Carbon deposition on Ni/YSZ anode SOFC for direct methane steam reforming

Haiyang Li

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Carbon deposition on Ni-YSZ anode SOFC for direct methane steam reforming

Haiyang Li

Problem report submitted to the Benjamin M. Statler College of Engineering and Mineral Resources at West Virginia University in partial fulfillment of the requirements for the degree of Master in Department of Mechanical & Aerospace Engineering

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ABSTRACT

Carbon deposition on Ni-YSZ anode SOFC for direct methane steam reforming

Haiyang Li

Solid Oxide Fuel Cells (SOFCs) are electrochemical devices that produce electricity directly from oxidizing fuels. Compared to direct combustion of hydrogen to generate power, it has a big advantage in aspects from efficiency and safety when using hydrogen as the fuel of SOFCs. Nowadays, about 50% of the hydrogen of world demand is derived from the natural gas. Hydrocarbon reforming is one of the conventional methods to convert nature gas into hydrogen. While, considering the difficulty in storage and transportation of hydrogen, we can utilize the supporting materials on the anode side of SOFCs as catalyst to generate hydrogen via hydrocarbon reforming process and pour the hydrogen as fuel into the SOFC system. Among many kinds of anode materials that have a good catalytic reforming and electrochemical reactivity, Ni/YSZ is the most commonly used because of its cost-effective and well suitable for anode-supported fuel cell design requirements. While there are also some drawbacks, the biggest one is the performance degradation of fuel cell caused by solid carbon formation on the surface of the Ni/YSZ anode cermet, which may block gas diffusion tunnel. Moreover, the accumulation of carbon on catalysts can crack the cell.

In the present report, methane steam reforming and carbon deposition on Ni catalyst from the thermodynamic and kinetic views are discussed. The process of carbon deposition on Ni catalyst is also described. In order to face the challenge, some measures have been taken to suppress the effect including optimizing system parameters, addition of other metal elements and synthesizing smaller Ni particle catalyst. In the future, a lot of work should be done on adjusting catalyst compositions, feed compositions, and reaction conditions, especially on developing new materials that fit the system perfectly. For the application in SOFC system, it is reported to have less carbon deposition by adjusting the current density of the cell. More efforts are still to be made from the system aspect.
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Carbon deposition on Ni-YSZ anode SOFC for direct methane steam reforming

1. Introduction

Hydrogen is a perfect fuel gas for our human beings when we are facing greenhouse effect and try to avoid further temperature rise in our planet because of its environmental-friendly production after oxidation. About 50% of the hydrogen for world demand is derived from the natural gas. Hydrogen can be obtained from many resources including nuclear power, natural gas, coal, biomass and other renewable sources[1]. Overall, there are three conventional methods to generate hydrogen from natural gas nowadays, including hydrocarbon reforming, partial oxidation and auto-thermal reforming [2]. Methane is an important fuel source which we can get from seabed as methane hydrate and it is reported to be quite abundant that can support human beings for a long time. Because of the increase hydrogen demand and the importance of syngas production, methane reforming, including steam reforming and dry reforming, will be much more important in fields related to hydrogen economy [3].

In these two kinds of reforming reaction, methane dry reforming can consume CO$_2$ which can reduce the greenhouse effect and make a contribution to the environment. However, methane dry reforming is reported to be inefficient because of the water-gas shift (WGS) reaction at 973K or higher temperature, where is the temperature range for the typical operation of fuel cells. While methane steam reforming can still produce great amount of hydrogen in such circumstances. Moreover, a stable conversion rate of hydrogen generated by methane steam reforming is also at a very high level for higher pressure[4]. Besides the turnover rate difference between these two reactions, the side product is another big issue we have to take into consideration. For methane dry reforming, carbon is inevitable in production because the high atom percentage in the reactants and carbon is especially harmful to fuel cell system. Carbon like graphite
or other forms has high hardness which can crack the pallet. While methane steam reforming reaction can efficiently reduce the effect. So methane steam reforming is overall a much more promising way to better use the natural gas which we can get directly from seabed or via fossil fuel decomposition.

The reaction of methane steam reforming is given in following reaction equation:

\[ CH_4 + H_2O \leftrightarrow CO + 3H_2 \quad \Delta H_{298}^0 = 206\text{kJ/mol} \] (1)

Methane steam reforming is an endothermic reaction which requires very high temperature (700°C -900°C) and catalysts are needed to realize the reaction. Catalysts like Ni, Pt and rare earth elements are great candidates for the reaction because they all have a high catalytic efficiency on methane steam reforming. The details of these catalysts will be discussed in following sections.

![Diagram of SOFC](image)

**Figure.1** (a) Mechanism of a solid-oxide fuel cell (b) schematic of anode-supported SOFC single cell[5]

SOFCs (solid oxide fuel cell) are electrochemical devices that produce electricity directly from oxidizing fuels. Compared to direct combustion of hydrogen to generate power, it has a big advantage on efficiency. In our case, the fuels can be hydrogen or hydrocarbons. Figure.1 (by Sakurambo) shows a conventional schematic image of SOFC structure and how SOFCs generate power. SOFCs usually consist of three main components: anode, electrolyte and cathode. The conventional ceramic anode layer must have a porous structure to allow the fuel gas flow towards the electrolyte to realize the electrochemical reaction. As a result, granular matter or powder is often used for anode fabrication procedures[6]. The oxygen-ion
conducting electrolyte is a dense layer which conducts oxygen ions to the anode side that react with the fuels including hydrogen, methane, ethane, methanol, acetone and other hydrocarbons. An important aspect of electrolyte is the shielded function of electrons which has a great influence on the overall performance of the SOFCs. Generally speaking, there are three popular electrolyte materials widely used for our researches nowadays, including yttria-stabilized zirconia (YSZ), scandia stabilized zirconia (ScSZ) and gadolinium doped ceria (GDC)[7]. Cathode is a porous structure where oxygen reduction takes place and oxygen vacancies form. Cathode materials have to be conductive and have a similar thermal expansion to electrolyte like YSZ or GDC to remain structurally and chemically stable during the test of cells at elevated temperatures.

In recently years, anode-supported fuel cells have been drawing the attention from all over the world because they can achieve both high performance at relatively low temperature and perform great thermodynamically mechanical stability[8]. Another great advantage of anode-supported fuel cell is that it allows direct internal methane reforming on the porous support material so that the conversion of methane to hydrogen can be transformed from a huge plant to a small part of anode as long as the conversion rate remains high and stable during the reforming process. Then, anode-supported fuel cells always have a smaller internal resistance compared to electrolyte-supported cells because of the much thinner electrolyte. The resistance of electrolyte is the main reason for the voltage drop within a cell during the test.

