of ultrasound in breast diagnosis is still under investigation. Magnetic Resonance Imaging (MRI) is used to determine the extent of cancer in the body after diagnosis. According to the American Cancer Society MRI is
used for diagnosing patients who have more than 20% life time risk of developing cancer. MRI may also be useful in imaging dense breast tissues (3).

However mammogram images can be ambiguous in many cases. This makes it difficult to localize the presence of the tumor and might lead to complete resection of the breast. Positron Emission Tomography (PET) is an effective solution in this direction. It has the potential to identify the presence of cancer even when the other imaging techniques give normal results. It is especially helpful in the cases where a mammogram is not able to provide clear information. Advances in nuclear medicine have introduced new techniques like radionuclide imaging. F-18 Flouro-deoxyglucose (FDG) is the most widely used radiopharmaceutical for imaging breast cancer. The cancer cells demonstrate increased metabolic rate compared to normal tissue, and the FDG can be imaged using a PET imager (5).

Once the location of the cancerous tissue is identified the surgeon removes the cancerous lesion under the guidance of the mammogram images. The excised breast specimen is delivered to pathology with the edges of the specimen marked. The marked edges of the specimen are called margins. The success of the surgery lies in achieving negative margins which means adequate healthy tissue is surrounding the cancer cells. If the margins are positive then re-excision is to be done and this entire process may extend up to an hour. Through this entire period of time the patient is held under anesthesia with an open incision. In as many as 25-50% of cases a follow up surgery is necessary to remove residual cancerous tissue left during the first procedure.

The 'Dual Modality PET/optical Imager' is an attempt to determine these margins of the healthy tissue around the cancerous lesion thereby assisting the surgeon in achieving negative margins. This may potentially avoid the necessity of an additional surgery to remove the cancerous lesions and reduce the waiting time.
1.2 Motivation

The challenge associated with breast conservation procedure in breast cancer treatment is adequate margins while preserving the healthy tissue as much as possible. In most of the cases after the cancerous lesion is removed surgically the excised tissue is sent to the pathology for margin assessment. This process might take 20-30 minutes or more to get a confirmation that adequate margins are achieved. The surgeon and the patient must wait to hear from pathology. The waiting time may further be prolonged if adequate margins are not achieved as expected and this process may be repeated several times before the surgery is concluded. Through this entire process the patient is held with an open incision and exposed to anesthesia which can result in increased morbidity and adverse neurological effects of anesthesia. Extended waiting time means an increase in the cost of the surgical procedure to the patients.

Various reports say that positive margins occur in 20-70 % of the patients leading to a second surgery (6). Positive margins can lead to multiple re-excisions which mean additional costs and anxiety to the patients, a compromise in the cosmetic outcome or can possibly result in mastectomy. The benefits associated with the decrease in the rate of positive margins have encouraged many studies to investigate and find a solution to this problem with margin analysis being a step in that direction. Surgical margin analysis has proved to be a critical component of breast conservation therapy in spite of various issues being controversial (6). Intra-operative margin assessment has been investigated as a tool to reduce the rate of positive margins as re-excision is done at the same time, thereby eliminating the need for a second surgery. This importance raises a need to find a standardized procedure to calculate the margins and to help the patient by reducing the need for multiple re-excisions and also help the surgeon in making treatment decisions. The margin assessment methods may influence the final pathological results and ultimately the treatment decisions taken by the surgeons (7).

Various margin analysis techniques like frozen section analysis, permanent section analysis and multicolor inking systems have been studied. While all these techniques may reduce the rate of positive margins, the problem still persists. Reports show that at least 20% of the patients return to the operating room for re-excision. Despite the best efforts of the surgeons the rates of re-excisions continue to be high (4). From these numbers it is understood that there is a dire need to investigate new technologies which can reduce the rates of positive margins.
1.3 Proposed Novel Approach

The dual modality PET /Optical imager (DMI) is a table top or mobile 3d imaging system, located in the operating room (OR), and providing fast in-situ determination of tumor resection and the adequacy of surgical margins. DMI uses PET and optical modalities to evaluate the margins of an excised sample of tissue, typically a cancerous lesion surgically removed from a patient, with an appropriate healthy tissue margin. The Positron Emission Tomography (PET) Tissue Sample system uses a pair of small PET detectors to identify the cancerous lesion by imaging the intensity of a radio labeled tracer in the excised breast tissue while the optical modality uses a camera to give the physical outline of the same.

The excised specimen is placed on a specimen holder which is present on a rotary table. For the optical reconstruction the specimen is rotated from 0 to 350 degrees and an image is captured by the camera every 10°. PET images are taken at the same time. Optical 3D reconstruction of the surface of the excised breast tissue is done from the 36 projections taken by the camera while the PET process produces images of only the cancerous tissue. 3D volumes obtained from both the modalities are merged and the margins are evaluated. If there are any positive margins the surgeon can go back to the patient and re-excite to obtain negative margins. The processing time of the imager for margin assessment is anticipated to be 15 minutes.

Such an instrument can reduce the overall surgery time and the number of iterations required for adequate margins although the final margin confirmation may have to be obtained from the pathology. The DMI may also reduce the number of follow-up surgeries required.
1.4 Objectives and Contributions

The objective of this research is to develop the optical modality of the prototype of a dual modality PET/Optical imager and perform the margin assessment by merging the reconstructed PET and optical images. The scope of the work is as follows:

- Add the optical modality to the existing PET prototype.
- Develop software to do the 3D reconstruction and slice generation of the surface of the excised specimen from the optical data.
- Mathematically merge the PET and optical volumes.
- Evaluate the margins of the merged volume to determine the adequacy of the margins obtained.
- Develop calibration fixtures and procedures for the DMI.
- Test and demonstrate the system.
2 Literature Survey

2.1 Background

Breast cancer is the second major cause of deaths due to cancer in women, after lung cancer and more than 184,000 patients were diagnosed with breast cancer in 2008. In 2008 more than 40,480 women died from breast cancer in the USA. Breast cancer can be treated if it is diagnosed early. More than 90% of the patients have localized disease during diagnosis in western countries. One in eight of the North American women (who live up to the age of 85) have a lifetime risk of developing breast cancer (3).

2.2 Imaging in Breast Cancer

Technological development in various imaging modalities has contributed to advances in breast cancer management and has led to a decrease in the mortality rate due to breast cancer. New evolving diagnostic technologies look promising in detecting cancer at an early stage and in improving the breast cancer survival rate. Early detection of cancer is the key factor in increasing the survival rate from breast cancer.

2.2.1 Mammography

Mammographic screening helps in early diagnosis and has contributed to a 25% to 30% decrease in mortality rate (3). It has been the gold standard for breast cancer detection and is found to be the best method to decrease the mortality rate due to breast cancer. Accuracy of mammography is influenced by factors like age and dense breasts. Sensitivity varies from 62.9% in women with extremely dense breasts to 87.0% in women with almost entirely fatty breasts (8). In the case of dense breasts the sensitivity is as low as 30-48% (9). Sensitivity is also influenced by age and increases from 68.6% in women 40 to 44 years of age to 83.3% in women 80 to 89 years of age (8). These factors along with a family history of breast cancer and long intervals between mammograms may lead to false positive results in mammography. Mammography has limitations in imaging dense and augmented breasts and plays a very limited role in axillary lymph node metastasis.
2.2.2 Ultrasonography

Screening mammography is the best available technique for breast cancer detection, yet some breast cancers cannot be identified by mammography. Ultrasound is an adjunct technique to mammography for breast cancer diagnosis. Ultrasonography (US) can be used for additional information when mammograms are ambiguous. This technique is especially helpful in diagnosing young, pregnant and lactating women, women with dense breasts and those at a high risk of developing cancer. US may detect 3-4 cancers additionally compared to mammography per 1000 women in the high risk category(10). The role of US in breast cancer detection is still being studied in a large randomized trial, conducted by the American College of Radiologists Imaging Network (ACRIN). Use of US requires highly experienced operators but the benefits are that the process is painless and requires no radiation (11).

2.2.3 Magnetic Resonance Imaging

Various studies conducted from the mid to late 1990s reported significantly higher sensitivity in breast cancer diagnosis for MRI compared with the other modalities. American Cancer Society guidelines recommend MRI screening as an adjunct to mammography for women who have a lifetime risk of 20-25% or greater. It is demonstrated by several studies that MRI has higher sensitivity in determining small tumors compared with mammography (12). The exceptional ability of MRI in detecting cancers and in identifying small tumors compared to other modalities is the reason for the increasing popularity of this technology as a supplement in breast cancer diagnosis. MRI screening is limited only for the patients with high risk of breast cancer because of its high cost and the requirement for intravenous contrast injection. Claustrophobia also reduces the tolerance of the patients to imaging process(13).
2.2.4 PET Imaging

Positron Emission Tomography is a radionuclide imaging technique used in management of various malignancies and images the tissue based on its metabolic activity. It was initially developed to observe the functional changes in the brain by looking at the brain’s biochemical activities. Lately PET is being used to diagnose various malignancies. Pet imaging is done by injecting the patient with a radionuclide such as F-18 Flouro-deoxyglucose, a radiopharmaceutical that is preferentially metabolized by cancer cells. The F-18 nuclei are proton rich and emit positrons which have a short life. After travelling a few millimeters positrons ($\beta^+$) interact with tissue electrons ($\beta^-$) resulting in two 511 KeV annihilation photons which are released at 180° to one another. These gamma photons are then detected by the PET cameras (14).

Malignant tissue has a higher metabolic rate compared to the adjacent healthy tissue and this is targeted by PET using a radiopharmaceutical like 2-[18F] flouro-2-deoxy-D-glucose (FDG) which is glucose analog. FDG- PET works by providing functional information about the tissue compared with the anatomic details given by the other modalities. PET- FDG is used to detect malignancies in the lung, brain, head and neck, colon and breast. PET has high sensitivity to detect breast cancer(15). FDG is widely used because breast cancer is avid of FDG and it has a comparatively long physical life. FDG-PET is found to be effective in patients who have ambiguous mammographies(5).

A study conducted by Noh D-Y et al. for determining the diagnostic value of PET in detecting breast cancer reported that PET has high sensitivity for breast cancer and can be used as an accurate diagnostic tool. PET displayed excellent diagnostic accuracy in detecting primary tumor mass (97%) in comparison with physical examination (78%) and mammography (67%). As a part of this study 27 patients have undergone breast operations based on PET results from June 1995 to November 1996. For axillary lymph node metastasis PET had a 96% accuracy compared with physical examination (74%) and mammography (60%) (15).
PET has a promising role in detecting distant metastasis and recurrence of breast cancer. PET is also proved to be helpful in prognosis and in understanding a patient’s response to the treatment. This would help to make a decision on the treatment methods to be followed for the patient. The role of PET in breast cancer management is briefly discussed in the following sections.

2.2.4.1 Early Stage Breast Cancer Diagnosis

The role of FDG-PET in determining breast cancer in early stages is limited due to its limited ability to identify small lesions and the high costs associated(16). In one of the studies conducted by Avril et al it was observed that zero were detected out of four tumors with size less than 0.5 cm while one out of eight tumors was identified for tumors with sizes of 0.5 cm to 1.0 cm. Diagnostic accuracy of FDG-PET increased with the tumor size from 68.2 % (tumor size ≤ 2.0 cm) to 91.9%(tumor size>2-5.0 cm) and reached 100% for tumors with size greater than 5 cm(17).

2.2.4.2 Breast Positron Emission Mammography

Positron Emission Mammography (PEM) is a technique where PET results are integrated with the results obtained from conventional mammography. PEM can detect smaller lesions unlike whole body PET and provides better visualization of dense breasts and breasts with fibrocystic disease (16).
2.2.4.3 Axillary Lymph Node Staging

Axillary lymph node involvement is an important factor which affects the treatment selection and prognosis at localized level. Nuclear medicine technologies have gained popularity in detecting axillary lymph node involvement due to limitations of non nuclear methods. It is reported that FDG-PET gives equally good results as sentinel lymph node (SLN) biopsy in identifying the status of lymph nodes when the surgery is performed by a well trained surgeon (18)(15)(19). It is seen from Table 1 that the sensitivity of PET in detecting axillary node involvement varies widely from 25% to 90% while the specificity is around 80% to 100%. The role of FDG-PET in axillary lymph node staging seems to be increasing but axillary lymph node dissection is followed as a standard procedure at this point due to its better accuracy and sensitivity (16).

Table 1: Axillary Lymph Node Staging in Patients with Early Stage Breast Cancer (16)

<table>
<thead>
<tr>
<th>Study</th>
<th>N</th>
<th>Sensitivity</th>
<th>Specificity</th>
<th>Author’s Conclusions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wahl et al(20)</td>
<td>308</td>
<td>61%</td>
<td>80%</td>
<td>Multiple intense foci of PET uptake are predictive for nodal involvement</td>
</tr>
<tr>
<td>Veronesi et al(21)</td>
<td>236</td>
<td>37%</td>
<td>96%</td>
<td>PET-positive axilla should have an axillary lymph node dissection for axillary staging</td>
</tr>
<tr>
<td>Van der hoeven et al(22)</td>
<td>70</td>
<td>25%</td>
<td>97%</td>
<td>Low sensitivity; uptake was related to axillary tumor load</td>
</tr>
<tr>
<td>Avril et al(23)</td>
<td>51</td>
<td>79%</td>
<td>96%</td>
<td>Better detection of axillary nodes in tumors&gt;2.0 cm</td>
</tr>
<tr>
<td>Chung et al(24)</td>
<td>51</td>
<td>60%</td>
<td>100%</td>
<td>Patients with an uptake value &gt; 2.3 had axillary metastases.</td>
</tr>
<tr>
<td>Smith et al(25)</td>
<td>50</td>
<td>90%</td>
<td>97%</td>
<td>PET may obviate the need for axillary surgery in women with small primary tumors</td>
</tr>
</tbody>
</table>
2.2.4.4 Distant Metastases

PET has great potential in detecting distant metastases and recurrence of breast cancer as shown in Figure 1. It is considered to be a powerful imaging modality as the whole body can be diagnosed and staging of the tumor can be done in single procedure. PET plays a promising role in evaluating visceral lesions (liver, lung, distant lymph nodes) and bone metastases (26) (18). FDG-PET is superior to the conventional imaging modalities in tumor localization as it can significantly detect more lesions at different sites in the body with a single examination. It is known from different studies that FDG-PET is successful in diagnosing a significant number of metastases which would have been missed or incorrectly diagnosed by other modalities like CT/US/MRI/bone scintigraph as in Figure 2(5). Different studies confirm that PET has a significant role to play in defining the extent of disease and in making a decision regarding the treatment of patients with advanced breast cancer. Table 2 shows the results from different studies which have been done to evaluate the role of PET in detecting distant metastasis.

Figure 1: PET scan showing locally advanced right breast cancer with axillary metastasis (11)
Figure 2: FDG-PET detecting liver metastasis. The woman with breast cancer has been treated with surgery and radiotherapy. During the follow-up US detected a suspicious hepatic nodule that was described as a benign hemangioma by CT. FDG-PET showed intense uptake of FDG within the mass correctly suggesting a liver metastasis (5).

Table 2: Use of PET in Breast Cancer Patients with Distant Metastasis.(16).

<table>
<thead>
<tr>
<th>Study</th>
<th>N</th>
<th>Sensitivity</th>
<th>Specificity</th>
<th>Author's Conclusions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gallowitsch et al,</td>
<td>62</td>
<td>97%</td>
<td>82%</td>
<td>In clinically suspicious cases with negative tumor marker, PET was reliable in detecting metastasis</td>
</tr>
<tr>
<td>(27)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Eubank et al,</td>
<td>61</td>
<td>94%</td>
<td>91%</td>
<td>PET altered the therapeutic plan in 32% of patients</td>
</tr>
<tr>
<td>(28)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Fueger et al,</td>
<td>58</td>
<td>94%</td>
<td>84%</td>
<td>Compared PET/CT with PET alone and found equivalent results</td>
</tr>
<tr>
<td>(29)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Weir et al,</td>
<td>27</td>
<td>89%</td>
<td>88%</td>
<td>Distant metastases were demonstrated in 30% of patients who were thought only to have loco regional recurrence</td>
</tr>
<tr>
<td>(30)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ladheer et al,</td>
<td>25</td>
<td>95%</td>
<td>20%</td>
<td>In primary breast cancer setting, patient management was changed for 5 women</td>
</tr>
<tr>
<td>(31)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
2.2.4.5  **Response to Therapy**

FDG-PET can measure the metabolic activity of the tumors. It is widely known that metabolic response of the tumor is prior to the physical changes in dimensions which can be measured by the standard imaging modalities like CT, MRI etc. This is because the treatment given to the patient first affects the metabolism of the cancer cells and only at a later stage the tumor size. Decrease in FDG uptake is considered as the treatment being responsive while an increase in FDG uptake is considered as tumor progression and non-response to treatment. Other radiopharmaceuticals like $^{11}$C-labeled methionine (MET) and $^{11}$C-labeled tyrosine (TYR) have been used as alternatives to FDG to evaluate the response after therapy (5)(18).