Among many kinds of anode materials that have a good catalytic reforming and electrochemical reactivity, Ni/YSZ is the most commonly used because of its cost-effective and well suitable for anode-supported fuel cell design requirements[9]. Moreover, Ni/YSZ anode containing 40-60% (mass ratio) nickel has a similar thermal expansion coefficient compared to YSZ[10], which balances the catalytic and conductive ability very well and thus becomes a great candidate for anode material. Figure.1 (b)[5] shows a schematic image of Ni-based anode-supported SOFC. LSM+YSZ are used as cathode materials and dense YSZ is used for electrolyte. Anode can be divided into two layers: anode functional layer and anode conductive layer. For the structure in Figure.1 (b), anode functional layer is about 30um in thickness and this is where hydrogen oxidation reaction takes place and power comes out. For the anode conductive layer,
porous Ni/YSZ is used as the backbone of the cell structure. Methane or other hydrocarbons like methanol[11], ethanol[12] are pumped in and become hydrogen and carbon monoxide for power generation on the functional layer. With an anode-supported SOFC having high catalytic activity of methane steam reforming reaction, we can directly pump in methane or other hydrocarbons without any external reformer and thus a big amount of money spent on reactors, plants and industrial land can be saved.

At the same time, despite of these advantages for Ni-based anode material, some problems like sulfur poisoning, instability at high temperature, carbon deposition, are still limiting the wide application of this material. Among the challenges of limitation listed above, the biggest one is the performance degradation of fuel cell caused by solid carbon formation on the surface of the Ni/YSZ anode cermet.

Carbon deposition on the Ni/YSZ cermet anode materials mainly happen through the following three chemical reactions[13], shown in Equation (2) (3) and (4): a) Methane decomposition at high temperature and low steam to carbon ratio; b) Boudouard reaction occurs at low temperatures because of high concentration of CO; c) Reduction of carbon monoxide by hydrogen produced by previous reactions. The reverse reaction of Equation (4) can also be used as a pathway to remove surface coke, which we will discuss in the following section.

\[
CH_4 \Leftrightarrow C + 2H_2 \quad \Delta H = 75KJ/mol \quad (2)
\]

\[
2CO \Leftrightarrow C + CO_2 \quad \Delta H = -172KJ/mol \quad (3)
\]

\[
CO + H_2 \Leftrightarrow C + H_2O \quad \Delta H = -131KJ/mol \quad (4)
\]

Table.1 Catalyst composition and BET surface area of each catalyst[14]

<table>
<thead>
<tr>
<th>Catalyst</th>
<th>Ni (%)</th>
<th>MgO (%)</th>
<th>CaO (%)</th>
<th>Al₂O₃ (%)</th>
<th>S_BET (m²/g)</th>
<th>S_N₂ (m²/g)</th>
<th>Dp₁ (nm)</th>
<th>Dp₂ (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>NiHT30</td>
<td>12.5</td>
<td>24.5</td>
<td>59.6</td>
<td>271</td>
<td>8.6</td>
<td>12</td>
<td>12</td>
<td></td>
</tr>
<tr>
<td>NiHT50</td>
<td>12.5</td>
<td>42.6</td>
<td>41.5</td>
<td>201</td>
<td>4.2</td>
<td>24</td>
<td>23</td>
<td></td>
</tr>
</tbody>
</table>

4
The morphology and amount of carbon deposition depend on the reactants, anode materials and operation temperature of the cells[15]. Figure 2[14] are the HR-TEM pictures of different mythologies of carbon nanofibers at different composition of Ni/MgO Al₂O₃ support. The CNF diameter produced on Ni/HT30 is smaller than that produced on Ni/HT50, which indicates that anode support materials can greatly influence the morphology of the generated carbon.

Furthermore, Ni catalyst on anode-supported fuel cells can be damaged by the formation of the carbon whiskers or nanofibers, which have a high hardness, leading to the appearance of cracks on the surface of catalysts. Another big disadvantage of the carbon deposition is that it can block the active sites thereby inhibiting gas transportation, preventing reforming reactions by blocking the triple-phase boundary (TPB)[16]. The detailed mechanism of carbon formation will be illustrated in the following section.
2. **Carbon deposition and its mechanism on Ni-YSZ catalyst for methane steam reforming**

The main composition of natural gas is methane, and the Ni-Y2O3-stabilized zirconia (Ni-YSZ) catalyzes the steam methane reforming at high temperature, usually from 700°C to 900°C. The advantages of Ni-YSZ as anode materials has been illustrated in the previous part. In this part, carbon deposition thermodynamics and kinetics from catalytic view will be based on this particular material. In order to get a deep understanding of the coke formation for methane steam reforming, we must study the thermodynamics and kinetics of it because we want the highest production of hydrogen along with the highest methane conversion rate. Carbon deposition is only a side product which can deactivate catalysts and even crack the anode electrode of SOFC. The activity of the catalyst will be significantly affected by the nature of the deposited carbon, which including the amount, the shape and the distribution.

The phenomenon of carbon deposition on the catalyst surface is shown in Figure.3 [17]. Carbon may chemisorb strongly as a monolayer or physically adsorb in multilayers to block access of the reactant to active metal surface sites. Shalini Arora and co-workers[18] listed different types of carbon species deposited during methane drying reforming process in Table.2. Carbon forms different shapes on different temperatures and supports, thus the influence to catalysts is also quite different. Some forms of carbon decrease the catalyst activity by blocking the sites or plugging the pores to deactivate the anode. As shown in Table.3[19], deactivation and failure of methane steam reforming catalysts at high reaction temperature (500-900°C) may be caused by a 50-70nm-layer of dissolved carbon on the Ni surface. If carbon atoms continue to gather on the Ni surface, adsorption and reaction process will be slowed down until a complete termination[19].

From the view of thermodynamic, factors like temperature, pressure and ratio of feedstock, all greatly influence the conversion rate of methane and the fraction of hydrogen production[20]. These important factors also show big effect on carbon deposition morphology which has been illustrated. For
industrial production of hydrogen, regions of carbon forming potential in hydrocarbon steam reforming could be carefully avoided. The filamentous carbon grows at an extremely high speed and causes catastrophic pore plugging. By using this catalytic property of Ni on carbon accumulation and growth, some researchers [14, 21, 22] even synthesis filamentous carbon or other shapes of carbon on different conditions for multiple uses.

On the other hand, sometimes it is difficult to suppress carbon deposition in industrial production due to the cost of related equipment or other reasons, which means coke may occur thermodynamically. For example, more steam benefits the conversion of methane for methane steam reforming and decreases of coke based on thermodynamic calculation. However, it is quite expensive to generate more steam because of the cost on generators and accessories. At the same time, the maintenances of the whole system cost a lot. So we must think of a way from the kinetic aspect to suppress this deactivating agent. Providing SOFCs with fuels containing hydrocarbons leads to the risk of depositing carbon on the anode[23, 24]. In the beginning, the investigations on methane steam reforming reaction have been mainly studied on the preparation of catalyst and process analysis. While in the past forty years, the kinetics and the reaction mechanisms have also been addressed [25-27] to propose coherent reaction mechanism. Carbon deposition is a side product which can degrade the catalyst and methane conversion rate. Equation (1) and Equation (2) mentioned above are two main sources for carbon deposition on Ni catalyst surface. So if we want to study the kinetics of carbon formation on catalyst surfaces, we must focus on the homogenous global reactions during methane steam reforming and give detailed expressions on the reactions we are interested in, which are the reactions related to coke.
Figure 3. Pore plugging in a supported metal catalyst owing to carbon deposition

Table 2: Details of different carbon species formed on the catalyst surface

<table>
<thead>
<tr>
<th>Carbon structure</th>
<th>Designation</th>
<th>Temperature range (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Adsorbed, atomic carbon (surface carbide)</td>
<td>Cₐ</td>
<td>200–400</td>
</tr>
<tr>
<td>Polymers, amorphous films</td>
<td>Cₚ</td>
<td>250–500</td>
</tr>
<tr>
<td>Ni carbide (bulk)</td>
<td>C₇</td>
<td>150–250</td>
</tr>
<tr>
<td>Vermicular filaments or whiskers</td>
<td>Cᵥ</td>
<td>300–1000</td>
</tr>
<tr>
<td>Graphite (crystalline) platelet films</td>
<td>C₇</td>
<td>500–550</td>
</tr>
</tbody>
</table>

Table 3: Carbon species formed in steam reforming of hydrocarbons on Ni catalysts

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Encapsulating film</th>
<th>Whisker-like</th>
<th>Pyrolytic carbon</th>
</tr>
</thead>
<tbody>
<tr>
<td>Formation</td>
<td>Slow polymerization of C₆H₆ radicals on Ni surface, into encapsulating film</td>
<td>Diffusion of C through Ni crystal, nucleation and whisker growth with Ni crystal at top</td>
<td>Thermal cracking of hydrocarbon; deposition of C precursors on catalyst</td>
</tr>
<tr>
<td>Effects</td>
<td>Progressive deactivation</td>
<td>No deactivation of Ni surface. Breakdown of catalyst and increasing ΔP</td>
<td>Encapsulation of catalyst particle; deactivation and increasing ΔP</td>
</tr>
<tr>
<td>Temp. range. °C</td>
<td>&lt;500</td>
<td>&gt;450</td>
<td>&gt;600</td>
</tr>
<tr>
<td>Critical parameters</td>
<td>Low temperature, low H₂O/C₆H₆, low H₂/C₆H₆, aromatic feed</td>
<td>High temperature, low H₂O/C₆H₆, no enhanced H₂O adsorption, low activity, aromatic feed</td>
<td>High temperature, high void fraction, low H₂O/C₆H₆, high pressure, acidic catalyst</td>
</tr>
</tbody>
</table>
2.1 Thermodynamic calculations and experiments of carbon deposition for methane steam reforming

2.1.1 Methane steam reforming thermodynamics

Methane steam reforming is the current commercial method for syngas production in petrochemical and industrial scale plants. The syngas is used for the chemical, petrochemical and refinery industries for producing methanol, ammonia and other hydrocarbons with higher added value[28]. The process of methane steam reforming requires a large amount of energy, which combining methane steam reforming and water gas shift reaction together[29, 30]. Water gas shift reaction (WGSR) is a low exothermic reaction in nature and is expressed by Equation (6). It is also a path of hydrogen production.

\[
\begin{align*}
CH_4 + H_2O &\leftrightarrow CO + 3H_2 \quad \Delta H_{298}^0 = 206kJ/mol \quad (5) \\
CO + H_2O &\leftrightarrow CO_2 + H_2 \quad \Delta H_{298}^0 = -46kJ/mol \quad (6)
\end{align*}
\]

In order to analyze the thermodynamic equilibrium of all the variables at any temperature and pressure, multicomponent mixture must be considered properly. Previous works have been presented the application of Gibbs free energy minimization method for various fuels reacted with steam or carbon dioxide, such as methane [31-33], ethanol[12], propane[34], glycerol[35]. Other computations of the equilibrium constants based on standard ΔH and ΔG values[36, 37], entropy maximization calculations [28] are also used to study the thermodynamic system related to hydrogen production or reforming process.

While, the Gibbs minimization method has been widely used because of its simplicity and its ability to calculate equilibrium compositions even for systems where the reaction pathways are unknown. By using the minimization of Gibbs free energy method, we can quantitatively predict product distribution at equilibrium conditions in a quite complicated system. For the system we are now interested in, the compositions of methane steam reforming can contain CH4, CO2, CO, H2, H2O and solid carbon when coke is considered.
The method of Gibbs free energy minimization to study the thermodynamic of methane steam reforming or other hydrocarbon reforming is quite similar[20]. The total Gibbs free energy of a chemical reactive system is given by Equation (7).

\[ G^t = \sum_{i=1}^{N} n_i u_i \]  
\[ u_i = \Delta G^0_i + RT \ln \left( \frac{f_i}{f_i^0} \right) \]  

The total of Gibbs free energy at constant temperature and pressure, the number of species in the feed and the mole of species are presented by \( G^t \), \( N \) and \( n_i \) respectively. Equation (8) is the chemical potential of the whole system.

Where \( f_i \) is the fugacity in the system and \( f_i^0 \) refers to the standard fugacity and both can be given as:

\[ f_i = y_i \phi_i P \]  
\[ f_i^0 = P_0 \]

Where \( \phi_i \) is the fugacity coefficient of species \( i \) in the feedstock, which can be calculated by using the Virial equation of state, and \( y_i \) the molar fraction of species \( i \). \( R \) is the universal gas constant, \( \Delta G^0_i \) is the standard Gibbs energy of formation, that related only to temperature and reports in some references. Study of the equilibrium conditions in the gas phase by introducing the Lagrangian multiplier leads to Equation (11)

\[ \sum_{i}^N n_i \left( \Delta G^0_i + RT \ln \left( \frac{f_i}{f_i^0} \right) + \sum_k \lambda_i a_{ik} \right) = 0 \]  

Amount of Gibbs free energy and enthalpy of formation for the present composition in the system are shown in Table.4 [38]. Softwares like MATLAB[20, 39], Aspen-SYSYS 2006[33], Aspen Plus[40] are commonly used to study the multi-compositions in the system.
Table 4. A list of amounts of enthalpy and Gibbs free energy of formation[38]

<table>
<thead>
<tr>
<th>Species</th>
<th>$\Delta H_{298}^\circ$ (kJ mol$^{-1}$)</th>
<th>$\Delta G_{298}^\circ$ (kJ mol$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH$_4$</td>
<td>-74.5</td>
<td>-50.5</td>
</tr>
<tr>
<td>CO</td>
<td>-110.5</td>
<td>-137.2</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>-393.5</td>
<td>-394.4</td>
</tr>
<tr>
<td>H$_2$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>H$_2$O</td>
<td>-241.8</td>
<td>-228.6</td>
</tr>
<tr>
<td>O$_2$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

For the methane steam reforming reaction, methane conversion rate, selectivity of hydrogen are main factors to evaluate the quality of catalyst and reforming, which show the efficiency of the catalytic process[28]. Although the existence of some inevitable side reactions causes the inaccuracy in hydrogen production such as Equation (2)-(4), higher methane conversion rate indicates higher hydrogen production to some extent and thus a better performance for power generation in solid oxide fuel cells. To study the performance of methane steam reforming under different carbon to steam ratio, temperature and pressure, theoretical calculations and practical experiments were performed to optimize the ratio in different situations.