2.3  **Justification of PET**

The role of PET in breast cancer management is evolving. FDG-PET has great potential to differentiate the cancer cells from the healthy tissue. The large number of clinical studies conducted proves that PET is highly sensitive to breast cancer and FDG-PET has an excellent role to play in diagnosing breast cancer. As explained above FDG-PET contribution in axillary lymph node staging is being explored while it is superior to traditional imaging modalities in diagnosing distant metastasis. FDG-PET is also useful in monitoring the therapy response of a patient. FDG-PET has a great potential in reducing the mortality due to breast cancer and has a wide range of applications in breast cancer management. Development of the dual modality PET/optical imager to assess the margins of the excised breast tissue is an attempt to utilize the potential of FDG-PET in decreasing the rate of positive margins and minimize the wait time during the surgery. This may also lead to a decrease in the number of resections required in the follow-up surgeries which is due to the inadequate margin definition during the initial surgery.
2.4 Margin Assessment Methods

2.4.1 Current Status

In 11-60% of the lumpectomy surgeries, a second surgery is required for complete tumor resection (32). In order to evaluate the size of the tumor, a mammogram of the breast is performed. Preoperative wire localization has been the standard procedure to guide the surgeon for tumor resection for small and nonpalpable lesions. The tumor areas are marked under the guidance of the wire. Once the wire is inserted the surgeon uses the mammogram to estimate the breast tissue to be removed and the depth of the tumor relative to the entry site of the wire. The tumor with an acceptable margin is excised from the patient’s breast. After the surgery a mammogram or US is taken of the specimen to ensure complete resection or negative margins. If the margins are positive resection is done during the same time or as a separate procedure (32).

According to a survey conducted by S. L. Blair et al (33), the current surgical practices followed by the surgeons to achieve negative margins are highly varied and there is no standardized procedure. The issue of margin analysis remains controversial and is to be addressed for minimizing the rate of local recurrence and the number of re-excisions. Very few surgeons did intraoperative margin assessment while only 48% did pathological margin examination. Margin assessment methods like frozen section analysis or imprint cytology are rarely done. The definition of acceptable or negative margins differed with surgeons. Table 3 shows the results of the survey and the large variation in the definition of acceptable margins. The first column in the table gives the acceptable minimum margins while the second column gives the percentage of surgeons who accept the respective margins.

<table>
<thead>
<tr>
<th>Negative Margins</th>
<th>Percentage of Surgeons</th>
</tr>
</thead>
<tbody>
<tr>
<td>Any negative margin</td>
<td>50%</td>
</tr>
<tr>
<td>1-mm</td>
<td>28%</td>
</tr>
<tr>
<td>2-mm</td>
<td>50%</td>
</tr>
<tr>
<td>5-mm</td>
<td>12%</td>
</tr>
<tr>
<td>10-mm</td>
<td>3%</td>
</tr>
</tbody>
</table>
2.4.2 Other Potential Approaches

A study conducted by Mendez JE (7) reports that margin assessment methods followed by the surgeon may alter the results thereby affecting re-excisions, treatment plan and the cosmetic outcome. Many studies show that local recurrence of cancer is at a higher rate for patients with positive margins compared to the patients with negative margins. A few of the practiced margin assessment methods are discussed in this section.

DeJean P et al (32) conducted a study to analyze an intraoperative 3D ultrasound system for tumor margin determination in breast conservation therapy. They have developed a portable, intra-operative, cost-effective 3DUS system to increase the surgical accuracy by providing the tumor geometry relative to the inserted guide wire. They claim that the system has the potential to reduce the number of re-excision surgeries and reduce the operative time for the patient with anesthesia (32).

Another study done at the University of Florida by Camp ER, et al (6) analyzed the rates of re-excisions, locoregional recurrences and survival rates by conducting frozen section analysis of shaved breast tissue from the cavity bed. 1-cm of margin of healthy tissue was considered as negative margin. Frozen section analysis when compared with the permanent margin analysis led to lower re-excision rates though there was no difference in locoregional recurrence rate. Though this technique has advantages in terms of cosmetic outcome and re-excision rates it is time consuming and expensive (6).

Hughes JH et al (34) conducted a multi-site trial of tumor localization using a radioactive seed as an alternative to the standard wire localization procedure. For invasive and in-situ disease margins ≥2 mm were considered as negative margins. Negative margins were achieved in 73% of the radioactive seed localization (RSL) patients compared to 54% in wire localization (WL) patients. A re-excision was done in 8% of the RSL patients versus 25% of WL patients. Results obtained from this trial show that RSL has the potential to reduce the rate of positive margins and decrease the number of second surgeries to be performed (34).
A study conducted by Paredes P et al (35), used a portable intraoperative gamma camera to evaluate the re-excision of non-palpable breast cancer lesions. The patients were injected with 99m Tc-labelled nanocolloid a day before the surgery. The surgery was done under the guidance of a gamma probe and the images of the surgical bed and the excised specimen were taken with the portable gamma camera. Also a 99mTc pointer of 11 MBq was used to visualize the outline of the excised breast tissue. The pointer gave the flexibility to draw an appropriate outline image of the tissue with lower intensity than that of the tumor. The results obtained using the portable gamma camera, were in accordance with the pathological results by 60%. Figure 3 shows the results obtained using the gamma camera (35).

![Figure 3: Images obtained with the portable gamma camera. On the left the image shows the tumor centered inside the specimen. However, on the right, the image clearly demonstrates the close proximity of the tumor to the 3 o’clock margin (35)](image)

As discussed earlier there is no consensus on optimal techniques for margin assessment in breast conservation therapy. The rate of positive margins remains high despite using various strategies. Therefore there is a need to further investigate the margin assessment methods to reduce the number of re-excisions and the rate of positive margins. Hence the current study of development of dual modality PET/Optical imager gains importance as a potential technique to reduce the number of re-excisions and decrease wait time during surgery.
3 Materials and Methods

3.1 Overview of the solution

Dual modality PET /Optical imager is a compact table top/mobile 3D imaging system which uses the dual modalities Positron Emission Tomography and Optical modality for imaging. PET is used to identify the cancerous lesion in the excised breast tissue while optical modality is used to provide the physical outline of the tissue. The margins are evaluated after merging the individual 3D volumes obtained from PET and optical systems. If the margins are less than 5 millimeters it is considered as positive margins are obtained which indicates further resection is required. Alternatively if the margin is greater than 5 millimeters it is considered that negative margins are obtained and the entire cancerous lesion is removed successfully from the patient. Using the Dual modality PET/Optical imager for margin analysis is an intraoperative procedure which can potentially reduce the operating time and the requirement for a second surgery.

Positron Emission Tomography with F-18 Flouro-deoxyglucose (FDG) has proved to play an important role in breast cancer imaging. The patient will be subjected to intravenous injection of FDG before the surgery. Cancer tumors show an increased uptake of FDG which allows them to be imaged in non interventional methods using PET imagers. In a few of the cases, the patient may have a wire inserted into the center of the lesion under the guidance of mammography to provide additional information about the location of the center of the lesion. Using the information from diagnostic imaging and from the wire location the surgeons remove the cancerous lesion. In order to map the specimen orientation the surgeon places one short stitch, at the superior specimen margin, which is marked as a 12 o’ clock reference and 3 o’ clock reference is marked with a long stitch in the same plane which is referred as lateral. Also the excised tissue and the surgical bed may be marked with dyes in order to retain the specimen orientation and for margin analysis. Currently the maximum size of the specimen can be about 3”.

The excised breast tissue is placed in the dual modality PET /Optical imager for margin assessment. It is placed on the specimen tray and rotated by limited angles as required by the PET and Optical 3D reconstruction. The specimen holder is placed in between two planar PET
detectors. The PET cameras image the cancerous lesion in the excised breast tissue. The specimen is rotated from 0 to 180 degrees for PET 3D reconstruction in steps of 10 degrees. The cancerous tissue will typically be identified as a focal area or areas of increased radiotracer accumulation within the excised specimen. Slices are generated from the 3D reconstructed PET images of the cancerous lesion and exported as a binary file.

The PET/Optical imager uses a Prosilica GC-750C camera to do the 3D reconstruction of the physical surface of the excised breast tissue. Optical images of the specimen are obtained after PET acquisition. The specimen tray is made to rotate from 0 to 350 degrees in steps of 10 degrees to collect complete information about the surface of the specimen. A photograph is taken by the camera every 10 degrees. 35 images are taken as the input and 3D reconstruction of the surface is done using Matlab. Slices are generated from the reconstructed 3D point cloud.

Slices obtained from the PET system are merged with their corresponding slices obtained from optical system using a calibration procedure for proper merging. After merging, the slices consist of the physical outline of the excised tissue obtained from the optical modality and the cancerous lesion obtained from the PET modality. The margins are assessed to determine if adequate margins have been obtained or a re-excision is required. The process takes approximately 15 minutes.

3.2 System Design

3.2.1 Key components of the Dual Modality PET/Optical Imager

- One planar PET pair with typically 10cm x 10cm active field of view and ~ 1.0 -3.0 mm intrinsic spatial resolution.
- Prosilica GC 750C color camera
- Flexible LED strip
- Samsung CCTV, 5.5- 33 mm varifocal, manual iris lens
- Velmex rotary table, B4800TS
- Animatics smart motor SM2316D-PLS2
- Petri dish with 5” diameter
- OR-compatible mobile cabinet with shelves, and the PET/optical imager on top, for housing electronics/computers
- Computer(s) with monitor, keyboard and mouse
- Imager signal processing electronics with low voltage and high voltage power supplies
- PET imager data acquisition system (hardware)
- Data acquisition and processing software
- Image reconstruction software, optionally on the second computer
- Medical quality USB/isolation transformer to assure uninterrupted power during surgery and to provide electrical safety buffer

The imager is a table top/mobile compact 3D PET/Optical imaging system. It consists of a pair of detector heads placed on fixtures to maintain constant separation between them, a rotary table and a motor to rotate the specimen, an optical camera to provide the physical outline of the specimen, a LED strip to provide back lighting for optical reconstruction and a specimen holder to hold the specimen. A holder is fixed on the back side of the box to hold the camera and half of the imager top is covered with a transparent lid for easy monitoring while the image process is on. The box is provided with handles for easy handling and portability. The mobile cabinet holds CPU, electronics control box, data acquisition system, UPS/Isolation transformer and has an arm to hold the monitor. The imager is placed on top of the OR-compatible cabinet that supports all the components of the system as shown in Figure 4.
The positions of the camera, PET imagers, rotary table and the specimen holder are as shown in Figure 5. The camera is placed on the back of the box as explained earlier. A hole is drilled on the back wall of the imager to provide an opening for the camera view. The camera is placed such that the camera’s field of view is perpendicular to the PET camera’s field of view. Figure 6 shows the rotary table and the smart motor which are used to rotate the specimen holder.
The excised specimen is placed on a pedestal between two planar PET detectors as shown in Figure 7. The pedestal is used to provide the required elevation to the specimen to keep it within the field of view of the optical camera and the PET detectors. An LED strip is attached on to the walls of the imager to provide back lighting within the box. Figure 8 shows all the views of the imager.
Figure 7: Components of the PET/Optical imager

Figure 8: Images of the PET/Optical Imager. (a) Front View (b) Top View (c) Back View (d) Side View
3.3 PET Modality

The excised specimen with radioactive tracer is placed in the specimen holder between the pair of detectors. The field-of-view of the detectors is approximately 10 cm square. Each PET detector is comprised of 4 by 4 arrays of Hamamatsu R5900-C8 position-sensitive photomultiplier tubes. PSPMTs are coupled to a pixellated array of GSO scintillating crystals with each crystal being 3 mm*3 mm*10 mm. The signals from the PSPMTs are read using readout reduction schemes. A custom built 16-channel FPGA based ADC is used to read the detectors. Image acquisition software is written in Kmax (Sparrow Corporation, Port Orange, FL) which stores the data in the form of event data files. These event data files are exported to the reconstruction software. The PET system uses the program PEM_RECON to perform image reconstruction of the PET detectors by backprojection (laminography) or by the iterative maximum likelihood expectation maximization (MLEM) algorithm. Slices generated at a known distance from the reconstructed 3D image are exported as a binary file. For example slices can be taken at every 1 millimeter or so as required by the user (36).

3.4 Optical Modality

The Optical modality provides the anatomical map of the excised breast tissue. It uses a camera to provide the 3D physical outline of the specimen. The hardware and the software used to perform 3D reconstruction of the specimen are explained in this section.

3.4.1 Hardware

The hardware required for optical reconstruction includes Prosilica GC750C camera, Samsung lens, LED strip, Velmex turn table, Animatics motor and a specimen holder as explained in the previous section. The Prosilica GC750C color camera captures upto 60 frames per second in VGA with an image resolution of 752*480 and square pixels of size 6.0µm*6.0µm. A varifocal lens of 5.5-33M is used along with the camera. LED lights are used to provide backlighting which is important in acquiring the silhouettes of the specimen for optical 3D reconstruction. The specimen holder is placed on the turntable which is in turn connected to the motor. The specimen is made to rotate from 0 to 350 degrees in 10 degree intervals.
3.4.2 Technical Approach, Optical 3D Reconstruction

The basic idea behind the approach used for generating 3D coordinates of the specimen surface is to find the radial (r) and angular (θ) coordinates of the object coordinate system from the camera coordinate system. The angle of rotation of the turn table is considered as the angular coordinate while the radial coordinate is calculated. The Cartesian coordinates X and Z of the object are calculated from the cylindrical coordinates r and θ while Y is calculated from the images. The coordinate systems are shown in Figure 9.

![Diagram showing coordinate systems](image)

**Figure 9: Top view of the DMI showing the object coordinate system**

The reconstruction of the excised breast tissue is done from the multiple silhouettes. The basic principle is to generate a point cloud from the multiple view silhouettes of the specimen. The silhouette is generated by using a strip of LED lights to backlight a translucent screen behind the specimen and adjusting the camera iris manually. The Silhouette is used because the optical modality needs to describe only the physical outline of the excised tissue while the interior details of the tissue can be ignored. Multiple views of the specimen are obtained by rotating the specimen on the turn table while keeping the camera stationary as shown in Figure 10. An image
of the specimen is captured for every 10 degrees while rotating the specimen from 0 to 350 degrees respectively.

Figure 10: Multiple view silhouettes of the specimen taken at different angles

The excised breast tissue is assumed to have a convex surface for the 3D reconstruction. The specimen coordinate system is referred to as the object coordinate system and the optical coordinate system of the camera is called the camera coordinate system. Object coordinates of the physical outline are calculated from the multiple 2D camera images. The Object coordinate system is in millimeters and the camera coordinate system is in pixels. The conversion factor to convert pixels to millimeter is identified by a calibration process. \((X_0, Y_0)\) is the origin of the object coordinate frame. \(X_0\) and \(Y_0\) are identified in the camera coordinate frame by using a calibration process for the AOR (Axis of Rotation). The radial and angular coordinates are calculated from the 2D camera images. The Cartesian coordinates of the object are calculated
with respect to the AOR in the object coordinate system from the cylindrical coordinates. From
the multiple views a point cloud describing the surface of the tissue is obtained. The AOR is
considered as 0 mm (millimeter) and slices are taken consecutively at required distances. The
camera settings should not be changed throughout the entire process which includes the focal
length, the position of the camera and the distance of the camera from the object.

The algorithm applied for 3D surface reconstruction and the slice generation is explained
in the following sections.

3.4.2.1 Pixel to millimeter conversion calibration

The camera pixel to millimeter conversion factor is determined experimentally by linear
transformation. A symmetrical object of known physical dimensions for example a squash ball,
is taken and placed on the AOR on the turn table of the imager. Images of the object are taken
for every 90 degrees from 0 to 360 degrees. The dimension of the squash ball i.e. the diameter is
measured with respect to the object coordinate space using vernier calipers. The diameter of the
squash ball in pixels is calculated with respect to the image coordinate system. The dimensions
obtained from both the coordinate systems are used to find the pixel to millimeter conversion
factor as explained in this section. The pixel to millimeter conversion factor is calculated in both
horizontal (x) and vertical (y) directions and found to be the same, due to the square pixel format
of the camera. The conversion factor is a function of the geometry and the lens settings i.e. the
focal length.

3.4.2.1.1 Algorithm

1. Measure the diameter of the squash ball using vernier calipers. Let the diameter be D mm
   and it is the same in both horizontal and vertical directions.
2. Consider the image at 0 degrees and find the diameter of the squash ball as \( d_{h1} \) pixels in
   the horizontal direction and \( d_{v1} \) pixels in the vertical direction.
3. Repeat step 1 for the remaining three images and find the diameter in the horizontal
direction as \( d_{h2}, d_{h3}, d_{h4} \) pixels and the diameter in the vertical direction as \( d_{v2}, d_{v3}, d_{v4} \) in
   pixels respectively.
4. Calculate the mean diameter in horizontal direction as \( d_{mh} \) pixels of \( d_{h1}, d_{h2}, d_{h3}, d_{h4} \) and
   mean diameter in vertical direction \( d_{mv} \) pixels of \( d_{v1}, d_{v2}, d_{v3}, d_{v4} \)
5. The pixel to millimeter conversion factor in horizontal direction then becomes
\[ D(\text{mm}) = d_{\text{mh}}(\text{pixels}) \]  
\[ \Rightarrow 1(\text{mm}) = \frac{d_{\text{mh}}}{D}(\text{pixels}) \]

\[ \text{Pixel2mm - Factor (horizontal)} = \frac{d_{\text{mh}}}{D}(\text{pixels for 1 mm}) \]  

6. Pixel to millimeter conversion factor in vertical direction

\[ D(\text{mm}) = d_{\text{mv}}(\text{pixels}) \]  
\[ \Rightarrow 1(\text{mm}) = \frac{d_{\text{mv}}}{D}(\text{pixels}) \]

\[ \text{Pixel2mm - Factor (vertical)} = \frac{d_{\text{mv}}}{D}(\text{pixels for 1 mm}) \]  

3.4.2.2 Axis of rotation Calibration

The origin of the object coordinate frame \((X_0, Y_0)\) is identified in the camera coordinate frame. \(X_0\) is the coordinate of the axis of rotation and \(Y_0\) is the coordinate of the top of the pedestal on which the object rests. A calibration procedure is followed to identify \((X_0, Y_0)\) in the camera coordinate system as explained here. A capillary tube filled with food color is placed on the AOR of the turn table as shown in Figure 11. The capillary tube is made to rotate from 0 to 358 degrees with intervals of 2 degrees. An image is taken for every 2 degrees to minimize the error.