Farshad Farshichi Tabrizi and co-workers[20] studied hydrogen production in the ranges of steam to methane ratio from 0.5 to 3, reaction pressure from 1 to 50 bar (~0.1 to 5 atmosphere) and operative temperature from 600 to 1200K using Gibbs free energy minimization method. 3-D images were plotted to clearly illustrate the influence of carbon to steam ratio, temperature and pressure to methane conversion and hydrogen selectivity. Figure 4 (a) shows that the temperature significantly change the methane conversion rate. Due to the endothermic property of methane steam reforming reaction, we can also see the methane conversion increases with the growing temperature in the range of 600-1200K. The reaction favors low pressure, which can be noticed from Equation (1). Figure 4(a) also told the same trend. It is clear that methane conversion was increased with the increasing temperature and inlet steam to carbon.
Conversion of methane as re and the inlet (H₂O/CH₄) as a function of the (a) temperature and pressure (b) temperature (c) pressure and the inlet (H₂O/CH₄)

\[
\text{ConvCH}_4 = -3.25019 + 0.00770488 \times T - 0.0317249 \times P + 0.0354457 \times \left(\frac{H_2O}{CH_4}\right) - 3.5056 \times 10^{-6} \times T^2 + 0.000151511 \times P^2 - 0.0444696 \times \left(\frac{H_2O}{CH_4}\right)^2 + 1.32682 \times 10^{-5} \times T^2 + 0.000127971 \times T \times \left(\frac{H_2O}{CH_4}\right) + 0.00225275 \times P \times \left(\frac{H_2O}{CH_4}\right)
\]  

After theoretical charts illustration, Equation (12) was calculated and shown to describe the relations between the methane conversion and three main parameters. All these three parameters are important and temperature is the most significant one because of the quadratic term in the equation, which perfectly matched the results shown in Figure.4. Moreover, the interaction of temperature with inlet and interaction of pressure with inlet has no important influence on the methane conversion.
Hydrogen selectivity has also been studied, as shown in Figure.5. Hydrogen is the main production we desire for the next electrochemical reaction on anode material to generate power in SOFCs. It is evident that the high hydrogen production favors low pressure. As also clearly visible in Figure.5 (a), the effect of pressure at high temperature is far weaker than that at low temperature, which indicates the big effect of temperature on hydrogen selectivity. On the condition of temperature and steam to methane ratio,
temperature is also the dominant parameter according to Figure.5 (b). When considering the influence of inlet ratio and system pressure, we can see a linear behavior on the selectivity of hydrogen.

Equation (13) was calculated to show the mathematical modeling selectivity of hydrogen in methane steam reforming with all operational conditions including temperature. Same conclusions can be drawn that the inlet ratio is almost a negligible variable, while temperature is a crucial parameter for hydrogen selectivity.

M.S Challiwala and his co-workers [39] used MATLAB to evaluate the potential of overcoming the limitations of dry reforming by integrating it with other commercial methane reforming technologies such as steam reforming and partial oxidation reforming in industrial operating conditions. They studied simultaneous effects of temperature (200°C-1200°C), pressure (1-20 bar) and feed mole ratios (of methane, steam, carbon dioxide and oxygen). After calculation, the optimized operating condition of 750°C at 1 bar pressure at a feed mole ratio CH4:H2O:O2:CO2 of 1:0.4:0.3:1. At this condition, carbon deposition can be totally eliminated and CO2 conversion rate can be as high as 47.84%.

Y.S.Seo and co-workers [41] have done some thermodynamic calculations and analysis on methane steam reforming (SMR), partial oxidation (POX) and auto-thermal reforming (ATR) by adjusting the temperature, reactor pressure, and carbon to steam ratio using AspenPlusTM. They calculated the optimum steam-to-carbon (S: C) ratio of the SMR and found it to be 1.9. After comparing the CH4 flow rate required to generate 1mol/s of hydrogen, they demonstrated that partial oxidation reforming system has the lowest energy cost because of the least methane consumed.

Thermodynamic calculation on steam reforming of other hydrocarbon was also investigated. Sushil Adhikari [42] studied the steam reforming of glycerol for hydrogen production. To reach the high production of hydrogen, high temperature is also needed, usually higher than 900K. A high molar to glycerol can not only benefit the yield of hydrogen, but can also minimize some of the side productions like methane and carbon.
2.1.2 Thermodynamics of carbon deposition for methane steam reforming

Thermodynamic calculation of methane steam reforming is shown in the previous part of this report. Presence of carbon deposition coming from the methane pyrolysis described by Equation (2) leads to rapid deactivation of catalyst by covering the active sites available for reactions. While, this side product caused by complicated reactions in methane steam reforming system can be partially eliminated by choosing the right operational conditions through thermodynamic approaches.

Further developing of Equation (11) by Farshad Farshchi Tabrizi [20] to calculate coke formation, graphite was considered in the list of component collection. However, Gibbs free energy of graphite formation is zero thus it was only calculated in the elemental constraints. By using minimization of Gibbs free energy method, the final form of main equation is shown in Equation (14).

![Graph showing coke formation as a function of temperature and pressure, temperature and inlet (H₂O/CH₄), and pressure and inlet (H₂O/CH₄).](image)

Figure 6: Coke formation as a function of the (a) temperature and pressure (b) temperature and the inlet (H₂O/CH₄) (c) pressure and the inlet (H₂O/CH₄)
\[ \sum_{i=1}^{N-1} n_i \left( \Delta G_{f_i}^o + RT \ln \left( \frac{\bar{f}_i}{\bar{f}_0} \right) + \sum_k \lambda_{ik} a_{ik} \right) + (n_c \Delta G_{f_{c(s)}}^o) = 0 \] (14)

Figure 6 shows the amount of coke formation (number of moles of carbon at the equilibrium/inlet number of moles of CH\(_4\)) or C/M at the equilibrium condition as a function of temperature, pressure and steam to carbon ratio. C/M is obviously mainly influenced by pressure and the amount of coke formation decreases in the increase in pressure till to P=32.9 bar then it increases again. The elevation of temperature resulted to decomposition of methane according to Equation (1). Moreover, the increase in steam to carbon ratio strongly presented a negative effect on the coke presence because of the carbon gasification reaction which shows by Equation (15).

\[ C + H_2O \leftrightarrow CO + H_2 \] (15)

The full quadratic equation for coke formation is shown in Equation (16), which indicates that the effect of pressure on coke deposition is vital for long-term service of catalysts.

\[
\frac{C}{M} = 0.125015 + 6.07031 \times 10^{-5} \times T - 0.00661950 \times P - 0.0405367 \times \left( \frac{H_2O}{CH_4} \right) - 1.43576 \times 10^{-8} \times T^2 \\
+ 9.67926 \times 10^{-5} \times P^2 + 0.00783472 \times \left( \frac{H_2O}{CH_4} \right)^2 - 1.70018 \times 10^{-7} \times T \times P - 1.44237 \times 10^{-5} \times T \\
+ 0.000353826 \times P \times \left( \frac{H_2O}{CH_4} \right) \] (16)

As for the application of solid oxide fuel cell fueled with hydrocarbons, ternary diagram containing C-H-O is useful to predict the cell potential and coke formation. Tatsuya Takeguchi and his colleagues[43] calculated equilibrium partial pressure of oxygen and the boundary of carbon deposition region in the C-H-O diagram at temperature ranging from 400 °C to 1000 °C on Ni-YSZ cermet, which is the most commonly used anode material for solid oxide fuel cell. The contour map was shown in Figure 7. The broken lines showed the boundary of carbon deposition region in four pictures and the carbon deposition region is expected in carbon-rich compositions beyond the lines. The stars shown in the pictures indicated
the highest theoretical cell voltage in the carbon free region because of the lowest oxygen partial pressure at the anode side.

Y.S. Seo and co-workers [41] have done some thermodynamic calculations and analysis on methane steam reforming by adjusting the temperature, reactor pressure, and carbon to steam ratio. Figure 8 is a contour diagram that combines the conversion and C(s) mole fraction in terms of both the air ratio and the reactor temperature. Using the simulation, we can see that the optimum steam to carbon ratio in the steam methane reforming (SMR) is found to be 1.9 or more.

Figure 7 The equilibrium partial pressure of oxygen and the boundary of carbon deposition region in gas mixtures for the C–H–O diagram at temperatures ranging from 400 to 1000℃[43].
Besides methane as a fuel gas for steam reforming, other kinds of hydrocarbon were also studied for the feed of steam reforming. Coke problems have also been studied for decades by thermodynamic analysis. S. Assabumrungrat [11] undertook a detailed thermodynamic analysis for carbon formation in a solid oxide fuel cell system with a direct internal reformer (DIR) fueled by methanol. The results indicated that carbon formation can be prevented by either increasing the inlet H$_2$O: MeOH ratio or by increasing the operating temperature, which is shown in Figure.9.

![Contour diagram of C(s) and conversion with regard to both reactor temperature and S:C ratio in SMR reactor. Reactor pressure, 1.0 bar; (- - -) C(s) mole fraction; (-) conversion.](image1)

**Figure.8**[41] Contour diagram of C(s) and conversion with regard to both reactor temperature and S:C ratio in SMR reactor. Reactor pressure, 1.0 bar; (- - -) C(s) mole fraction; (-) conversion.

![Influence of extent of electrochemical reaction of hydrogen on requirement of inlet H$_2$O: MeOH ratio at different operating temperature](image2)

**Figure.9** [11] Influence of extent of electrochemical reaction of hydrogen on requirement of inlet H$_2$O: MeOH ratio at different operating temperature
Aline Lima da Silva [12] calculated the carbon deposition thermodynamic during ethanol steam reforming and found that at high contact times, for $T > 550 \text{K}$ an inlet steam/ethanol ratio of 3:1 would be suitable to perform steam reforming of ethanol without coke presence. For lower temperature like 400K, an inlet steam/ethanol ratio should be as high as 5:1 to prevent carbon deposition. The thermodynamic calculation result is shown in Figure.10.

![Figure.10](image1)

**Figure.10**[12] Carbon activities as function of temperature, for five inlet H$_2$O/EtOH ratios

![Figure.11](image2)

**Figure.11** Energies for the species on Ni (211) and Ni (111). All energies are relative to CH$_4$ and H$_2$O in the gas phase and calculated using results for individual species[44]
Many theoretical scientists [45-47] are also working on the simulations and calculations of carbon deposition. Density functional theory (DFT) is another computational quantum mechanical modeling method often applied to calculate the carbon deposition energy and issues related to similar problems. DFT was first proposed by Hohenberg and Kohn[48] as a branch of first-principles calculations based on the electron density. In 1983, Parr wrote a review to alert the promise of this theory in the description of chemical phenomena[49]. With time passing by, DFT theory has been further developed with different functions particularly when calculating different systems, which builds a tight and strong correlation between theoretical and experimental data in elemental physics and chemistry.

By using DFT calculations, H.S.Bengaard and co-workers[44] were able to propose that there were at least two kinds of active sites for steam reforming on Ni catalysts and gave an explanation of the reason why additives like potassium or gold can suppress the carbon formation. Figure.11 concludes the results of density functional theory (DFT) calculations of methane steam reforming process over a Ni (111) surface and a stepped site Ni (211) surface. Two important features can be concluded:

- There are at least two reaction channels for carbon deposition. The step sites Ni (211) are much more active than close-packed surface Ni (111), which means carbon formation are likely to occur on step sites.

- Atomic carbon has much higher stability on steps than on terrace sites.

The carbon atoms adsorb on Ni surface chemically, but the adsorptive production remains undetected directly for quite a long time. While, Nabeel A. Jarrah and co-workers [21] first directly observed that before the formation of CNFs on polycrystalline Ni, C atoms combined with Ni to form a meta-stable compound Ni$_3$C initially. Then the Ni$_3$C decomposes into Ni and C because of its instability. Figure.12 shows the micrographs of Ni catalyst after short time exposure in C$_2$H$_4$ and N$_2$ is used as protecting atmosphere. The initial stage of carbon formation can be observed from Figure.12 (a) (b) (c). After a long time of exposure, the carbon nanofibers become larger and Ni particles are lifted from the bottom of the surface to the very tiny tips of carbon nanofibers according to Figure.12 (d) (e) (f). Figure.13
[50] is the XRD patterns evidence of Ni₃C observation which matches very well with Figure.12(b) in contrast to longer times of exposure to ethylene.