3.4.2.2.1 Algorithm

1. Consider the first image and identify the top of the pedestal as \(Y_0\)
2. Change the color image into grayscale and identify the edges of the capillary tube in the image
3. Save the X coordinates of the edges in a matrix as \(X_1, \ldots, X_n\).
4. Calculate the mean of the X coordinates of the edges in the image as \(X_{M1}\)
5. Repeat the steps 2 to 4 for all the images and save the means of X coordinates as \(X_{M1}, X_{M2} \ldots X_{M178}\)
6. \( X_0 \) is the mean of \( X_{M1}, X_{M2} \ldots X_{M178} \)

3.4.2.3 Optical 3D Reconstruction and Slice Generation

The excised specimen to be reconstructed is assumed to be convex. The camera position and the focal length settings should the same as during the calibration procedures. The specimen to be reconstructed is placed on the AOR of the turn table and rotated from 0 to 350 degrees and an image is taken for every 10 degrees. The Pixel to millimeter conversion factor is obtained from the calibration procedure and the AOR is identified in the image coordinate frame from the AOR calibration as \((X_0, Y_0)\). The height at which slices are to be generated from the reconstructed phantom is specified which can typically be 0.5 mm or 1 mm etc. as specified by the end user. The camera coordinate system and the object coordinate systems are as shown in Figure 12 and Figure 13.

Figure 11: Capillary tube with food color

\( Y_0 = 395 \) (pixels)
AOR (X0,Y0) identified in the camera coordinate system

Figure 12: Image coordinate system

AOR (X0,Y0)

Figure 13: Object coordinate system
3.4.2.3.1 Algorithm

1. Initialize
   - conversion factor as Pixel2mm_Factor from the pixel to millimeter calibration procedure
   - AOR as \( (X_0, Y_0) \) from the AOR calibration
   - Degree of Rotation of the turn table as DOR=10 degrees
   - Angle=0 to 350 degrees in steps of DOR
   - Sliceheight=1 mm
   - Threshold= 0.5
   - Number of images as nimg=35 which starts from 0
   - Set the xlimit and y limit to crop the image
     \[
     [r_i, c_i] = \text{size(cropped image)}
     \]

2. FOR \( i=1 \) to length(Angle)
   \[
   C = \cos(Angle(i))
   S = \sin(Angle(i))
   \]
   END FOR

3. FOR \( nn=0 \) to nimg
   - Read Image. A sample of an image taken by the camera at 0 degrees is shown in Figure 14.

![Figure 14: Camera image at 0 degrees](image-url)
• Crop the image. An example of a cropped image at 0 degrees is shown in Figure 15.

\[ [r_i, c_i] = \text{size(cropped image)} \]

![Figure 15: Cropped Image at 0 degrees](image)

• Change the color image to grayscale image
• Detect the edges in the image using the canny edge detection technique with the specified threshold value. Figure 16 shows different images of the specimens taken at 0 degrees, 90 degrees, 180 degrees and 270 degrees with the edges identified.
Figure 16: Edges identified for images taken at different angles

- Considering the AOR \((X_0, Y_0)\) in the image plane as 0 mm find the consecutive y pixel coordinates at 1mm, 2mm etc using the pixel to mm conversion factor

\[
y = \left( Y_0 - (h \times \text{Pixel2mm\_factor}) \right)
\]  
(5)

- Starting from 0 mm find the x and y pixel coordinates on the left and right edges of the AOR
- At the edges compute \(r\) in millimeter as follows

\[
r = \frac{(x - X_0)}{\text{Pixel2mm\_Factor}}
\]  
(6)
• At each point compute X, Y and Z which are in calculated in millimeter

\[ X = r \cdot C(nn + 1) \]  
\[ Z = r \cdot S(nn + 1) \]  
\[ Y = h \]

• Store coordinates as (X, Y, Z) for each image

END FOR

4. A point cloud of the surface coordinates of the object to be reconstructed is obtained where the coordinates are in mm. The front view of the point cloud is shown in Figure 17 and the top view of the point cloud is shown in Figure 18.

![2D Plot of the 3D Reconstructed Point Cloud](image)

Figure 17: Front view of the point cloud
5. Calculate the arc tangent of the Z and X coordinates as below

\[ \theta = \tan^{-1} \frac{Z}{X} \]  \hspace{1cm} (10)

6. Radius of the points on the surface is calculated from the (0,0) as below

\[ \text{Radius} = \sqrt{X^2 + Z^2} \]  \hspace{1cm} (11)

7. Slices are generated from minimum value of Y coordinates to maximum value of Y coordinates respectively.

8. FOR Temp_Var = minimum (Y) to maximum (Y)
   - Find all the points whose Y = Temp_Var and save X, Y, Z, Theta, R of the respective points
   - Theta values range from 0 to 350 degrees. Each theta might have more than one corresponding point. From the set of points available for each theta value select
the point with the minimum radius and save as P. The point cloud corresponding to a particular slice is as shown below. Figure 19 shows the point cloud of the slice at 0 mm.

![Figure 19: Point cloud of the slice at 0 mm](image)

- Countvar1=1
  FOR Points P=1 to length (P)
    - Take two consecutive points \( P_1(X_1, Z_1) \) and \( P_2(X_2, Z_2) \) and calculate the difference between their X and Z coordinates
      \[
      X_{\text{diff}} = \max \{X_1, X_2\} - \min \{X_1 - X_2\}
      \]
      \[
      Z_{\text{diff}} = \max \{Z_1, Z_2\} - \min \{Z_1 - Z_2\}
      \]
    - IF ( \( X_{\text{diff}}>Z_{\text{diff}} \))
      - Fit a polynomial \( p(x) \) of degree 1 to the points and calculate the coefficients.
➢ Values of ‘Z’ are evaluated at different values of X and saved in the matrices as Points_X and Points_Z

ELSE

➢ Fit a polynomial p(z) of degree 1 to the points and calculate the coefficients.
➢ Values of ‘X’ are evaluated at different values of Z and saved in the matrices as Points_X and Points_Z

END

Curve_Coords (countvar1, 1) = Points_X
Curve_Coords (countvar1, 2) = Points_Z

END FOR

• At the end of the above for loop a continuous curve is obtained joining all the individual points and the X and Z coordinates of all the points are saved in the matrix Curve_Coords. Figure 20 shows the slice at 0 mm after the curve fitting is done as explained in the above steps.
Figure 20: Slice at 0 mm after the curve fitting

- Change the X and Z coordinates saved in Curve_Coords from millimeters to pixels and translate the X coordinates by $X_0$ and Z coordinates by $(r_1/2)$

$$XZ = Curve\_Coords \times Pixel2mm\_Factor$$  \hspace{1cm} (14)

- Maximum Y is identified as the Last_Slice

$$Last\_Slice = Maximum(Y) \times Pixel2mm\_Factor$$  \hspace{1cm} (15)

- Create an image, IMG1 of size $(r_1, c_1)$ with pixel values as zeros. Fill the pixels with the XZ coordinates in the image with values of 1 such that the image ultimately is a slice with the outline of the phantom placed in the imager. Figure 21 shows the image of the slice at 0mm where the X and Z coordinates are in pixels. X and Z coordinates are converted from millimeter to pixels as the image merging and the display processes use the image file format.
\[ IMG1 = \text{zeros}(r_1, c_1) \]

\[
FOR \ j = 1 \ to \ \text{length}(XZ) \\
\]

\[ IMG1(XZ(j,2), XZ(j,1)) = 1 \]

\[ END \ FOR \]

![Image of the slice at 0 mm after the curve fitting](image)

Figure 21: Image of the slice at 0 mm after the curve fitting

END FOR

9. The optical slices are arranged from bottom to top
10. Slices are generated from the y=Yo to y=1 based on the slice height specified

### 3.5 Image Fusion

The slices obtained from the PET and optical modalities are merged. In order to merge these images properly a calibration procedure is followed. The calibration phantom is made of 4 glass spheres filled with dark colored radioactive solution such that it is visible to both the PET and optical modalities. The phantom is imaged with both the modalities. The centroids of the four spheres are identified in both the optical and PET modalities. Coordinates of the centroids are used to calculate the scaling, translational and rotational
offsets between the two modalities. At the end of the calibration procedure a homogeneous transformation matrix is obtained which is recorded for further use.

A phantom made of latex caulk was constructed and holes were drilled into the phantom. Radioactive beads of 5 mm diameter were inserted into these holes. PET reconstruction was done and the slices were saved in a data file. The PET slices were transformed by the homogeneous transformation matrix obtained from the calibration procedure. Optical reconstruction was done in a similar way as described in the previous section. After the transformation of the PET slices, their coordinates were obtained with respect to the optical coordinate system. As both the physical outline and the radioactive beads were in the same coordinate system, the merged images were generated as explained in the following sections.

### 3.5.1 Calibration

The calibration phantom consists of four glass spheres held on glass rods as shown in Figure 22. These spheres are filled with the radionuclide FDG mixed with a dark food color. The radioactive nature of the liquid makes it visible to the PET cameras and the dark color helps in easy identification for the optical modality. The four spheres which are of different sizes and heights are placed on the turn table. Different heights are chosen for each sphere for easy identification of the spheres in both the modalities.

The coordinates of the centroids of the spheres are calculated to be \((X_{op}, Y_{op}, Z_{op})\) in the optical system and \((X_p, Y_p, Z_p)\) in the PET system. Sixteen unknowns are present while finding the homogeneous transformation matrix. In order to find sixteen unknowns it is necessary to have multiple images of the four spheres.
3.5.1.1 Identification of the centroids in optical modality

In the calibration phantom the spheres do not lie on the AOR so the degree of rotation is not known, but the difference in degree of rotation between successive images is known. An image of the four spheres where all of them are clearly visible is considered as a reference image and the angle is referred as ‘Theta’. Two more images are considered whose degree of rotation from the reference image is known and referred as ‘Theta1’ and ‘Theta2’ respectively. Spheres are numbered 1 to 4 in descending order of their heights.

In order to minimize the error three sets of images are taken and the coordinates of the centroids of the spheres are an average obtained from the three sets. At least three images are required in one set to find the centroids of the spheres. The process of finding the coordinates of the centroids for one set of images is explained below.

3.5.1.1.1 Algorithm

1. Initialize

   - AOR as \((X_0,Y_0)\) from the AOR calibration
   - Difference in degree of rotation of the first image from the reference image as Theta1 ‘\(\theta_1\)’
• Difference in degree of rotation of the second image from the reference image as 
  \( \Theta_2 \)

2. Read the reference image

3. Crop the reference image

\[
[r_1, c_1] = \text{size(cropped image)}
\]

4. Identify the edges of the spheres alone in the image. Figure 23 shows the images of the spheres with their edges identified.

5. Find the centroid of the sphere1 as \( \text{Centroid}_X \) and find the respective \( Y \) coordinate as \( Y \)

6. Calculate the distance of the centroids of all the spheres from \( X_0 \) and save it as

\[
a_{Sp1} = \text{Centroid}_X X_{Sp1} - X_0
\]
7. Repeat steps 5 and 6 for the remaining spheres such that \( a_2 \text{ _Sp}_2, a_3 \text{ _Sp}_3, a_4 \text{ _Sp}_4 \) are obtained for the four spheres.

8. Repeat steps 2 to 7 for image 1 and image 2 such that \( a_1 \text{ _Sp}_1, a_2 \text{ _Sp}_2, a_3 \text{ _Sp}_3, a_4 \text{ _Sp}_4 \) for image 1 and \( a_1 \text{ _Sp}_1, a_2 \text{ _Sp}_2, a_3 \text{ _Sp}_3, a_4 \text{ _Sp}_4 \) for image 2 are calculated.

9. Calculate radius \( R \text{ _Sp}_1 \) for sphere 1 in the reference image as below where \( R \text{ _Sp}_1 \) and \( \theta \text{ _Sp}_1 \) are unknown:

\[
R \text{ _Sp}_1 = \frac{a \text{ _Sp}_1}{\cos(\theta \text{ _Sp}_1)} \tag{17}
\]

10. Calculate radius \( R \text{ _Sp}_1 \) for sphere 1 in image 1 as below where \( \theta_1 \text{ _Sp}_1 \) is known and \( R \text{ _Sp}_1 \) is unknown:

\[
R \text{ _Sp}_1 = \frac{a \text{ _Sp}_1}{\cos(\theta \text{ _Sp}_1 + \theta_1 \text{ _Sp}_1)} \tag{18}
\]

11. Calculate radius \( R \text{ _Sp}_1 \) for sphere 1 in image 2 as below where \( \theta_2 \text{ _Sp}_1 \) is known and \( R \text{ _Sp}_1 \) is unknown:

\[
R \text{ _Sp}_1 = \frac{a \text{ _Sp}_1}{\cos(\theta \text{ _Sp}_1 + \theta_2 \text{ _Sp}_1)} \tag{19}
\]

12. From equation (18) and equation (19) solve for \( \theta \text{ _Sp}_1 \) as below:

\[
\frac{a \text{ _Sp}_1}{\cos(\theta \text{ _Sp}_1 + \theta_1 \text{ _Sp}_1)} = \frac{a \text{ _Sp}_1}{\cos(\theta \text{ _Sp}_1 + \theta_2 \text{ _Sp}_1)} \tag{20}
\]
\[
\theta_{-Sp_1} = \arctan \left( \frac{(a1_{-Sp_1} \cos(\theta2_{-Sp_1})) - (a2_{-Sp_1} \cos(\theta1_{-Sp_1}))}{(a1_{-Sp_1} \sin(\theta2_{-Sp_1})) - (a2_{-Sp_1} \sin(\theta1_{-Sp_1}))} \right) 
\]

(21)

13. From equation (19) calculate \( R_{-Sp_1} \) using the value of \( \theta_{-Sp_1} \) obtained from equation (21).

14. Find X, Y and Z coordinates of the centroid for sphere 1 as below

\[
X_{op_{-Sp_1}} = R_{-Sp_1} \cos(\theta_{-Sp_1}) + X_0
\]

(22)

\[
Y_{op_{-Sp_1}} = Y_{-Sp_1}
\]

(23)

\[
Z_{op_{-Sp_1}} = (R_{-Sp_1} \sin(\theta_{-Sp_1})) + \frac{r}{2}
\]

(24)

15. Repeat steps 9 to 14 for the remaining three spheres to calculate X, Y and Z coordinates.

### 3.5.2 Homogeneous Coordinate Transformation

#### 3.5.2.1 Theory

- A vector is represented as a matrix

\[
\vec{p} = \begin{bmatrix}
\dot{a}_x \\
\dot{b}_y \\
\dot{c}_z
\end{bmatrix}
\]

- Homogeneous matrix is represented as below

\[
\begin{bmatrix}
\dot{a}_x & \dot{b}_x & \dot{c}_x & \dot{d}_x \\
\dot{a}_y & \dot{b}_y & \dot{c}_y & \dot{d}_y \\
\dot{a}_z & \dot{b}_z & \dot{c}_z & \dot{d}_z \\
0 & 0 & 0 & 1
\end{bmatrix}
\]
• In the above matrix the following part of the matrix represents the rotations about X, Y and Z axes

\[
\begin{bmatrix}
  a_x & b_x & c_x \\
  a_y & b_y & c_y \\
  a_z & b_z & c_z \\
\end{bmatrix}
\]

• The last column of the homogeneous matrix represents the translation

\[
\begin{bmatrix}
  d_x \\
  d_y \\
  d_z \\
\end{bmatrix}
\]

• The fourth row is added to combine the rotations and translations into a single 4*4 matrix.