Figure.12 SEM micrographs of the surface of Ni foam (reduced at 700°C) after exposure to 25% C₂H₄ in N₂ (total flow rate 107 mL/min) at 450°C during (a) 1 min, (b) 5 min, (c) 20 min, (d) 30 min, (e) 60 min, (f) 120 min; in the right-hand panels in micrographs (d), (e), and (f) Ni particles show bright.

Figure.13 Ni₃C X-Ray diffraction patterns on Ni foams (reduced at 700°C) after exposure to 25% C₂H₄ in N₂ (total flow rate 107 mL/min) at 450°C during 0, 10 to 20 min.
2.2 Kinetics of carbon deposition on Ni-YSZ catalyst

2.2.1 Methane steam reforming kinetics

Although we can intentionally prevent the coke formation by running the catalytic steam methane reforming reaction at regions where coke can be thermodynamically eliminated, kinetic restrictions can still lead to carbon deposition on the surface of catalyst. Before addressing the carbon deposition kinetics on Ni-YSZ catalyst, the kinetics of methane steam reforming have to be discussed.

Temkin et al. [51] proposed one of the early accurate kinetic model on methane steam reforming in 1979. He conducted the experiments on nickel foil at atmospheric pressure and changed the temperature from 470-900°C. The results of the tests showed that the reforming reaction followed a first-order kinetic reaction and now there is a general agreement on this issue [52]. Later, Xu and Froment [53, 54] improved the Temkin’s model and developed the most popular kinetic model for methane steam reaction. They provided a series of reactions and then reduced to three main reactions by considering Langmuir-Hinshelwood reaction mechanism, which was a commonly used approximation when dealing with complicated reactions [55]. The key assumption of the Langmuir-Hinshelwood mechanism is that the methane molecules, and C and H atoms were adsorbed onto the same sites. Therefore, the decomposition of one methane molecule requires five adsorption sites [56]. The proposed rate reaction expressions are shown in Equation (16)-(18) as for the reaction (19)-(21), where $k_i$ are the coefficient of reactions, $K_i$ adsorption constants and $K_{eq,i}$ equilibrium constant of reactions [57].

$$r_1 = \frac{k_1 \cdot \frac{p_{CH_4} \cdot p_{H_2O}}{k_1} \cdot \left(1 + K_{CO} \cdot p_{CO} + K_{H_2} \cdot p_{H_2} + K_{CH_4} \cdot p_{CH_4} + K_{H_2O} \cdot \frac{p_{H_2O}}{p_{H_2}}\right)^2}{\left(1 + K_{CO} \cdot p_{CO} + K_{H_2} \cdot p_{H_2} + K_{CH_4} \cdot p_{CH_4} + K_{H_2O} \cdot \frac{p_{H_2O}}{p_{H_2}}\right)}$$

(16)
Ethan S. Hecht et al. [58] reported investigations of thermal methane reforming chemistry within porous Ni-YSZ anode materials. Table 5 lists a reaction mechanism which used to describe the heterogeneous kinetics within a Ni-YSZ anode. It represented all the global processes in the SOFC anode including methane steam reforming, water-gas-shift and surface carbon coverage. The net activation energy of reactions 12, 20, 21, and 23 depend on the CO(s) coverage as shown in Equation (22) [59], where A is a constant decided by reaction and $\theta_{cov}$ is the available vacancies for the reactions.

$$k = A T^n \exp \left( - \frac{E}{R T} \right) \exp \left( - \frac{\varepsilon_{cov} \theta_{cov}}{R T} \right)$$  \hspace{1cm} (22)$$

In summary, many studies have been investigated methane steam reforming kinetic by analyzing different catalysts and supports. They proposed different kinetic expressions by assuming different rate limiting steps for elementary reactions. According to Jones et al. [60], the differences in kinetics mechanisms are caused by the different distribution of particle sizes, metal particles dispersion, and support used in each study.
Table 5 [51] Heterogeneous reaction mechanism for CH$_4$ reforming on Ni-based catalysts