3.5.2.1.1 Scale Transformations
• Non Uniform Scaling scales the object along X, Y and Z axes by \(s_x\), \(s_y\) and \(s_z\) factor respectively.

\[
S_n(s) = \begin{bmatrix}
  s_x & 0 & 0 & 0 \\
  0 & s_y & 0 & 0 \\
  0 & 0 & s_z & 0 \\
  0 & 0 & 0 & 1 \\
\end{bmatrix}
\]

• The entire object is scaled by a factor of \(S\) by using a uniform scaling matrix

\[
S_u(s) = \begin{bmatrix}
  s & 0 & 0 & 0 \\
  0 & s & 0 & 0 \\
  0 & 0 & s & 0 \\
  0 & 0 & 0 & 1 \\
\end{bmatrix}
\]
3.5.2.1.2 Rotation Matrices

\[ R_x(\theta) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \]

\[ R_y(\theta) = \begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \]

\[ R_z(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \]

3.5.2.1.3 Translation Matrix

A translation matrix that translates an object by vector \( r \) is as shown below

\[ T(r) = \begin{bmatrix} 1 & 0 & 0 & r_x \\ 0 & 1 & 0 & r_y \\ 0 & 0 & 1 & r_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \]

3.5.2.1.4 General Combination Matrix

A sequence of translations, scalings, rotations and shears can be combined to form a single matrix. The order in which the rotations, scaling and translations are done is important. All the matrices explained above have the last row of the form \([0 0 0 1]\). When any two matrices of this form are multiplied the resulting matrix will also be of the same form \([0 0 0 1]\). The single matrix is as follows:

\[ V' = MV \]

(25)
\[
\begin{bmatrix}
V_x' \\
V_y' \\
V_z' \\
1
\end{bmatrix}
= \begin{bmatrix}
a_1 & b_1 & c_1 & d_1 \\
a_2 & b_2 & c_2 & d_2 \\
a_3 & b_3 & c_3 & d_3 \\
0 & 0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
V_x \\
V_y \\
V_z \\
1
\end{bmatrix}
\]  
(26)

\[
V_x' = a_1 V_x + b_1 V_y + c_1 V_z + d_1 \\
V_y' = a_2 V_x + b_2 V_y + c_2 V_z + d_2 \\
V_z' = a_3 V_x + b_3 V_y + c_3 V_z + d_3 \\
1 = 0V_x + 0V_y + 0V_z + 1
\]

3.5.2.2 Implementation to the current problem

The centroids of the four spheres are identified in the optical and PET modalities. The optical coordinates of the centroids of the four spheres are obtained from the calibration procedure as \((X_{op1}, Y_{op1}, Z_{op1})\), \((X_{op2}, Y_{op2}, Z_{op2})\), \((X_{op3}, Y_{op3}, Z_{op3})\), \((X_{op4}, Y_{op4}, Z_{op4})\). The PET coordinates of the centroids of the spheres are \((X_{p1}, Y_{p1}, Z_{p1})\), \((X_{p2}, Y_{p2}, Z_{p2})\), \((X_{p3}, Y_{p3}, Z_{p3})\), \((X_{p4}, Y_{p4}, Z_{p4})\). Optical coordinates are represented by V, PET coordinates are represented by V’ and the combination matrix by M as shown in equation(25). The combination matrix is calculated from the coordinates of the four spheres obtained from both the modalities using the Gaussian elimination method. The procedure followed to find the matrix M is explained in this section:

\[
\begin{bmatrix}
X_{op1} \\
Y_{op1} \\
Z_{op1} \\
1
\end{bmatrix}
= \begin{bmatrix}
a_1 & b_1 & c_1 & d_1 \\
a_2 & b_2 & c_2 & d_2 \\
a_3 & b_3 & c_3 & d_3 \\
0 & 0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
X_{p1} \\
Y_{p1} \\
Z_{p1} \\
1
\end{bmatrix}
\]  
(27)

\[
\begin{bmatrix}
X_{op2} \\
Y_{op2} \\
Z_{op2} \\
1
\end{bmatrix}
= \begin{bmatrix}
a_1 & b_1 & c_1 & d_1 \\
a_2 & b_2 & c_2 & d_2 \\
a_3 & b_3 & c_3 & d_3 \\
0 & 0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
X_{p2} \\
Y_{p2} \\
Z_{p2} \\
1
\end{bmatrix}
\]  
(28)
From equations (27), (28), (29) and (30)

\[
X_{op1} = a_1X_{p1} + b_1Y_{p1} + c_1Z_{p1} + d_1
\]  
(31)

\[
Y_{op1} = a_2X_{p1} + b_2Y_{p1} + c_2Z_{p1} + d_2
\]  
(32)

\[
Z_{op1} = a_3X_{p1} + b_3Y_{p1} + c_3Z_{p1} + d_3
\]  
(33)

\[
X_{op2} = a_1X_{p2} + b_1Y_{p2} + c_1Z_{p2} + d_1
\]  
(34)

\[
Y_{op2} = a_2X_{p2} + b_2Y_{p2} + c_2Z_{p2} + d_2
\]  
(35)

\[
Z_{op2} = a_3X_{p2} + b_3Y_{p2} + c_3Z_{p2} + d_3
\]  
(36)

\[
X_{op3} = a_1X_{p3} + b_1Y_{p3} + c_1Z_{p3} + d_1
\]  
(37)

\[
Y_{op3} = a_2X_{p3} + b_2Y_{p3} + c_2Z_{p3} + d_2
\]  
(38)

\[
Z_{op3} = a_3X_{p3} + b_3Y_{p3} + c_3Z_{p3} + d_3
\]  
(39)

\[
X_{op4} = a_1X_{p4} + b_1Y_{p4} + c_1Z_{p4} + d_1
\]  
(40)

\[
Y_{op4} = a_2X_{p4} + b_2Y_{p4} + c_2Z_{p4} + d_2
\]  
(41)

\[
Z_{op4} = a_3X_{p4} + b_3Y_{p4} + c_3Z_{p4} + d_3
\]  
(42)
Equations 7, 10, 13, 16 can be written as

\[
\begin{bmatrix}
X_{op1} \\
X_{op2} \\
X_{op3} \\
X_{op4}
\end{bmatrix} =
\begin{bmatrix}
X_{p1} & Y_{p1} & Z_{p1} & 1 \\
X_{p2} & Y_{p2} & Z_{p2} & 1 \\
X_{p3} & Y_{p3} & Z_{p3} & 1 \\
X_{p4} & Y_{p4} & Z_{p4} & 1
\end{bmatrix}
\begin{bmatrix}
a_1 \\
b_1 \\
c_1 \\
d_1
\end{bmatrix}
\]

(43)

Similarly equations 8, 11, 14, 17 can be written as

\[
\begin{bmatrix}
Y_{op1} \\
Y_{op2} \\
Y_{op3} \\
Y_{op4}
\end{bmatrix} =
\begin{bmatrix}
X_{p1} & Y_{p1} & Z_{p1} & 1 \\
X_{p2} & Y_{p2} & Z_{p2} & 1 \\
X_{p3} & Y_{p3} & Z_{p3} & 1 \\
X_{p4} & Y_{p4} & Z_{p4} & 1
\end{bmatrix}
\begin{bmatrix}
a_2 \\
b_2 \\
c_2 \\
d_2
\end{bmatrix}
\]

(44)

Equations 9, 12, 16, 19 can be written as

\[
\begin{bmatrix}
Z_{op1} \\
Z_{op2} \\
Z_{op3} \\
Z_{op4}
\end{bmatrix} =
\begin{bmatrix}
X_{p1} & Y_{p1} & Z_{p1} & 1 \\
X_{p2} & Y_{p2} & Z_{p2} & 1 \\
X_{p3} & Y_{p3} & Z_{p3} & 1 \\
X_{p4} & Y_{p4} & Z_{p4} & 1
\end{bmatrix}
\begin{bmatrix}
a_3 \\
b_3 \\
c_3 \\
d_3
\end{bmatrix}
\]

(45)

Let

\[
PET =
\begin{bmatrix}
X_{p1} & Y_{p1} & Z_{p1} \\
X_{p2} & Y_{p2} & Z_{p2} \\
X_{p3} & Y_{p3} & Z_{p3} \\
X_{p4} & Y_{p4} & Z_{p4}
\end{bmatrix}
\]

\[
\text{optical } X =
\begin{bmatrix}
X_{op1} \\
X_{op2} \\
X_{op3} \\
X_{op4}
\end{bmatrix}
\]
optical \_Y = \begin{bmatrix} Y_{op1} \\ Y_{op2} \\ Y_{op3} \\ Y_{op4} \end{bmatrix}

optical \_Z = \begin{bmatrix} Z_{op1} \\ Z_{op2} \\ Z_{op3} \\ Z_{op4} \end{bmatrix}

and \ A_1 = \begin{bmatrix} a_1 \\ b_1 \\ c_1 \\ d_1 \end{bmatrix}, \quad A_2 = \begin{bmatrix} a_2 \\ b_2 \\ c_2 \\ d_2 \end{bmatrix}, \quad A_3 = \begin{bmatrix} a_3 \\ b_3 \\ c_3 \\ d_3 \end{bmatrix}

From the above equations the combination matrix can be calculated following the Gaussian elimination method as explained below.

\[ A_1 = \frac{PET}{Optical \_X} \]
\[ A_2 = \frac{PET}{Optical \_Y} \]
\[ A_3 = \frac{PET}{Optical \_Z} \]
\[ A_4 = [0 \ 0 \ 0 \ 1] \]

Therefore combination matrix

\[ T = \begin{bmatrix} A_1' \\ A_2' \\ A_3' \\ A_4' \end{bmatrix} \]

Which means?
$$T = \begin{bmatrix} a_1 & b_1 & c_1 & d_1 \\ a_2 & b_2 & c_2 & d_2 \\ a_3 & b_3 & c_3 & d_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$ (46)

### 3.5.3 Image Fusion with Phantom

The PET slices of the phantom are transformed by the combination matrix shown in equation 19. PET slices show the radioactivity identified in the phantom as a white blob on black background.

After transformation, the coordinates of the PET slices are obtained with respect to the optical coordinate system. The PET and optical slices with the same Y coordinates i.e. the same slices are identified. The respective X and Z coordinates for a particular image of a slice are filled with the pixel values of 1.

1. Initialize
   - nimg\_PET = 60
   - Last\_Slice, identified in the optical reconstruction as the last slice
2. FOR 1: nimg\_PET
   - Read the image
     - Change the image to binary image
     - Initialize PET\_X= [ ] as an empty matrix
     - Identify the X and Z coordinates of the activity in the slices as PET\_X and PET\_Z
       - PET\_X=column pixel coordinate

![Figure 24: PET slice](image-url)
PET_Z = row pixel coordinate

- IF PET_X is empty
  Continue;
End

- Save PET_X, PET_Y and PET_Z coordinates in PET_Coords where PET_Y is the slice number

- Multiply PET_Coords by the matrix T as in equation (46).
  \[
  \text{PET\_Trans\_Coords} = \text{PET\_Coords} \times T
  \]

- Save the PET_Trans_Coords of all the images where activity is present as PET_coordmatrix

END FOR

- Identify the corresponding optical slices and fill the pixels of respective IMG1 with the PET_Trans_Coords
  - FOR j = 1 to length (PET_Trans_Coords)
    \[
    \text{IMG1} (\text{PET\_Trans\_Coords} (j, 3), \text{PET\_Trans\_Coords} (j, 1)) = 1
    \]
  END FOR

- A sample of merged slice is shown in Figure 25.
3.6 Margin Evaluation

Stitches are placed at 12 o’ clock reference and 3 o’ clock reference which are called as superior and lateral as per the margin assessment method. Margins are evaluated in the superior, lateral, medial, anterior and posterior directions in a standard type of margin assessment method which is identified by 6 different colors as shown in Figure 27.

In the current scenario, the points on the radioactive blob were identified in the superior, lateral, medial and inferior directions. The distance between these points and the points on the edges is measured and checked if it is less than 5 mm or greater than 5mm. The distance between these points is called the margin. If the margin is less than 5 mm then it is considered a positive margin and if it is greater than 5 mm then it is considered a negative margin. Figure 26 shows the image of an excised breast tissue with the margins marked in different colors. The margins are assessed in the specified directions. Let the points on the blob for a slice be represented by (x, z) and the points on the edge be represented by (X, Z). The distance between these points is calculated as below:

1. \[ \text{Margin} = \sqrt{(X - x)^2 + (Z - z)^2} \]
2. If Margin > 5 mm

    Display (‘Negative Margins’)

Else if Margin < 5 mm

    Display (‘Positive Margins’)

End

Figure 26: Margins in an excised breast tissue
Figure 27: Margin Assessment Method (7)
4 Results and Discussion

This chapter includes the experiments performed to ensure the correctness and accuracy of the algorithm. Various phantoms of different shapes were used which were similar to the real excised breast tissue. Different calibration procedures were followed and the corresponding results are discussed here.

4.1 Calibration Procedures

4.1.1 Pixel to Millimeter Calibration

A squash ball of known dimensions was used to perform the millimeter to pixel calibration. The pixel to mm conversion factor was found to be the same in both horizontal and vertical directions.

\[
\text{Pixel2mm\_Factor(Vertical) = Pixel2mm\_Factor(Horizontal)}
\]

The Pixel2mm_Factor was found to be 4.8 pixels for 1 mm for that particular focal length of the lens used and the camera position. The Pixel2mm_Factor varies with the change in focal length and the position of the camera.

4.1.2 Axis of rotation Calibration

The images were cropped to 400* 400 resolution and \(X_0\) and \(Y_0\) were identified as (215,395) in the image coordinate system using the procedure explained in the section 3.4.2.2.

4.1.3 Calibration for Image Fusion

Figure 22 shows the calibration phantom used to find the homogeneous matrix parameters. The procedure is explained in section 3.5. Five sets of camera images were taken to find the centroids of the four spheres in the optical system. Each set consists of three images. An image taken at 20 degrees of the turntable was considered as the reference image for all the sets. The images in which all the four spheres were visible were considered for the analysis. The sets of images were as follows:
Set 1: Reference image at 0 degrees, Image 1 at 40 degrees and Image 2 at 90 degrees

Set 2: Reference image at 0 degrees, Image 1 at 130 degrees and Image 2 at 220 degrees

Set 3: Reference image at 0 degrees, Image 1 at 270 degrees and Image 2 at 310 degrees

Set 4: Reference image at 0 degrees, Image 1 at 310 degrees, Image 2 at 320 degrees

Set 5: Reference image at 0 degrees, Image 1 at 40 degrees, Image 2 at 320 degrees

Table 4 shows the coordinates of the centroids of the four spheres in optical and PET system. Optical coordinates are calculated using the values given in Table 4 while the PET coordinates are read from the PET slices of the calibration phantom.

Table 4: (X, Y, Z) coordinates of the centroids of spheres in optical and PET coordinate systems

<table>
<thead>
<tr>
<th>Sphere</th>
<th>Optical Coordinates</th>
<th>PET Coordinates</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>X</td>
<td>Y</td>
</tr>
<tr>
<td>Sphere 1</td>
<td>195.0000</td>
<td>29.0000</td>
</tr>
<tr>
<td>Sphere 2</td>
<td>259.0000</td>
<td>88.0000</td>
</tr>
<tr>
<td>Sphere 3</td>
<td>301.0000</td>
<td>136.0000</td>
</tr>
<tr>
<td>Sphere 4</td>
<td>128.0000</td>
<td>186.0000</td>
</tr>
</tbody>
</table>

The coordinate homogeneous transformation matrix is calculated from the coordinates of the centroids of the four spheres as explained in the section 3.5.2. The matrix shown below is obtained after the calculations and the PET coordinates are transformed using the homogeneous matrix.

\[
\begin{bmatrix}
3.2298 & 0.1869 & -7.1076 & 333.8395 \\
-0.2989 & 7.5912 & -0.0283 & -41.4722 \\
-7.2029 & -0.4687 & -2.5298 & 511.3700 \\
0 & 0 & 0 & 1
\end{bmatrix}
\]
4.2 Optical 3D Reconstruction and Slice Generation

4.2.1 Digital Phantom

In order to have the proof of concept, an attempt was initially made using a digital phantom. The images of a perfect sphere taken at any interval through the 360 degrees of rotation would be a circle as shown in Figure 28. 35 circles with diameter of 340 pixels in X direction and 339 pixels in Y direction approximately were taken as input. The algorithm to perform the 3D reconstruction of the surface from the 2 dimensional camera images was applied on this digital phantom. The point cloud obtained from the reconstruction procedure is plotted as shown in Figure 29 using a triangular surface plot in Matlab. Figure 30 shows the reconstructed slices of the digital phantom which are at different heights. The slices are taken from Y=0 to Y=1, the end of the image space. The estimated diameter of the reconstructed surface was found to be 340 pixels in X direction, 340 pixels in Y direction and 341 pixels in Z direction. The reconstructed diameter is within ±1 pixel to the original diameter in all the directions. There are slight distortions present in the slices which are due to the curve fitting procedure followed. These distortions can be minimized by taking more number of images with the degree of rotation being lesser than 10 degrees.

Figure 28: Digital Phantom, Circle of Diameter 84 mm
Figure 29: Reconstructed sphere from the point cloud generated from the camera images

Figure 30: Slices of Digital Phantom
4.2.2 Perfect Convex object: Squash Ball

A squash ball of 39.5 mm diameter shown in Figure 31 was taken as a real phantom to check the accuracy of the optical reconstruction. The squash ball was made to rotate from 0 to 350 degrees and images were taken for every 10 degrees interval.

Figure 31: Double Yellow Squash Ball

Several tests were run using different phantoms with convex surfaces. A squash ball was used as an object with a perfect convex surface. The slices obtained after the reconstruction of the squash ball are shown in Figure 32. Slices are shown at different heights. The diameter of the biggest slice from the reconstructed slices was considered as the estimated diameter of the reconstructed surface. Estimated diameter is X=40.5 mm, Y=39 mm and Z = 40.0 mm. The reconstructed diameter is within ±1 mm to the original diameter.

Figure 32: Slices of Squash Ball
4.2.3 Irregular Phantoms of different shapes

Tests with digital phantoms and objects with convex surfaces proved that the system works fine with perfectly convex surfaces. Next an attempt was made to test with phantoms of irregular shapes and sizes. The phantoms were constructed such that they are similar in shape and size to the excised breast tissue. It was taken care that the size of the phantoms was less than 3 inches as the size of the excised breast tissue in lumpectomy would generally be less than 3 inches, according to the oncology surgeon.