<table>
<thead>
<tr>
<th>Reaction</th>
<th>$A^{h}$</th>
<th>$n$</th>
<th>$E^{b}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. $H_2 + Ni(s) + Ni(s) \rightarrow H(s) + H(s)$</td>
<td>$1.000 \times 10^{-2}$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>2. $H(s) + H(s) \rightarrow Ni(s) + Ni(s) + H_2$</td>
<td>$5.593 \times 10^{-19}$</td>
<td>0.0</td>
<td>88.12</td>
</tr>
<tr>
<td>3. $O_2 + Ni(s) + Ni(s) \rightarrow O(s) + O(s)$</td>
<td>$1.000 \times 10^{-2}$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>4. $O(s) + O(s) \rightarrow Ni(s) + Ni(s) + O_2$</td>
<td>$2.508 \times 10^{-23}$</td>
<td>0.0</td>
<td>470.39</td>
</tr>
<tr>
<td>5. $CH_4 + Ni(s) \rightarrow CH_4(s)$</td>
<td>$8.000 \times 10^{-3}$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>6. $CH_4(s) \rightarrow Ni(s) + CH_4$</td>
<td>$5.202 \times 10^{-15}$</td>
<td>0.0</td>
<td>33.15</td>
</tr>
<tr>
<td>7. $H_2O + Ni(s) \rightarrow H(s)O(s)$</td>
<td>$1.000 \times 10^{-6}$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>8. $H_2O(s) \rightarrow Ni(s) + H_2O$</td>
<td>$4.579 \times 10^{-12}$</td>
<td>0.0</td>
<td>62.68</td>
</tr>
<tr>
<td>9. $CO_2 + Ni(s) \rightarrow CO_2(s)$</td>
<td>$1.000 \times 10^{-6}$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>10. $CO_2(s) \rightarrow Ni(s) + CO_2$</td>
<td>$9.334 \times 10^{-17}$</td>
<td>0.0</td>
<td>28.80</td>
</tr>
<tr>
<td>11. $CO + Ni(s) \rightarrow CO(s)$</td>
<td>$5.000 \times 10^{-11}$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>12. $CO(s) \rightarrow Ni(s) + CO$</td>
<td>$4.041 \times 10^{-11}$</td>
<td>0.0</td>
<td>112.85</td>
</tr>
<tr>
<td>13. $O(s) + H(s) \rightarrow OH(s) + Ni(s)$</td>
<td>$5.000 \times 10^{-22}$</td>
<td>0.0</td>
<td>97.90</td>
</tr>
<tr>
<td>14. $OH(s) + Ni(s) \rightarrow O(s) + H(s)$</td>
<td>$2.005 \times 10^{-21}$</td>
<td>0.0</td>
<td>37.19</td>
</tr>
<tr>
<td>15. $OH(s) + H(s) \rightarrow H_2O(s) + Ni(s)$</td>
<td>$3.000 \times 10^{-20}$</td>
<td>0.0</td>
<td>42.70</td>
</tr>
<tr>
<td>16. $H_2O(s) + Ni(s) \rightarrow O(s) + H(s)$</td>
<td>$2.175 \times 10^{-21}$</td>
<td>0.0</td>
<td>91.56</td>
</tr>
<tr>
<td>17. $OH(s) + O(s) \rightarrow O(s) + H_2O(s)$</td>
<td>$3.000 \times 10^{-21}$</td>
<td>0.0</td>
<td>100.00</td>
</tr>
<tr>
<td>18. $O(s) + H_2O(s) \rightarrow OH(s) + OH(s)$</td>
<td>$5.423 \times 10^{-23}$</td>
<td>0.0</td>
<td>209.37</td>
</tr>
<tr>
<td>19. $CH_3OH(s) + Ni(s) \rightarrow CH_3OH(s) + Ni(s)$</td>
<td>$5.200 \times 10^{-23}$</td>
<td>0.0</td>
<td>148.10</td>
</tr>
<tr>
<td>20. $CO(s) + Ni(s) \rightarrow O(s) + C(s)$</td>
<td>$1.418 \times 10^{-22}$</td>
<td>-3.0</td>
<td>115.97</td>
</tr>
<tr>
<td>21. $O(s) + CO(s) \rightarrow CO_2(s) + Ni(s)$</td>
<td>$2.000 \times 10^{-19}$</td>
<td>0.0</td>
<td>123.06</td>
</tr>
<tr>
<td>22. $CO_2(s) + Ni(s) \rightarrow O(s) + CO(s)$</td>
<td>$3.214 \times 10^{-25}$</td>
<td>-1.0</td>
<td>86.50</td>
</tr>
<tr>
<td>23. $HCOO(s) + Ni(s) \rightarrow CO(s) + H_2O(s)$</td>
<td>$3.700 \times 10^{-21}$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>24. $CO(s) + H(s) \rightarrow HCO(s) + Ni(s)$</td>
<td>$2.338 \times 10^{-20}$</td>
<td>-1.0</td>
<td>127.08</td>
</tr>
<tr>
<td>25. $HCOO(s) + Ni(s) \rightarrow O(s) + CH(s)$</td>
<td>$3.700 \times 10^{-24}$</td>
<td>-3.0</td>
<td>95.80</td>
</tr>
<tr>
<td>26. $O(s) + CH_2(s) \rightarrow HCO(s) + Ni(s)$</td>
<td>$7.914 \times 10^{-20}$</td>
<td>0.0</td>
<td>114.22</td>
</tr>
<tr>
<td>27. $CH_2(s) + Ni(s) \rightarrow CH_2(s) + H(s)$</td>
<td>$3.700 \times 10^{-21}$</td>
<td>0.0</td>
<td>57.70</td>
</tr>
<tr>
<td>28. $CH_2(s) + H(s) \rightarrow CH_2(s) + Ni(s)$</td>
<td>$4.438 \times 10^{-21}$</td>
<td>0.0</td>
<td>58.53</td>
</tr>
<tr>
<td>29. $CH_2(s) + Ni(s) \rightarrow CH_2(s) + H(s)$</td>
<td>$3.700 \times 10^{-24}$</td>
<td>0.0</td>
<td>100.00</td>
</tr>
<tr>
<td>30. $CH_2(s) + H(s) \rightarrow CH_2(s) + Ni(s)$</td>
<td>$9.513 \times 10^{-22}$</td>
<td>0.0</td>
<td>52.58</td>
</tr>
<tr>
<td>31. $CH_2(s) + Ni(s) \rightarrow CH_2(s) + H(s)$</td>
<td>$3.700 \times 10^{-24}$</td>
<td>0.0</td>
<td>97.10</td>
</tr>
<tr>
<td>32. $CH_2(s) + H(s) \rightarrow CH_2(s) + Ni(s)$</td>
<td>$3.086 \times 10^{-24}$</td>
<td>0.0</td>
<td>76.43</td>
</tr>
<tr>
<td>33. $CH_2(s) + Ni(s) \rightarrow C(s) + H_2(s)$</td>
<td>$3.700 \times 10^{-21}$</td>
<td>0.0</td>
<td>18.80</td>
</tr>
<tr>
<td>34. $C(s) + H(s) \rightarrow CH(s) + Ni(s)$</td>
<td>$4.400 \times 10^{-22}$</td>
<td>0.0</td>
<td>160.49</td>
</tr>
<tr>
<td>35. $O(s) + CH_4(s) \rightarrow CH_4(s) + OH(s)$</td>
<td>$1.700 \times 10^{-24}$</td>
<td>0.0</td>
<td>88.30</td>
</tr>
<tr>
<td>36. $CH_4(s) + OH(s) \rightarrow O(s) + CH_4(s)$</td>
<td>$8.178 \times 10^{-22}$</td>
<td>0.0</td>
<td>28.72</td>
</tr>
<tr>
<td>37. $O(s) + CH_4(s) \rightarrow CH_4(s) + OH(s)$</td>
<td>$3.700 \times 10^{-24}$</td>
<td>0.0</td>
<td>130.10</td>
</tr>
<tr>
<td>38. $CH_4(s) + OH(s) \rightarrow O(s) + CH_4(s)$</td>
<td>$3.815 \times 10^{-21}$</td>
<td>0.0</td>
<td>21.97</td>
</tr>
<tr>
<td>39. $O(s) + CH_4(s) \rightarrow CH_4(s) + OH(s)$</td>
<td>$3.700 \times 10^{-24}$</td>
<td>0.0</td>
<td>126.80</td>
</tr>
<tr>
<td>40. $CH_4(s) + O(s) \rightarrow O(s) + CH_4(s)$</td>
<td>$1.206 \times 10^{-23}$</td>
<td>0.0</td>
<td>45.42</td>
</tr>
<tr>
<td>41. $O(s) + CH_4(s) \rightarrow C(s) + OH(s)$</td>
<td>$3.700 \times 10^{-21}$</td>
<td>0.0</td>
<td>48.10</td>
</tr>
<tr>
<td>42. $C(s) + OH(s) \rightarrow O(s) + CH_4(s)$</td>
<td>$1.764 \times 10^{-21}$</td>
<td>0.0</td>
<td>129.08</td>
</tr>
</tbody>
</table>

$^a$ Arrhenius parameters for the rate constants written in the form: $k = AT^a \exp (-E/RT)$. The units of $A$ are given in terms of moles, cm, and s. $E$ is in kJ/mol.

$^b$ Sticking coefficient.

$^c$ Coverage-dependent activation energy (see Eq. 11). Total available surface site density is $\Gamma = 2.60 \times 10^{-8}$ mol/cm$^2$.