4.2.3.1 Phantom 1 with Irregular Surface

Figure 33 shows the phantom that was used to test the reconstruction of an irregular surface. The resolution of the image was (480*621) and the AOR was (317,465). The slice at 0 mm was taken where Y= 465 in pixels. As slices start at Y= 365 pixels the plot in Figure 34 shows that the points in the bottom row are on the axis in one line while the phantom in Figure 33 looks different in the bottom. Figure 34 was compared with Figure 33 to cross check the accuracy of the reconstruction procedure. It is seen that the front views of the phantom are the same before and after the reconstruction.

Figure 35 shows the slices of the phantom in the top view. The slices are taken from Y=Y0 to Y=1, the end of the image space. The size of the slices keeps decreasing from the slice at 0 mm to the slice at 22 mm as it is the case with the phantom shown in Figure 33. The last slice is blank because there is no object present in this part of the image space.
Figure 33: Phantom of Irregular Surface

Figure 34: 3D surface plot of the reconstructed Point Cloud
Figure 35: Slices of Irregular Phantom Shown in Figure 33

4.2.3.2 Phantom 2 with Irregular Surface

Figure 36 shows the phantom 2 used to test the reconstruction of irregular phantoms. Figure 37 is the front view of the phantom in Figure 36 as seen by the camera. Comparing Figure 36 with Figure 37 it can be understood that the 3D reconstructed point cloud is similar to the phantom. There are gaps in between the points because the points are calculated in the steps of one millimeter where each millimeter is equal to 7 pixels. Figure 38 shows the slices which represent the top view of phantom 2. The slices are generated from $Y=Y_0$ to $Y=1$, the end of the image space.
Figure 36: Irregular Phantom 2

Figure 37: 2D Plot of the 3D reconstructed point Cloud of Phantom 2
4.2.3.3 Phantom 3 with irregular surface

Phantom 3 is of a different shape and size when compared to phantoms 1 and 2. Figure 39 shows the phantom 3 used to test the reconstruction of irregular phantoms. Figure 40 is the front view of the phantom 3 as seen by the camera. Comparing Figure 39 with Figure 40 it can be understood that the 3D reconstructed point cloud is similar to the phantom. Figure 41 shows the slices which represent the top view of phantom 2. The slices are generated from \( Y = Y_0 \) to \( Y = 1 \), end of the image space.
Figure 39: Phantom 3 with Irregular Surface

Reconstructed 3D Surface

Figure 40: 2D Plot of 3D Reconstructed Point Cloud of Phantom 3
4.3 Image Fusion

4.3.1 Image Fusion with Phantom

Figure 42 shows the phantom used for image fusion. Three radioactive beads of 5 mm diameter were taken and placed in the phantom. Radioactive beads are visible to the PET cameras while the physical outline of the phantom is visible to the optical camera. The reconstructed slices from both the systems are merged and the result is as shown in Figure 43. Slices are generated from $Y=Y_0$ to $Y=1$ and the last slice is the end of the image space where $Y=1$. 
Figure 42: Phantom used for Image Fusion

Physical Outline of the phantom

Radioactivity

Figure 43: Slices of the Fusion Phantom
In Figure 43 slice at 0 mm has no activity present so only the physical outline of the phantom is shown. In the other slices at 9mm, 12mm and 15mm activity is present and it is shown by the small patches inside the physical outline. The slice at 29mm has no activity so only the physical outline of the phantom is present. The last slice is the top of the image where the object is not present so it is a blank image.

4.3.2 Margin Evaluation

After the slices are merged, the PET points are identified in the superior, medial, inferior and lateral direction. In the same directions optical points are also identified. The distance between the corresponding points is calculated and this distance is the margin. If the margin is greater than 5 mm it is considered a negative margin and if the margin is less than 5 mm it is considered to be a positive margin. Figure 44 shows two slices whose margins are evaluated. The margins in the four directions are represented by four different colors. The superior is represented by red arrow, medial by orange, inferior by blue and lateral by orange respectively. The slice at 6 mm is found to have negative margins in the superior, medial, inferior and lateral directions with the margins being:

- Superior: Negative Margin. The margin is 10 mm
- Inferior: Negative Margin. The margin is 32 mm
- Medial: Negative Margin. The margin is 39 mm
- Lateral: Negative Margin. The margin is 16 mm

The slice at 19 mm is found to have positive margins in the inferior and lateral directions while it has negative margins in superior and medial directions with the margins being:

- Superior: Negative Margin. The margin is 10 mm
- Inferior: Positive margin. The margin is 4 mm
- Medial: Negative Margin. The margin is 23 mm
- Lateral: Positive Margins. The margin is 3 mm
4.4 Error Analysis

4.4.1.1 Intervals in the degree of rotation

A squash ball was taken as the test phantom. Readings were taken by rotating the phantom from 0 to 350 degrees at different intervals. Error analysis was performed for different intervals and the 10 degree interval was selected based on a tradeoff between the total time which is the sum of computation time and data acquisition time and the percentage error. The interval within the 360 degree of rotation was accepted as 10 degree based on the values in

The percentage error is calculated as shown in the Figure 45:
Let

\[ \theta = \text{Angle of rotation} \]
\[ R = \text{Radius of the circle} \]
\[ \Delta R = R - L \]
\[ \Delta R = R \left( 1 - \cos \left( \frac{\theta}{2} \right) \right) \]

\[ \text{PercentageError} = \left( \frac{\Delta R}{R} \right) \times 100 \]

Table 5. It is observed that percentage error increases from 0.004% to 0.381% from 1 degree to 10 degrees while the total time is vice versa. The permissible error limit was considered to be less than or equal to 0.5mm. All the intervals of DOR are found to be within the permissible error limits. Figure 46 shows the tradeoff between the total time and percentage error to be between 4 or 5 degrees. The percentage error for 10 degrees of rotation is 0.308% which is still within the acceptable error limits. As the error is within the acceptable limits and the total time is also within the required time frame of 20 minutes for the whole processing of the dual modality PET/Optical imager.

The percentage error is calculated as shown in the Figure 45:
Figure 45: Error analysis based on degree of rotation

Let

\[ \theta = \text{Angle of rotation} \]
\[ R = \text{Radius of the circle} \]
\[ \Delta R = R - L \]
\[ \Delta R = R \left( 1 - \cos \left( \frac{\theta}{2} \right) \right) \]

\[ \text{Percentage Error} = \left( \frac{\Delta R}{R} \right) \times 100 \]

Table 5: Error Analysis for the intervals of Degree of Rotation

<table>
<thead>
<tr>
<th>Degree of Rotation (Degrees)</th>
<th>Computation Time (min:sec)</th>
<th>Data Acquisition Time (min:sec)</th>
<th>Total Time (min:sec)</th>
<th>Time Error (ΔR/R)*100</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3:89</td>
<td>4:42</td>
<td>8:31</td>
<td>0.004</td>
</tr>
<tr>
<td>2</td>
<td>1:97</td>
<td>2:45</td>
<td>4:42</td>
<td>0.015</td>
</tr>
<tr>
<td>3</td>
<td>1:41</td>
<td>2:05</td>
<td>3:46</td>
<td>0.034</td>
</tr>
<tr>
<td>4</td>
<td>1:11</td>
<td>1:42</td>
<td>2:53</td>
<td>0.061</td>
</tr>
<tr>
<td>5</td>
<td>1:02</td>
<td>1:32</td>
<td>2:34</td>
<td>0.095</td>
</tr>
<tr>
<td>6</td>
<td>0:49</td>
<td>1:24</td>
<td>1:73</td>
<td>0.137</td>
</tr>
<tr>
<td>8</td>
<td>0:39</td>
<td>1:15</td>
<td>1:54</td>
<td>0.244</td>
</tr>
<tr>
<td>9</td>
<td>0:39</td>
<td>1:12</td>
<td>1:51</td>
<td>0.308</td>
</tr>
<tr>
<td>10</td>
<td>0:34</td>
<td>1:10</td>
<td>1:44</td>
<td>0.381</td>
</tr>
</tbody>
</table>
Figure 46: Angle of Rotation versus Total time and Percentage Error
5 Conclusions and Future Study

5.1 Conclusion from the Experimental Results

Margin assessment procedures play an important role in determining the success rate of lumpectomy breast cancer surgeries. This has led to the development of a dual modality margin specification imager. The imager was tested with the PET and optical modalities to assess the margins.

Optical modality has been designed and developed for the DMI. It has been shown that the 3D reconstruction can be done for a squash ball with an accuracy of ±1 mm to the original diameter in X, Y and Z directions respectively. The 3D reconstruction of the surface of a digital phantom was obtained within the range of ±1 pixel to the original diameter in X and Y directions. The algorithm works for various phantoms with irregular surfaces and also works well for different sizes of phantoms. The basic idea that has been implemented to obtain 3D volumes from both the modalities and to evaluate the margins on the merged volumes was successful. The excised breast tissue was assumed to be convex in shape, based on discussions with the surgeon. The current algorithm implemented might not give the desired results in reconstructing phantoms with sharp corners and concave shaped structures. It was not possible to test with real excised breast tissue due to various concerns.

The surgeon places stitches on the excised specimen which indicate the superior and lateral directions and help in orientation to relate back to the patient. Identification of the stitches is beyond the scope of current work. An alternative method was suggested to keep the orientation intact by using a specimen holder which has 12 o’clock, 3 o’clock, 6 o’ clock and 9 o’ clock markings. The excised breast tissue should be placed with care on the holder such that superior lies at 12 o’ clock and lateral at 9 o’ clock positions respectively. Also the superior, lateral, medial and inferior directions of the excised breast tissue can be colored with different dyes alternatively.

The successful design and development of the prototype of the dual modality PET/optical imager proves that this concept is potential enough for clinical trials with a robust system.
5.2 Future Study

3D surface reconstruction of the excised breast tissue has the potential for further research. Structured light can be utilized to perform 3D reconstruction of the excised breast tissue and it is potential enough to provide high end resolution and improve the accuracy levels. User-friendly interface can be developed for easy use by the surgeon. The speed and accuracy of the algorithm can be further improved.

If the tests can be performed with real breast tissue the real time challenges of the optical modality can be identified and handled which would be helpful in obtaining the desired results during future clinical trials.


Appendix A

6 Source Codes

6.1 Pixel to millimeter calibration

%% Pixel to Millimeter Conversion
% This program is to find the pixel to millimeter conversion factor. A symmetric object of known dimensions is taken. Four images of the symmetric object at 0deg, 90deg, 180deg and 270deg named as pixel_0, pixel_90, pixel_180, pixel_270 are taken as input

%Function Name : Pixel2MM_Calib
%Version        : 1.0
%Date           : 08.24.2010
%Author         : Krishna Nandanavanam

%variables
%Diameter_Actual : The actual diameter of the symmetric object measured using vernier calipers.
%img             : Read the image and save as img
%imgC            : Crop the image by setting the limits manually
%imgG            : Grayscale image
%imgE            : Image with the edges detected
%r               : Rows of imgE
%c               : Columns of imgE
%edgeX           : X coordinates of the identified edges in imgE
%edgeY           : Y coordinates of the identified edges in imgE
%Xmin            : Minimum X coordinate of the X coordinates identified
%Xmax            : Maximum X coordinate of the X coordinates identified
%Ymin            : Minimum Y coordinate of the Y coordinates identified
%Ymax            : Maximum Y coordinate of the Y coordinates identified
%Diameter_H      : Horizontal diameter of the symmetrical phantom
%Diameter_V      : Vertical diameter of the symmetrical phantom
%Pixel2mm_Factor_H: Pixel to millimeter conversion factor in the horizontal direction
%Pixel2mm_Factor_V: Pixel to millimeter conversion factor in the vertical direction
%Pixel2mm_Factor : Pixel to millimeter conversion factor

Diameter_Actual=39.5;
for n=1:4
    % Read the image
    str=strcat('pixel_',int2str(n),'.jpg');
    eval(['img=imread(str);']);
    % Crop the image
imgC=imcrop(img,[201 45 399 399]);
% Convert the image to grayscale from color image

imgG=rgb2gray(imgC);

% Identify the edges in the image using sobel edge detection technique

imgE=edge(imgG,'sobel');

% Save the X and Y coordinates of identified edges of imgE in edgeX and
% edgeY respectively.
[r,c]=size(imgE);
row_var=1;
for i=1:r
    for j=1:c
        if imgE(i,j)==1
            edgeX(row_var)=j;
            edgeY(row_var)=i;
            row_var=row_var+1;
        end
    end
end

% Find the minimum and maximum values of the X and Y coordinates
Xmin=min(edgeX);
Xmax=max(edgeX);
Ymin=max(edgeY);
Ymax=max(edgeY);

% Calculate the diameter of the symmetrical object in horizontal and
% vertical directions
Diameter_H=(Xmax-Xmin);
Diameter_V=(Ymax-Ymin);

% Find the conversion factor to convert pixels to millimeter using the
% below formula
Pixel2mm_Factor_H(n)= (Diameter_H/Diameter_Actual);
Pixel2mm_Factor_V(n)= (Diameter_V/Diameter_Actual);

clear edgeX;
clear edgeY;
end

% The Pixel2mm_Factor is found to be the same in both horizontal and vertical
% directions. The mean of the values obtained from 4 images is calculated to
% be the required Pixel2mm_Factor.
Pixel2mm_Factor=mean(Pixel2mm_Factor_H);
6.2 AOR calibration

%%%Calibration of Axis of Rotation (AOR)%%%  
This program is to find X0 and Y0, AOR in the image plane. 180 images of the capillary tube are taken into consideration where each image is taken at an angle of 2 degrees.

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%Function Name : Calib_AOR
%%%%%%%Version : 1.0
%%%%%%%Date : 08.24.2010
%%%%%%%Author : Krishna Nandanavanam
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%VARIABLES%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%nimg : Number of images
%%%X_Start : The column pixel coordinate where the image cropping is to be started
%%%Y_Start : The row pixel coordinate where the image cropping is to be started
%%%X_Width : number of columns to be cropped from X_Start
%%%Y_Width : number of columns to be cropped from Y_Start
%%%nn : Counter variable for number of images
%%%img : Camera image
%%%imgC : Cropped image
%%%imgG : Grayscale image
%%%imgE : Image with edges identified
%%%r1 : counter row variable
%%%c1 : counter column variable
%%%Col_var1 : counter column variable
%%%edgX_mat1 : Stores X coordinate of the edges in each row for each image
%%%Row_Mean : Average of X coordinates obtained in each row of an image
%%%Img_Mean : Mean of X coordinates for all the images
%%%X0 : X coordinate of AOR
%%%Y0 : Y Coordinate of AOR

%%%Note : Y0 value is hard coded which would change with the change in camera settings.

close all;
clear all;
c1c;

nimg=179;
Img_Mean=zeros(1,nimg+1);
X_Start=201;
Y_Start=45;
X_Width=399;
Y_Width=399;

% Loop to read camera images.
for nn=0:nimg
    % Read the image
str=strcat('test_',int2str(nn),'.jpg');
eval('img=imread(str);');

% Crop the image
imgC=imcrop(img,[X_Start Y_Start X_Width Y_Width]);

% Convert the color image to grayscale
imgG=rgb2gray(imgC);

% Identify the edges in the image using sobel edge detection technique
imgE=edge(imgG,'sobel');

% Loop to calculate the row wise mean value of X0 in each image
[r1,c1]=size(imgE);
Row_Mean=zeros(r1,1);
EdgX_Mat=zeros(1,1);
for i=1:r1
    Col_var1=1;
    for j=1:c1
        if(imgE(i,j)==1)
            EdgX_Mat(Col_var1) =j;
            Col_var1 = Col_var1+1;
        end
    end
    Row_Mean(i,:)=mean(EdgX_Mat);
    clear EdgX_Mat;
end

% Saving the mean value of X0 obtained for all the images
Img_Mean(nn+1)=mean(Row_Mean,1);
end

X0=round(mean(Img_Mean));

%Y0, the top of the pedestal is identified manually as 395.
Y0=395;

fprintf('The Axis of Rotation, AOR (X0,Y0) is: (%d,%d)',X0,Y0);
6.3 Image Fusion Calibration

6.3.1 Identification of the centroids in optical modality

This program is to calculate the coordinates of the centroids of the four spheres in the calibration phantom in the optical system.

Function Name : Fusion_Calib_Set1

%VARIABLES%

%%(X0,Y0) : AOR of the object coordinate frame identified in the camera coordinate frame. It is obtained from Calib_AOR.m
%%X_Start : The column pixel coordinate where the image cropping is to be started
%%Y_Start : The row pixel coordinate where the image cropping is to be started
%%X_Width : number of columns to be cropped from X_Start
%%Y_Width : number of rows to be cropped from Y_Start
%%nn : Counter variable for number of images
%%theta1 : Difference in degree of rotation of the first image from the reference image as theta1
%%theta2 : Difference in degree of rotation of the second image from the reference image as theta2
%%Threshold : The threshold value at which the canny algorithm should find the edges.
%%img : Camera image
%%imgC : Cropped image
%%imgG : Grayscale image
%%imgE : Image with edges identified
%%rowvar : counter row variable
%%colvar : counter column variable
%%tempvar : counter variable

%%Note: Similar pattern of naming the variables as explained below is followed for the remaining 3 spheres in reference image, first and second images.

%%edgX_Sp1 : Stores X coordinate of the edges of sphere1 in the reference image
%%edgY_Sp1 : Stores Y coordinate of the edges of sphere1 in the reference image
%%centroid_sp1_X: X coordinate of the centroid of sphere 1 in the reference image
%%centroid_sp1_Y: Y coordinate of the centroid of sphere 1 in the reference image

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```matlab
clc;
clear all;
close all;

% Initializing variables
X0=215;
Y0=395;
X_Start=201;
Y_Start=45;
X_Width=399;
Y_Width=399;
Threshold=0.5;
theta1=deg2rad(40);
theta2=deg2rad(90);

%%% Processing the reference image which is at 0 degree

%Read the reference image
img=imread('test_0.jpg');

%Crop the image
imgC=imcrop(img,[X_Start Y_Start X_Width Y_Width]);

%Convert the cropped image to grayscale image
imgG=rgb2gray(imgC);

%Identify the edges using Canny edge detection technique
imgE=edge(imgG,'canny',Threshold);

% Identifying Sphere1 in the reference image by identifying the row and % column limits manually
imgE_Sp1=imgE;
[rowVar,colVar]=size(imgE_Sp1);
for i=1:rowVar
    for j=1:colVar
```
if i>45
    imgE_Sp1(i,j)=0;
end
end

%Saving the X and Y coordinates of sphere 1 in the reference image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE_Sp1(i,j)==1)
            edgX_Sp1(tempvar)=j;
            edgY_Sp1(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end

%Finding the coordinates of the centroid(centroid_sp1_X,Y_Sp1) of sphere1 in the reference image.
xmin_Sp1=min(edgX_Sp1);
xmax_Sp1=max(edgX_Sp1);
ind1=find(edgX_Sp1==min(edgX_Sp1));
ind2=find(edgX_Sp1==max(edgX_Sp1));
minY_Sp1=mean(edgY_Sp1(ind1));
maxY_Sp1=mean(edgY_Sp1(ind2));
Y_Sp1=[minY_Sp1 maxY_Sp1];
centroid_sp1_X=round((xmax_Sp1+xmin_Sp1)/2); % centroid_sp1_X, Y_Sp1
a_Sp1=(centroid_sp1_X-X0); % Identifying Sphere2 in the reference image by identifying the row and column limits manually
imgE_Sp2=imgE;
for i=1:rowvar
    for j=1:colvar
        if (i<65 || i>109)
            imgE_Sp2(i,j)=0;
        end
        if (j<235||j>285)
            imgE_Sp2(i,j)=0;
        end
    end
end

%Saving the X and Y coordinates of sphere 2 in the reference image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE_Sp2(i,j)==1)
            edgX_Sp2(tempvar)=j;
            edgY_Sp2(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end
Finding the coordinates of the centroid(centroid_sp2_X,Y_Sp2) of sphere1 in the reference image

xmin_Sp2=min(edgX_Sp2);
xmax_Sp2=max(edgX_Sp2);
ind1=find(edgX_Sp2==min(edgX_Sp2));
ind2=find(edgX_Sp2==max(edgX_Sp2));
minY_Sp2=mean(edgY_Sp2(ind1));
maxY_Sp2=mean(edgY_Sp2(ind2));
Y_Sp2=[minY_Sp2 maxY_Sp2];
centroid_sp2_X=round((xmax_Sp2+xmin_Sp2)/2);
a_Sp2=(centroid_sp2_X-X0);
centroid_sp2_Y=round(mean(Y_Sp2));

Identifying Sphere3 in the reference image by identifying the row and column limits manually

imgE_Sp3=imgE;

for i=1:rowvar
    for j=1:colvar
        if (i<110||i>160)
            imgE_Sp3(i,j)=0;
        end
        if (j<275||j>330)
            imgE_Sp3(i,j)=0;
        end
    end
end

Saving the X and Y coordinates of sphere 3 in the reference image.

tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE_Sp3(i,j)==1)
            edgX_Sp3(tempvar)=j;
            edgY_Sp3(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end

Finding the coordinates of the centroid(centroid_sp3_X,Y_Sp3) of sphere3 in the reference image.

xmin_Sp3=min(edgX_Sp3);
xmax_Sp3=max(edgX_Sp3);
ind1=find(edgX_Sp3==min(edgX_Sp3));
ind2=find(edgX_Sp3==max(edgX_Sp3));
minY_Sp3=mean(edgY_Sp3(ind1));
maxY_Sp3=mean(edgY_Sp3(ind2));
Y_Sp3=[minY_Sp3 maxY_Sp3];
centroid_sp3_X=round((xmax_Sp3+xmin_Sp3)/2);
a_Sp3=(centroid_sp3_X-X0);
centroid_sp3_Y=round(mean(Y_Sp3));
% Identifying Sphere4 in the reference image by identifying the row and column limits manually
imgE_Sp4=imgE;

for i=1:rowvar
  for j=1:colvar
    if (i<155||i>211)
      imgE_Sp4(i,j)=0;
    end
    if (j<100||j>160)
      imgE_Sp4(i,j)=0;
    end
  end
end

%Savings the X and Y coordinates of sphere 4 in the reference image.
tempvar=1;
for i=1:rowvar
  for j=1:colvar
    if (imgE_Sp4(i,j)==1)
      edgX_Sp4(tempvar)=j;
      edgY_Sp4(tempvar)=i;
      tempvar=tempvar+1;
    end
  end
end

%Finding the coordinates of the centroid(centroid_sp4_X,Y_Sp4) of sphere3 in the reference image.
xmin_Sp4=min(edgX_Sp4);
xmax_Sp4=max(edgX_Sp4);
ind1=find(edgX_Sp4==min(edgX_Sp4));
ind2=find(edgX_Sp4==max(edgX_Sp4));
minY_Sp4=mean(edgY_Sp4(ind1));
maxY_Sp4=mean(edgY_Sp4(ind2));
Y_Sp4=[minY_Sp4 maxY_Sp4];
centroid_sp4_X=round((xmax_Sp4+xmin_Sp4)/2);
a_Sp4=(centroid_sp4_X-X0);
centroid_sp4_Y=round(mean(Y_Sp4));

%%%%40 degree
% 20 deg is the reference zero position for the calibration.
% Delta theta is the difference of the angle of the first image from the reference image.
% The image is at 60 degrees position with respect to the turntable while the delta theta is 40 degree
% Sphere1 to 4 are numbered in the descending order of their heights.

% Read the first image
img1=imread('test_40.jpg');

% Crop the first image
imgCl=imcrop(img1,[X_Start Y_Start X_Width Y_Width]);

% Convert the color image to grayscale image
imgCl=rgb2gray(imgCl);
% Identify edges using canny edge detection technique
imgE1=edge(imgG1,'canny',Threshold);
imgE1_Sp1=imgE1;

% Identifying Sphere1 in the first image by identifying the row and column limits manually
[r,c]=size(imgE1_Sp1);
for i=1:r
    for j=1:c
        if i>45
            imgE1_Sp1(i,j)=0;
        end
    end
end

% Saving the X and Y coordinates of sphere 1 in the first image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE1_Sp1(i,j)==1)
            edgX1_Sp1(tempvar)=j;
edgY1_Sp1(tempvar)=i;
tempvar=tempvar+1;
        end
    end
end

% Finding the coordinates of the centroid(centroid_sp1_X1,centroid_sp1_Y1) of sphere1 in the first image.
xmin1_Sp1=min(edgX1_Sp1);
xmax1_Sp1=max(edgX1_Sp1);
ind1=find(edgX1_Sp1==min(edgX1_Sp1));
ind2=find(edgX1_Sp1==max(edgX1_Sp1));
minY1_Sp1=mean(edgY1_Sp1(ind1));
maxY1_Sp1=mean(edgY1_Sp1(ind2));
Y1_Sp1=[minY1_Sp1 maxY1_Sp1];
centroid_sp1_X1=round((xmax1_Sp1+xmin1_Sp1)/2);
al_Sp1=(centroid_sp1_X1-X0);
centroid_sp1_Y1=round(mean(Y1_Sp1));

% Identifying Sphere2 in the first image by identifying the row and column limits manually
imgE1_Sp2=imgE1;
for i=1:rowvar
    for j=1:colvar
        if (i<65 || i>109)
            imgE1_Sp2(i,j)=0;
        end
        if (j<170||j>220)
            imgE1_Sp2(i,j)=0;
        end
    end
end
%Saving the X and Y coordinates of sphere 2 in the first image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE1_Sp2(i,j)==1)
            edgX1_Sp2(tempvar)=j;
            edgY1_Sp2(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end

%Finding the coordinates of the centroid(centroid_sp2_X1,centroid_sp2_Y1) of sphere2 in the first image.
xmin1_Sp2=min(edgX1_Sp2);
xmax1_Sp2=max(edgX1_Sp2);
ind1=find(edgX1_Sp2==min(edgX1_Sp2));
ind2=find(edgX1_Sp2==max(edgX1_Sp2));
minY1_Sp2=mean(edgY1_Sp2(ind1));
maxY1_Sp2=mean(edgY1_Sp2(ind2));
Y1_Sp2=[minY1_Sp2,maxY1_Sp2];
centroid_sp2_X1=round((xmax1_Sp2+xmin1_Sp2)/2);
a1_Sp2=(centroid_sp2_X1-X0);
centroid_sp2_Y1=round(mean(Y1_Sp2));

% Identifying Sphere3 in the first image by identifying the row and column limits manually
imgE1_Sp3=imgE1;
for i=1:rowvar
    for j=1:colvar
        if (i<155||i>160)
            imgE1_Sp3(i,j)=0;
        end
        if (j<250||j>330)
            imgE1_Sp3(i,j)=0;
        end
    end
end

%Saving the X and Y coordinates of sphere 3 in the first image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE1_Sp3(i,j)==1)
            edgX1_Sp3(tempvar)=j;
            edgY1_Sp3(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end

%Finding the coordinates of the centroid(centroid_sp3_X1,centroid_sp3_Y1) of sphere3 in the first image.
xmin1_Sp3=min(edgX1_Sp3);
xmax1_Sp3=max(edgX1_Sp3);
ind1=find(edgX1_Sp3==min(edgX1_Sp3));
ind2=find(edgX1_Sp3==max(edgX1_Sp3));
minY1_Sp3=mean(edgY1_Sp3(ind1));
maxY1_Sp3=mean(edgY1_Sp3(ind2));
Y1_Sp3=[minY1_Sp3 maxY1_Sp3];
centroid_sp3_X1=round((xmax1_Sp3+xmin1_Sp3)/2);
a1_Sp3=(centroid_sp3_X1-X0);
centroid_sp3_Y1=round(mean(Y1_Sp3));

% Identifying Sphere4 in the first image by identifying the row and
% column limits manually
imgE1_Sp4=imgE1;
for i=1:rowvar
    for j=1:colvar
        if (i<155||i>211)
            imgE1_Sp4(i,j)=0;
        end
        if (j<95||j>155)
            imgE1_Sp4(i,j)=0;
        end
    end
end

%Saving the X and Y coordinates of sphere 4 in the first image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE1_Sp4(i,j)==1)
            edgX1_Sp4(tempvar)=j;
            edgY1_Sp4(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end

%Finding the coordinates of the centroid(centroid_sp4_X1,centroid_sp4_Y1) of
sphere4 in the first image.
xmin1_Sp4=min(edgX1_Sp4);
xmax1_Sp4=max(edgX1_Sp4);
ind1=find(edgX1_Sp4==min(edgX1_Sp4));
ind2=find(edgX1_Sp4==max(edgX1_Sp4));
minY1_Sp4=mean(edgY1_Sp4(ind1));
maxY1_Sp4=mean(edgY1_Sp4(ind2));
Y1_Sp4=[minY1_Sp4 maxY1_Sp4];
centroid_sp4_X1=round((xmax1_Sp4+xmin1_Sp4)/2);
a1_Sp4=(centroid_sp4_X1-X0);
centroid_sp4_Y1=round(mean(Y1_Sp4));

% Identifying that 90 degree
% 20 deg is the reference zero position for the calibration. Delta theta is
% the difference of the angle of the image from the zero position. Delta theta
% is 90 degree. The image is taken at 110 degree with respect to the turn
table. Spheres 4 are numbered with the decreasing heights of the rods.

%Read the first image
img2=imread('test_90.jpg');
%Crop the first image
imgC2 = imcrop(img2, [X_Start Y_Start X_Width Y_Width]);

% Convert the color image to grayscale image
imgG2 = rgb2gray(imgC2);

% Identify edges using canny edge detection technique
imgE2 = edge(imgG2, 'canny', Threshold);
imgE2_Sp1 = imgE2;

% Identifying Sphere1 in the second image by identifying the row and column limits manually
[r, c] = size(imgE2_Sp1);
for i = 1:rowvar
    for j = 1:colvar
        if i > 50
            imgE2_Sp1(i, j) = 0;
        end
    end
end

% Saving the X and Y coordinates of sphere 1 in the second image.
tempvar = 1;
for i = 1:rowvar
    for j = 1:colvar
        if (imgE2_Sp1(i, j) == 1)
            edgX2_Sp1(tempvar) = j;
            edgY2_Sp1(tempvar) = i;
            tempvar = tempvar + 1;
        end
    end
end

% Finding the coordinates of the centroid(centroid_sp1_X2, centroid_sp1_Y2) of sphere1 in the second image.
xmin2_Sp1 = min(edgX2_Sp1);
xmax2_Sp1 = max(edgX2_Sp1);
ind1 = find(edgX2_Sp1 == min(edgX2_Sp1));
ind2 = find(edgX2_Sp1 == max(edgX2_Sp1));
minY2_Sp1 = mean(edgY2_Sp1(ind1));
maxY2_Sp1 = mean(edgY2_Sp1(ind2));
Y2_Sp1 = [minY2_Sp1 maxY2_Sp1];
centroid_sp1_X2 = round((xmax2_Sp1 + xmin2_Sp1)/2);
a2_Sp1 = (centroid_sp1_X2 - X0);
centroid_sp1_Y2 = round(mean(Y2_Sp1));

% Identifying Sphere2 in the second image by identifying the row and column limits manually
imgE2_Sp2 = imgE2;
for i = 1:rowvar
    for j = 1:colvar
        if (i < 60 || i > 108)
            imgE2_Sp2(i, j) = 0;
        end
        if (j < 105 || j > 160)
            imgE2_Sp2(i, j) = 0;
        end
    end
end
end
end
end

% Saving the X and Y coordinates of sphere 2 in the second image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE2_Sp2(i,j)==1)
            edgX2_Sp2(tempvar)=j;
            edgY2_Sp2(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end

% Finding the coordinates of the centroid(centroid_sp2_X2, centroid_sp2_Y2) of sphere 2 in the second image.
xmin2_Sp2=min(edgX2_Sp2);
xmax2_Sp2=max(edgX2_Sp2);
ind1=find(edgX2_Sp2==min(edgX2_Sp2));
ind2=find(edgX2_Sp2==max(edgX2_Sp2));
minY2_Sp2=mean(edgY2_Sp2(ind1));
maxY2_Sp2=mean(edgY2_Sp2(ind2));
Y2_Sp2=[minY2_Sp2 maxY2_Sp2];
centroid_sp2_X2=round((xmax2_Sp2+xmin2_Sp2)/2);
centroid_sp2_Y2=round(mean(Y2_Sp2));

% Identifying Sphere 3 in the second image by identifying the row and column limits manually
imgE2_Sp3=imgE2;
for i=1:rowvar
    for j=1:colvar
        if (i<115||i>160)
            imgE2_Sp3(i,j)=0;
        end
        if (j<230||j>280)
            imgE2_Sp3(i,j)=0;
        end
    end
end

% Saving the X and Y coordinates of sphere 3 in the second image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE2_Sp3(i,j)==1)
            edgX2_Sp3(tempvar)=j;
            edgY2_Sp3(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end
%Finding the coordinates of the centroid(centroid_sp3_X2, centroid_sp3_Y2) of sphere3 in the second image.
xmin2_Sp3=min(edgX2_Sp3);
xmax2_Sp3=max(edgX2_Sp3);
ind1=find(edgX2_Sp3==min(edgX2_Sp3));
ind2=find(edgX2_Sp3==max(edgX2_Sp3));
minY2_Sp3=mean(edgY2_Sp3(ind1));
maxY2_Sp3=mean(edgY2_Sp3(ind2));
Y2_Sp3=[minY2_Sp3 maxY2_Sp3];
centroid_sp3_X2=round((xmax2_Sp3+xmin2_Sp3)/2);
a2_Sp3=(centroid_sp3_X2-X0);
centroid_sp3_Y2=round(mean(Y2_Sp3));

% Identifying Sphere4 in the second image by identifying the row and column limits manually
imgE2_Sp4=imgE2;
for i=1:rowvar
    for j=1:colvar
        if (i<150||i>215)
            imgE2_Sp4(i,j)=0;
        end
        if (j<150||j>215)
            imgE2_Sp4(i,j)=0;
        end
    end
end

%Saving the X and Y coordinates of sphere 4 in the second image.
tempvar=1;
for i=1:rowvar
    for j=1:colvar
        if (imgE2_Sp4(i,j)==1)
            edgX2_Sp4(tempvar)=j;
            edgY2_Sp4(tempvar)=i;
            tempvar=tempvar+1;
        end
    end
end

%Finding the coordinates of the centroid(centroid_sp4_X2, centroid_sp4_Y2) of sphere4 in the second image.
xmin2_Sp4=min(edgX2_Sp4);
xmax2_Sp4=max(edgX2_Sp4);
ind1=find(edgX2_Sp4==min(edgX2_Sp4));
ind2=find(edgX2_Sp4==max(edgX2_Sp4));
minY2_Sp4=mean(edgY2_Sp4(ind1));
maxY2_Sp4=mean(edgY2_Sp4(ind2));
Y2_Sp4=[minY2_Sp4 maxY2_Sp4];
centroid_sp4_X2=round((xmax2_Sp4+xmin2_Sp4)/2);
a2_Sp4=(centroid_sp4_X2-X0);
centroid_sp4_Y2=round(mean(Y2_Sp4));

%Finding theta for the four spheres
theta_Sp1=atan(((a1_Sp1*cos(theta2))-(a2_Sp1*cos(theta1)))/((a1_Sp1*sin(theta2))-(a2_Sp1*sin(theta1))));
theta_Sp2=atan(((a1_Sp2*cos(theta2))-(a2_Sp2*cos(theta1)))/((a1_Sp2*sin(theta2))-(a2_Sp2*sin(theta1))));

theta_Sp3=atan(((a1_Sp3*cos(theta2))-(a2_Sp3*cos(theta1)))/((a1_Sp3*sin(theta2))-(a2_Sp3*sin(theta1))));

theta_Sp4=atan(((a1_Sp4*cos(theta2))-(a2_Sp4*cos(theta1)))/((a1_Sp4*sin(theta2))-(a2_Sp4*sin(theta1))));

%Calculating the Y coordinate of the centroids of the four spheres
centroid_y_sp1=[centroid_sp1_Y centroid_sp1_Y1 centroid_sp1_Y2];

centroid_Y_sp1=round(mean(centroid_y_sp1));

centroid_y_sp2=[centroid_sp2_Y centroid_sp2_Y1 centroid_sp2_Y2];

centroid_Y_sp2=round(mean(centroid_y_sp2));

centroid_y_sp3=[centroid_sp3_Y centroid_sp3_Y1 centroid_sp3_Y2];

centroid_Y_sp3=round(mean(centroid_y_sp3));

centroid_y_sp4=[centroid_sp4_Y centroid_sp4_Y1 centroid_sp4_Y2];

centroid_Y_sp4=round(mean(centroid_y_sp4));

%Calculating the radius of the centroids of four spheres from X0
r_Sp1=a_Sp1/cos(theta_Sp1);
r_Sp2=a_Sp2/cos(theta_Sp2);
r_Sp3=a_Sp3/cos(theta_Sp3);
r_Sp4=a_Sp4/cos(theta_Sp4);

% Calculating the (X,Y,Z) coordinates for four spheres
X_Sp1=round((r_Sp1*cos(theta_Sp1))+X0);
Y_Sp1=centroid_Y_sp1;
Z_Sp1=round((r_Sp1*sin(theta_Sp1))+(rowvar/2));

fprintf(' The coordinates of the centroid of sphere1 are: (%d,%d,%d)
',X_Sp1,Y_Sp1,Z_Sp1);

X_Sp2=round((r_Sp2*cos(theta_Sp2))+X0);
Y_Sp2=centroid_Y_sp2;
Z_Sp2=round((r_Sp2*sin(theta_Sp2))+(rowvar/2));

fprintf(' The coordinates of the centroid of sphere2 are: (%d,%d,%d)
',X_Sp2,Y_Sp2,Z_Sp2);

X_Sp3=round((r_Sp3*cos(theta_Sp3))+X0);
Y_Sp3=centroid_Y_sp3;
Z_Sp3=round((r_Sp3*sin(theta_Sp3))+(rowvar/2));

fprintf(' The coordinates of the centroid of sphere3 are: (%d,%d,%d)
',X_Sp3,Y_Sp3,Z_Sp3);
X_Sp4=round((r_Sp4*cos(theta_Sp4))+X0);
Y_Sp4=centroid_Y_sp4;
Z_Sp4=round((r_Sp4*sin(theta_Sp4))+(rowvar/2));

fprintf(' The coordinates of the centroid of sphere4 are: (%d,%d,%d)
\n',X_Sp4,Y_Sp4,Z_Sp4);

6.3.2 Identification of the centroids in PET modality

%This program is to calculate the coordinates of the centroids of the four
spheres in the calibration phantom in the PET system from the images obtained
from the binary file.

%%%Function Name    : PET_Centroid
%%%Version          : 1.0
%%%Date             : 08.24.2010
%%%Author           : Krishna Nandanavanam

%%%img1       : Camera image
%%%imgG1      : Grayscale image
%%%BW_Sp1     : Binary image
%%%rowvar     : counter row variable
%%%colvar     : counter column variable
%%%Note: Similar pattern of naming the variables explained below is followed
for the remaining 3 spheres

%%%edgX_Sp1      : Stores X coordinate of the edges of sphere1
%%%edgY_Sp1      : Stores Y coordinate of the edges of sphere1
%%%centroid_sp1_X: X coordinate of the centroid of sphere 1
%%%centroid_sp1_Y: Y coordinate of the centroid of sphere 1

%%% Calculate centroid of Sphere 1

%Read the image
img1=imread('11.jpg');

%Convert the image to grayscale image
imgG1=rgb2gray(img1);

% Conver the image to binary image
level = graythresh(imgG1);
BW_Sp1 = im2bw(imgG1,level);

%Saving the X and Y coordinates of sphere 2
[rowvar, colvar] = size(BW_Sp1);
tempvar = 1;
for i = 1:rowvar
    for j = 1:colvar
        if (BW_Sp1(i, j) == 1)
            edgX_Sp1(tempvar) = j;
            edgY_Sp1(tempvar) = i;
            tempvar = tempvar + 1;
        end
    end
end

% Finding the coordinates of the centroid of sphere 1
xmin_Sp1 = min(edgX_Sp1);
xmax_Sp1 = max(edgX_Sp1);
minY_Sp1 = mean(edgY_Sp1(edgX_Sp1 == min(edgX_Sp1)));
maxY_Sp1 = mean(edgY_Sp1(edgX_Sp1 == max(edgX_Sp1)));
Y_Sp1 = [minY_Sp1 maxY_Sp1];
centroid_sp1_X = (xmax_Sp1 + xmin_Sp1)/2;
centroid_sp1_Y = mean(Y_Sp1);

%%% Calculate centroid of Sphere 2

% Read the image
img2 = imread('18.jpg');

% Convert the image to grayscale image
imgG2 = rgb2gray(img2);

% Conver the grayscale image to binary image
level = graythresh(imgG2);
BW_Sp2 = im2bw(imgG2, level);

% Saving the X and Y coordinates of sphere 2
[rowvar, colvar] = size(BW_Sp2);
tempvar = 1;
for i = 1:rowvar
    for j = 1:colvar
        if (BW_Sp2(i, j) == 1)
            edgX_Sp2(tempvar) = j;
            edgY_Sp2(tempvar) = i;
            tempvar = tempvar + 1;
        end
    end
end

% Finding the coordinates of the centroid of sphere 2
xmin_Sp2 = min(edgX_Sp2);
xmax_Sp2 = max(edgX_Sp2);
minY_Sp2 = mean(edgY_Sp2(edgX_Sp2 == min(edgX_Sp2)));
maxY_Sp2 = mean(edgY_Sp2(edgX_Sp2 == max(edgX_Sp2)));
Y_Sp2 = [minY_Sp2 maxY_Sp2];
centroid_sp2_X = (xmax_Sp2 + xmin_Sp2)/2;
centroid_sp2_Y = mean(Y_Sp2);
Calculate centroid of Sphere 3

% Read the image
img3 = imread('25.jpg');

% Convert the image to grayscale image
imgG3 = rgb2gray(img3);

% Convert the grayscale image to binary image
level = graythresh(imgG3);
BW_Sp3 = im2bw(imgG3, level);

% Saving the X and Y coordinates of sphere 3
[rowvar, colvar] = size(BW_Sp3);
tempvar = 1;
for i = 1:rowvar
    for j = 1:colvar
        if (BW_Sp3(i, j) == 1)
            edgX_Sp3(tempvar) = j;
            edgY_Sp3(tempvar) = i;
            tempvar = tempvar + 1;
        end
    end
end

% Finding the coordinates of the centroid of sphere 3
xmin_Sp3 = min(edgX_Sp3);
xmax_Sp3 = max(edgX_Sp3);
minY_Sp3 = mean(edgY_Sp3(edgX_Sp3 == min(edgX_Sp3)));
maxY_Sp3 = mean(edgY_Sp3(edgX_Sp3 == max(edgX_Sp3)));
Y_Sp3 = [minY_Sp3 maxY_Sp3];
centroid_Sp3_X = (xmax_Sp3 + xmin_Sp3) / 2;
centroid_Sp3_Y = mean(Y_Sp3);

Calculate centroid of Sphere 4

% Read the image
img4 = imread('31.jpg');

% Convert the image to grayscale image
imgG4 = rgb2gray(img4);

% Convert the grayscale image into binary image
level = graythresh(imgG4);
BW_Sp4 = im2bw(imgG3, level);

% Saving the X and Y coordinates of sphere 4
[rowvar, colvar] = size(BW_Sp4);
tempvar = 1;
for i = 1:rowvar
    for j = 1:colvar
        if (BW_Sp4(i, j) == 1)
            edgX_Sp4(tempvar) = j;
            edgY_Sp4(tempvar) = i;
            tempvar = tempvar + 1;
        end
    end
end
tempvar=tempvar+1;
end
end
end

%Finding the coordinates of the centroid of sphere4
xmin_Sp4=min(edgX_Sp4);
xmax_Sp4=max(edgX_Sp4);
minY_Sp4=mean(edgY_Sp4(edgX_Sp4==min(edgX_Sp4)));
maxY_Sp4=mean(edgY_Sp4(edgX_Sp4==max(edgX_Sp4)));
Y_Sp4=[minY_Sp4 maxY_Sp4];
centroid_sp4_X=(xmax_Sp4+xmin_Sp4)/2;
centroid_sp4_Y=mean(Y_Sp4);

6.3.3 Homogeneous transformation Matrix

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%VARIABLES%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%% PET        :X,Y and Z PET coordinates of the 4 spheres in the
calibration phantom obtained from PET_centroid.m
%%%% Note      :Optical_X, Optical_Y and Optical_Z are obtained from the
average of X, Y and Z coordinates obtained from Fusion_Calib_Set1,
Fusion_Calib_Set2 and Fusion_Calib_Set3
%%%% Optical_X  :Matrix with X coordinate of the 4 spheres of the optical
%%%%             system
%%%% Optical_Y  :Matrix with Y coordinate of the 4 spheres of the optical
%%%%             system
%%%% Optical_Z  :Matrix with Z coordinate of the 4 spheres of the optical
%%%%             system
%%%% Optical_scaling: Extra row required to form the homogeneous matrix
%%%% Homogeneous_Matrix: Transformation matrix

PET=[40,11,38,1;22,18,21,1;39,25,23,1;22.5,31,40,1];
Optical_X=[195; 259; 301; 128];
Optical_Y=[121.9655;291.3442; 160.5544; 233.5841];
Optical_scaling=[1; 1; 1; 1];
%Calculation of the transformation matrix using Gaussian elimination method
A1=PET\Optical_X;
A2=PET\Optical_Y;
A3=PET\Optical_Z;
A4=PET\Optical_scaling;
Homogeneous_Matrix=[A1'; A2'; A3'; A4'];
6.4 Optical Slice Generation, Merging and Margin Evaluation

6.4.1 Function Main.m

% Program to read the optical camera images and generate the optical slices. 
Read the PET slices and merge the transformed PET slices with the respective 
Optical slices. Margins are evaluated for the merged slices and the images 
are written into a binary file MergedVolume.bin. MergedVolumefileinfo.txt has 
the information about the binary file.

%%%%%%Program Name   : Main.m
%%%%%%Version        : 1.0
%%%%%%Date           : 08.24.2010
%%%%%%Author         : Krishna Nandanavanam

% Calculating the computation time
profile on;
tic;

% Call the function Initialize.m
[X0,Y0,Sliceheight,Threshold,Pixel2mm_Factor,nimg,DOR,PET_Slices,C,S,r1,c1,Homogeneous_Matrix,X_Start,Y_Start,X_Width,Y_Width]= Initialize();

% Call the function Optical_Coordinates.m
[Optical_Coords, Top_Slice]= Optical_Coordinates(nimg, C, S, Sliceheight, Pixel2mm_Factor, X0, Y0, threshold, X_Start, Y_Start, X_Width, Y_Width);

% Call the function PET_Coordinates.m
[ PET_coordmatrix]=PET_Coordinates(PET_Slices,Top_Slice,Pixel2mm_Factor,Homogeneous_Matrix);

% Call the function SliceGeneration.m
SliceGeneration(Optical_Coords, PET_coordmatrix, r1,c1,Top_Slice, Sliceheight, Pixel2mm_Factor,X0,Y0, DOR);

toc;
6.4.2 Function Initialize.m

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Initialization of variables%%%%%%%%%%%%%%%%%%
%This function is to initialize the variables and the inputs are to be given
%by the end user.

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Inputs to be given by the user%%%%%%%%%%%%%%%%
%%% (X0,Y0) : AOR of the object coordinate frame identified in the
% camera coordinate frame. It is obtained from Calib_AOR.m
% Slice_Height : The height at which the slices are to be taken. In the
% present case the slices are taken for every 1 millimeter.
% Threshold : Threshold value
% Pixel2mm_Factor : The pixel to millimeter conversion factor is obtained from
% % Pixel2MM_Calib.m
% nimg : Number of images of the fusion phantom taken by the camera
% DOR : Degree of rotation in degrees
% PET_Slices : Number of PET slices
% X_Start : The column pixel coordinate where the image cropping is to
% be started
% Y_Start : The row pixel coordinate where the image cropping is to be
% started
% X_Width : Number of columns to be cropped from X_Start
% Y_Width : Number of rows to be cropped from Y_Start
% Homogeneous_Matrix: Transformation matrix obtained from
% % Homogeneous_transformation.m

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%VARIABLES%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%% C : Cosine values of the Angle values from 0 to 350 degrees
%%% S : Sine values of the Angle values from 0 to 350 degrees
%%% r1 : Rows in the cropped image
%%% c1 : Columns in the cropped image

function
[X0,Y0,Slice_Height,Threshold,Pixel2mm_Factor,nimg,DOR,PET_Slices,C,S,r1,c1,Homogeneous_Matrix,X_Start,Y_Start,X_Width,Y_Width]= Initialize()

X0=215;
Y0=395;
Slice_Height=1;
Threshold=0.5;
nimg=35;
DOR=10;
PET_Slices=1:60;
Pixel2mm_Factor=4.8;
X_Start=201;
Y_Start=45;
X_Width=399;
Y_Width=399;
Homogeneous_Matrix=[3.2298,0.1869,-7.1076,333.8395;-0.2990,7.5912,-0.0282,-41.4722;-7.2029,-0.46865,-2.5298,511.37;0,0,0,1];

% Calculating the cosine and sine for all the values of DOR
DOR_rads=(DOR*pi)/180;
Angle=0:DOR_rads:((2*pi)-DOR_rads);
C= cos(Angle);
S= sin(Angle);

% Crop the input image to know the resolution of the output image.
img=imread('test_0.jpg');
imgC=imcrop(img,[X_Start Y_Start X_Width Y_Width]);
imgG=rgb2gray(imgC);
[r1 c1]=size(imgG);
clear img;
clear imgC;
clear imgG;
6.4.3 Function Optical_Coordinates.m

% This function is to generate the point cloud of the optical system using % the camera images as input.

function [Optical_Coords, Top_Slice]= Optical_Coordinates(nimg, C, S, Sliceheight, Pixel2mm_Factor,X0,Y0,Threshold,X_Start,Y_Start,X_Width,Y_Width)

count1=0;
for nn=0:nimg

    % Read the image
    str=strcat('test_',int2str(nn),'.jpg');
    eval(['img=imread(str);']);

    % Crop the image
    imgC=imcrop(img,[X_Start Y_Start X_Width Y_Width]);

    % Convert the color image to grayscale
    imgG=rgb2gray(imgC);
    clear imgC;

    % Identify the edges in the image using canny edge detection technique
    % with the Threshold specified by the user
    imgE=edge(imgG,'canny',Threshold);

    %Calculate the Y pixel coordinates corresponding to Sliceheight using the %Pixel2mm_Factor starting from Y0
    HH=Y0:-round(Pixel2mm_Factor):1;

    % Extracting the X and Y coordinates of the edges at respective heights 
    [r2,c2]=size(imgE);
    row_var1=1;
    row_var2=1;
    row_var3=1;
    temp=0;
for i=1:length(HH)
    row_var4=HH(i);
    for j=1:c2
        if(imgE(row_var4,j)==1)
            edgyn(row_var1) = (row_var4);
            H(row_var3)=temp;
            edgxn(row_var2)=(j);
            row_var1 = row_var1 +1;
            row_var2 = row_var2+1;
            row_var3=row_var3+1;
        end
    end
    temp=temp+Sliceheight;
end
clear i;
clear j;

% Calculate r value
radius=((edgxn-X0)*(1/Pixel2mm_Factor));

% Generate the pointcloud. Calculate the X, Y and Z coordinates.
X=radius*C(nn+1);
Z=radius*S(nn+1);
Y=H;

Img_Coords=X';
Img_Coords(:,2)=Y';
Img_Coords(:,3)=Z';

% Storing the X, Y and Z coordinates for all the images in 'Optical_PtCloud'
for i=1:length(Img_Coords)
    Optical_PtCloud(count1+i,:) = Img_Coords(i,:);
end

count1=count1+i;
clear edgxn;
clear edgyn;
clear X;
clear Y;
clear Z;
clear r;
clear Img_Coords;
clear H;
end
clear i;
Optical_Coords=Optical_PtCloud;

% Round off the coordinates to four digits
Optical_Coords=round(Optical_Coords*10000)/10000;

% Calculate the arc tangent of the Z and X coordinates
for i=1:length(Optical_Coords)
    if Optical_Coords(i,1)>=0 && Optical_Coords(i,3)>0
        Optical_Coords(i,4)=round(atand(Optical_Coords(i,3)./Optical_Coords(i,1)));
    else if Optical_Coords(i,1)>0 && Optical_Coords(i,3)<0
        Optical_Coords(i,4)=round(rad2deg(atan2(Optical_Coords(i,3),Optical_Coords(i,1)))+360);
    else if Optical_Coords(i,1)<0 && Optical_Coords(i,3)>0
        Optical_Coords(i,4)=round(rad2deg(atan2(Optical_Coords(i,3),Optical_Coords(i,1))));
    else if Optical_Coords(i,1)<0 && Optical_Coords(i,3)<=0
        Optical_Coords(i,4)=round(atand(Optical_Coords(i,3)./Optical_Coords(i,1))+180);
    end
end
end

clear i;
% Calculate the radius of the points from (0,0)
for i=1:length(Optical_Coords)
    Optical_Coords(i,5)=sqrt((Optical_Coords(i,1)^2)+(Optical_Coords(i,3)^2));
end

clear i;
Maxedge=max(Optical_Coords(:,2));
Top_Slice=floor(Y0-(Maxedge*Pixel2mm_Factor));
6.4.4 Function Pet_Coordinates.m

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% This function is to find the PET coordinates which are transformed into
% the Optical system.
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%VARIABLES%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%PET_X        :X coordinates of the points in each PET slice
%%%PET_Z        :Z coordinates of the points in each PET slice
%%%PET_Coords   :X,Y and Z coordinates of a PET slice
%%%PET_Trans_Coords:X,Y and Z transformed coordinates of a PET slice
%%%PET_coordmatrix :X,Y and Z transformed coordinates of all the images
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

function
PET_coordmatrix=PET_Coordinates(PET_Slices,Top_Slice,Pixel2mm_Factor,Homogeneous_Matrix)

count=0;
for st=1:length(PET_Slices)

    % Read the image
    str=strcat(int2str(PET_Slices(st)),'.jpg');
    eval(['img1=imread(str);']);

    % Convert the image to grayscale image
    B1=rgb2gray(img1);
    clear img1;

    % Convert the grayscale image to binary image
    level = graythresh(B1);
    BW1 = im2bw(B1,level);
    clear B1;

    % Extracting the X and Z coordinates of the points where radioactivity
    % is present. The presence of radioactivity is shown by white color
    % on black background in the PET slices
    PET_X=[];
    [r,c]=size(BW1);
    l=1;
    m=1;
    for i=1:r
        for j=1:c
            if( BW1(i,j)==1)
                PET_X(l)=j;
                PET_Z(m)=i;
                l=l+1;
                m=m+1;
            end
        end
    end

end
% If there is no activity present in the slice continue with the next slice
if isempty(PET_X)
    continue;
end

% Saving the X, Y ans Z coordinates of the points identified in each slice
PET_Coords=PET_X';
PET_Coords(:,3)=PET_Z';
PET_Coords(:,2)=PET_Slices(st);
PET_Coords(:,4)=1;

% Transformation of the PET coordinates of each slice into optical system using the homogeneous matrix.
k=1;
for i=1:length(PET_Coords)
    temp=PET_Coords(i,:)';
    PET_Trans_Coords(k,:)=floor((Homogeneous_Matrix*temp)');
k=k+1;
end

% Excluding the radioactivity identified outside the phantom which is identified by using the slice number given by Top_Slice
if (PET_Trans_Coords(:,2)<Top_Slice)
    clear PET_Trans_Coords;
    clear PET_Coords;
    clear PET_X;
    clear PET_Z;
    continue;
end

PET_Trans_Coords(:,2)=round(mean(PET_Trans_Coords(:,2)));

% Saving the transformed coordinates obtained from all the slices
for i=1:length(PET_Trans_Coords)
    PET_coordmatrix(count+i,:)=PET_Trans_Coords(i,:);
end

count=count+i;
clear PET_Trans_Coords;
clear PET_Coords;
clear PET_X;
clear PET_Z;
end

% Collapsing the range of PET, Y coordinates obtained from one slice into one slice of the optical system.
PET_coordmatrix(:,5)=round(PET_coordmatrix(:,2)/round(Pixel2mm_Factor));
PET_coordmatrix(:,2)=PET_coordmatrix(:,5)*round(Pixel2mm_Factor);
6.4.5 Function Slice_Generation.m

%Generation of Optical slices, Merging with PET slices and Margin Evaluation
%%% This function is to generate the optical slices from the optical point
%%% cloud obtained from the function Optical_Coordinates.m. The optical
%%% slices are merged with the PET slices obtained from PET_Coordinates.m and
%%% the margins are evaluated for the merged slices using the function
%%% MarginEvaluation.m. The slices are written into the Merged_Volume.bin

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Functions used%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%CurveFitting.m         :Curve fitting to the point cloud on each
%                            optical slice
%%%%%MarginEvaluation.m     :Merging optical and PET slices and evaluating
%                            the margins
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%VARIABLES%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%Slice_matrix      :Optical slices in millimeter
%%%Slice_matrix_pix  :Optical slices in pixels
%%%Optical_Slice     :Coordinates of points in each optical slice
%%%PET_System_Coords :coordinates of points in each PET slice
%%%Merged_Volume.bin :Binary file where the merged images are written
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

function
SliceGeneration(Optical_Coords,PET_coordmatrix,r1,c1,Top_Slice,Sliceheight,Pixel2mm_Factor,X0,Y0,DOR)

% Calculating the slices in millimeter and pixels.
Slice_matrix=round(min(Optical_Coords(:,2))):Sliceheight:ceil(max(Optical_Coords(:,2)));
Slice_matrix_pix=Slice_matrix;
Slice_matrix_pix(2,:)=Y0-(Slice_matrix_pix(1,:)*round(Pixel2mm_Factor));

% Processing each optical slice, , and merging with the corresponding PET
% slice and Margin evaluation
for i=1:length(Slice_matrix)

%Extracting the coordinates of a particular slice from the optical point
% cloud
    if (Slice_matrix(i)==ceil(max(Optical_Coords(:,2))))

Optical_Slice=Optical_Coords((Optical_Coords(:,2)>=Slice_matrix(i)),:);
    else
        Optical_Slice=Optical_Coords((Optical_Coords(:,2)>=Slice_matrix(i) &
Optical_Coords(:,2)<Slice_matrix(i+1)),:);
    end

% Call the function Curve fitting to the point cloud of the optical points
[XZ]=CurveFitting(Optical_Slice,Pixel2mm_Factor,X0,DOR,r1);
%Finding the PET coordinates corresponding to the optical slice i

PET_System_Coords = PET_coordmatrix((Slice_matrix_pix(2,i) == PET_coordmatrix(:,2)),:);

%Margin evaluation of the merged slices if radioactivity is present

if (isempty(PET_System_Coords) == 0)
    [IMG2] = MarginEvaluation(XZ, PET_System_Coords, r1, c1, Pixel2mm_Factor, i);
    figure, imshow(IMG2);

    %Writing the slices into a binary file after merging
    fid = fopen('Merged_Volume.bin', 'a+');
    fopen(fid);
    fwrite(fid, IMG2, 'integer*4');
    fclose(fid);

else
    IMG2 = zeros(r1, c1);
    for t = 1:length(XZ)
        IMG2(XZ(t, 2), XZ(t, 1)) = 1;
    end
    figure, imshow(IMG2);

    %Writing the slices into a binary file after merging
    fid = fopen('Merged_Volume.bin', 'a+');
    fopen(fid);
    fwrite(fid, IMG2, 'integer*4');
    fclose(fid);

end

clear PET_System_Coords;
clear XZ;

end

%Slices from the top slice to the top of the image space
for s1 = Top_Slice-5:-5:1
    IMG3 = zeros(r1, c1);
    fid = fopen('Merged_Volume.bin', 'a+');
    fopen(fid);
    fwrite(fid, IMG3, 'integer*4');
    fclose(fid);
    figure, imshow(IMG3)
end
6.4.6 Function CurveFitting.m

%%%%%%Curve fitting to the point cloud in each optical slice%%%%%%
%% This function is to fit a curve to the individual points in each optical slice. This is done by fitting a straight line to two adjacent points.
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%VARIABLES%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%XZ       :Optical slices in millimeter
%%%theta    :Optical slices in pixels
%%%coords   :Coordinates of points in each optical slice
%%%xz_coord :X and Z coordinates of each slice
%%%XZ       :X and Z coordinates of all slices
%%%Merged_Volume.bin :Binary file where the merged images are written
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

function [XZ]=CurveFitting(Optical_Slice,Pixel2mm_Factor,X0,DOR,r1)
theta=0:DOR:360-DOR;
coords=zeros(1,5);
countvar=1;

%Select the point with maximum radius for each theta angle
for j=1:length(theta)
    temp=Optical_Slice((Optical_Slice(:,4)==theta(j)),:);
tf=isempty(temp);
    if tf==0
        ind1=find(temp(:,5)==max(temp(:,5)));
        coords(countvar,:)=temp(ind1(1),:);
        countvar=countvar+1;
    end
end
clear temp;

% Fit a straight line to two adjacent points and save the coordinates of all the points on the straight line.
[r4,c4]=size(coords);
countvar1=0;
for j=1:r4
    if j==r4
        coords_temp=coords(((coords(:,4)==coords(r4,4))|(coords(:,4)==0)),:);
        xdiff=max(coords_temp(:,1))-min(coords_temp(:,1));
        ydiff=max(coords_temp(:,3))-min(coords_temp(:,3));
        if xdiff>=ydiff
            p_temp=polyfit(coords_temp(:,1),coords_temp(:,3),1);
            X_temp =min(coords_temp(:,1)):0.1:max(coords_temp(:,1))+0.1;
            Z_temp = polyval(p_temp,X_temp);
        else
            p_temp=polyfit(coords_temp(:,3),coords_temp(:,1),1);
            Z_temp =min(coords_temp(:,3)):0.1:max(coords_temp(:,3))+0.1;
            X_temp = polyval(p_temp,Z_temp);
        end
    else
        ...
end
coords_temp=coords(((coords(:,4))>=coords(j,4))&(coords(:,4))<=coords(j+1,4)),);
    xdiff=max(coords_temp(:,1))-min(coords_temp(:,1));
    ydiff=max(coords_temp(:,3))-min(coords_temp(:,3));
    if xdiff>=ydiff
        p_temp=polyfit(coords_temp(:,1),coords_temp(:,3),1);
        X_temp =min(coords_temp(:,1)):0.1:max(coords_temp(:,1))+0.1;
        Z_temp = polyval(p_temp,X_temp);
    else
        p_temp=polyfit(coords_temp(:,3),coords_temp(:,1),1);
        Z_temp =min(coords_temp(:,3)):0.1:max(coords_temp(:,3))+0.1;
        X_temp = polyval(p_temp,Z_temp);
    end
end

xz_coord_temp=X_temp';
xz_coord_temp(:,2)=Z_temp';

% Save the coordinates of all the points present on the curve which joins all the points on each optical slice
for r=1:length(xz_coord_temp)
    xz_coord(countvar1+r,:)=xz_coord_temp(r,:);
end

countvar1=countvar1+r;

clear X_temp;
clear Z_temp;
clear p_temp;
clear coords_temp;
clear xz_coord_temp;
end

%Convert all the points on the curve from millimeter to pixels. The X coordinates are translated by X0 and Z coordinates are translated by r1/2.

XZ=round(xz_coord(:,1).*Pixel2mm_Factor);
XZ(:,2)=round(xz_coord(:,2).*Pixel2mm_Factor);
XZ(:,1)=XZ(:,1)+X0;
XZ(:,2)=XZ(:,2)+r1/2;
XZ(:,2)=round(r1-XZ(:,2));

clear xz_coord;
clear coords;
6.4.7 Function MarginEvaluation.m

function [IMG2] = MarginEvaluation(XZ,PET_System_Coords,r1,c1,Pixel2mm_Factor,i)

coordstemp1=zeros((length(PET_System_Coords)*13),2);
X1=zeros(1,1);
Z1=zeros(1,1);
count=0;

% Fit the optical coordinates into image
IMG2=zeros(r1,c1);
for t=1:length(XZ)
    IMG2(XZ(t,2),XZ(t,1))=1;
end

% The resolution of PET input images is 60*60 while for optical it is 400*400.
% So approximately 7 pixels of PET system form one pixel of optical system.
% Therefore six pixels around each PET pixel are computed.
for k=1:length(PET_System_Coords)
    X1(k)=PET_System_Coords(k,1);
    Z1(k)=PET_System_Coords(k,3);
    coordstemp=[X1(k)-3 Z1(k);
                X1(k)-2 Z1(k);
                X1(k)-1 Z1(k);
                X1(k)   Z1(k);
                X1(k)+1 Z1(k);
                X1(k)+2 Z1(k);
                X1(k)+3 Z1(k);
                X1(k)   Z1(k)+3;
                X1(k)   Z1(k)+2;
                X1(k)   Z1(k)+1;
                X1(k)   Z1(k)-3;
                X1(k)   Z1(k)-2;
                X1(k)   Z1(k)-1;];
end
for t=1:length(coordstemp)
    coordstemp1(count+t,:)=coordstemp(t,:);
end
    count=count+t;
end

%Fit the PET coordinates into image
for k=1:length(coordstemp1)
    IMG2(coordstemp1(k,2),coordstemp1(k,1))=0.2;
end

% Margin evaluation of the merged image.
xmin=min(coordstemp1(:,1));
zmin=min(coordstemp1(:,2));
xmax=max(coordstemp1(:,1));
zmax=max(coordstemp1(:,2));

%Find the coordinates of the superior point from the PET coordinates
ind1=find((coordstemp1(:,2)==zmin));
Superior_Pt=coordstemp1(ind1,:);

%Find the coordinates of the medial point from the PET coordinates
ind1=find((coordstemp1(:,1)==xmax));
Medial_Pt=coordstemp1(ind1,:);

%Find the coordinates of the inferior point from the PET coordinates
ind1=find((coordstemp1(:,2)==zmax));
Inferior_Pt=coordstemp1(ind1,:);

%Find the coordinates of the lateral point from the PET coordinates
ind1=find((coordstemp1(:,1)==xmin));
Lateral_Pt=coordstemp1(ind1,:);

%Find the coordinates of the superior point from the optical coordinates
ind=find(XZ(:,1)==Superior_Pt(:,1));
S_Pt=Superior_Pt(:,1);
S_Pt(1,2)=min(XZ(ind,2));

%Find the coordinates of the inferior point from the optical coordinates
ind=find(XZ(:,1)==Inferior_Pt(:,1));
I_Pt=Inferior_Pt(:,1);
I_Pt(1,2)=max(XZ(ind,2));

%Find the coordinates of the medial point from the optical coordinates
ind=find(XZ(:,2)==Medial_Pt(:,2));
M_Pt=Medial_Pt(:,2);
M_Pt(1,2)=max(XZ(ind,1));

%Find the coordinates of the lateral point from the optical coordinates
ind=find(XZ(:,2)==Lateral_Pt(:,2));
L_Pt=Lateral_Pt(:,2);
L_Pt(1,1)=min(XZ(ind,1));

% distance between PET and optical points in superior, inferior, medial and % lateral directions
Superior_Margin=round(sqrt((S_Pt(:,1)-Superior_Pt(:,1))^2+(S_Pt(:,2)-Superior_Pt(:,2))^2)/Pixel2mm_Factor);
Inferior_Margin=round(sqrt((I_Pt(:,1)-Inferior_Pt(:,1))^2+(I_Pt(:,2)-Inferior_Pt(:,2))^2)/Pixel2mm_Factor);
Medial_Margin=round(sqrt((M_Pt(:,1)-Medial_Pt(:,1))^2+(M_Pt(:,2)-Medial_Pt(:,2))^2)/Pixel2mm_Factor);
Lateral_Margin=round(sqrt((L_Pt(:,1)-Lateral_Pt(:,1))^2+(L_Pt(:,2)-Lateral_Pt(:,2))^2)/Pixel2mm_Factor);

fprintf('The margins of the slice %d are: 
', i);

% The margins are considered to be positive if they are lesser than 5 mm % and negative when greater than 5 mm.
if Superior_Margin>=5
    fprintf('Superior: Negative Margin. The margin is %d \n', Superior_Margin);
else
    fprintf('Superior: Positive Margin. The margin is %d \n', Superior_Margin);
end

if Inferior_Margin>=5
    fprintf('Inferior: Negative Margin. The margin is %d \n', Inferior_Margin);
else
    fprintf('Inferior: Positive margin. The margin is %d \n', Inferior_Margin);
end

if Medial_Margin>=5
    fprintf('Medial: Negative Margin. The margin is %d \n', Medial_Margin);
else
    fprintf('Medial: Positive Margin. The margin is %d \n', Medial_Margin);
end

if Lateral_Margin>=5
    fprintf('Lateral: Negative Margin. The margin is %d \n', Lateral_Margin);
else
    fprintf('Lateral: Positive Margins. The margin is %d \n', Lateral_Margin);
end

clear coordstemp1;