### 2.2.2 Kinetics of carbon deposition for methane steam reforming

For methane steam reforming, there are mainly two pathways for carbon deposition, which are decomposition of methane and CO disproportionation (Boudouard reaction). The reaction equations have been shown in previous parts by Equation (2) and Equation (3). The coke can also be removed by carbon
gasification, which is shown in Equation (4) as the reverse reaction. For Ni-YSZ anode material in solid oxide fuel cell, the diffusion of carbon through nickel particles can lead to the removal of surface carbon and this diffusion phenomenon can be regarded as one of the steps in the global mechanism of carbon filament formation and gasification[61]. The coupling of the surface reactions including methane cracking and CO disproportionation, the segregation process, and the diffusion of carbon through the nickel particle leads to a model of the process when we are dealing with carbon filament formation, which forms the basis for the kinetic modeling of carbon formation and gasification reactions.

The kinetic model of carbon deposition for methane steam reforming based on the elementary steps, which consists a rate-limiting dissociative chemisorption step and a stepwise dehydrogenation of the chemisorbed methyl group, was firstly suggested by Grabke and et.al [62-64]. They came to the conclusion that the first chemisorbed step of CH4 is the rate-limiting step. The elementary step of methane decomposition is shown in Table.6[65]. P.Fan and co-workers[66] further studied the carbon formation in a methane and hydrogen mixed atmosphere and calculated all the kinetic model by assuming each step was the rate-determining step. After running the experiments, they found that only the methane chemisorption step was verified to be the rate-limiting step.

Table.6[65] Mechanism of methane cracking starting with non-dissociative methane adsorption

<table>
<thead>
<tr>
<th>Reaction</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH₄ + I (Vacant site) = CH₄ (ad)</td>
</tr>
<tr>
<td>CH₄ (ad) = CH₃ (ad) + H (ad)</td>
</tr>
<tr>
<td>CH₃ (ad) = CH₂ (ad) + H (ad)</td>
</tr>
<tr>
<td>CH₂ (ad) = CH (ad) + H (ad)</td>
</tr>
<tr>
<td>CH (ad) = C (ad) + H (ad)</td>
</tr>
<tr>
<td>C (ad) = C (dissolved)</td>
</tr>
<tr>
<td>2H (ad) = H₂ + 2I</td>
</tr>
</tbody>
</table>
J-W Snoeck and G.F.Froment proposed a kinetic model for Boudouard reaction in which adsorbed oxygen atoms act as intermediate, because these are known to be important in the mechanism of steam reforming and the water-gas shift reaction. The elementary steps of the reactions considered were shown in Table.7.

As widely known, carbon atoms can dissolve into the bulk of Ni particles. The diffusion phenomenon can be a crucial factor for coke formation. In terms of Fick’s law, at steady state, the coking rate coming from the surface reaction equals the rate of carbon diffusion through Ni particles. The diffusion equation is written as:

\[
r = \frac{D_C}{d_{Ni}} a_{Ni}(C_{CNi,f} - C_{CNi,r})
\]  
(23)

Where \(D_C\) is the effective diffusivity for carbon diffusion through the nickel particle, \(d_{Ni}\) is the effective diffusion length in Ni particle, \(a_{Ni}\) is the specific surface area of Ni particles, \(C_{CNi,f}\) is the carbon concentration on the front side of the Ni particle, \(C_{CNi,r}\) is the carbon concentration on the rear side of the Ni particle.

\[
\begin{align*}
\text{Methane cracking} & : \quad \begin{aligned}
\text{CH}_4 + 1 &= \text{CH}_4 - 1 \\
\text{CH}_4 - 1 + 1 &= \text{CH}_3 - 1 + \text{H} - 1 \\
\text{CH}_3 - 1 + 3 \text{i} &= \text{C} - 1 + 3 \text{H} - 1 \\
\text{H}_2 + 2 \text{i} &= 2 \text{H} - 1 \\
\text{C} - 1 &= C_{Ni,i} + 1
\end{aligned}
\end{align*}
\]

\[
\begin{align*}
\text{Boudouard} & : \quad \begin{aligned}
\text{CO}_2 + 2 \text{i} &= \text{O} - 1 + \text{CO} - 1 \\
\text{CO} - 1 &= \text{CO} + 1 \\
\text{H}_2 \text{O} + 1 &= \text{O} - 1 + \text{H}_2 \\
\text{C} - 1 + \text{O} - 1 &= \text{CO} - 1 + 1
\end{aligned}
\end{align*}
\]

\[
\begin{align*}
\frac{D_{CNi}}{d_a} (C_{CNi,f} - C_{CNi,r}) a_{Ni} = \frac{K_{CH_4}}{K_{CH_4}} \left( \frac{1}{K_{CH_4}} + \frac{1}{K_{CH_4}} \right)
\end{align*}
\]

\[
\begin{align*}
\text{Diffusion through Ni} & : \quad \begin{aligned}
\text{CO}_2 + 2 \text{i} &= \text{O} - 1 + \text{CO} - 1 \\
\text{CO} - 1 &= \text{CO} + 1 \\
\text{H}_2 \text{O} + 1 &= \text{O} - 1 + \text{H}_2 \\
\text{C} - 1 + \text{O} - 1 &= \text{CO} - 1 + 1
\end{aligned}
\end{align*}
\]

\[
\begin{align*}
\frac{D_{CNi}}{d_a} (C_{CNi,f} - C_{CNi,r}) a_{Ni} = \frac{K_{CH_4}}{K_{CH_4}} \left( \frac{1}{K_{CH_4}} + \frac{1}{K_{CH_4}} \right)
\end{align*}
\]
Figure 13 [55] Elementary steps of coke formation from methane cracking and of the gasification of coke by H₂O and H₂. Net rate equation for coke formation accounting also for diffusion of carbon through the Ni particles of catalyst.

Coupling Equation (23) with the rate equations for adsorption, Equation (24) for the chemical steps of the finally retained model can be obtained and shown:

\[
\dot{r}_{C,B} = \frac{k_B^+ K_{CO} P_{CO}}{K_{O,CO_2} K_{CO}} \frac{P_{CO_2}}{P_{CO}} \\
= \left( 1 + \frac{K_{C_{C,[NI,F]}} + K_{CO} P_{CO}}{K_{O,CO_2} K_{CO} P_{CO}} \right) \left( \frac{P_{CO_2}}{P_{CO}} \right)^2
\]

(24)

So when the surface reactions including methane cracking and CO disproportionation are considered, the segregation process, and the diffusion of carbon through the nickel particle as a whole, we can get a net rate equation for carbon formation, which is shown in Figure 13[55].

Table 7 [67] Kinetic model of elementary steps for Boudouard reaction and carbon diffusion
2.3 Description of carbon deposition process on Ni particle

Considering carbon formation mechanism as a whole, the one [14, 68, 69] which is accepted most widely involves the following four steps[16]: a) hydrocarbon adsorption on the catalyst surface; b) conversion from the adsorbed hydrocarbon to absorbed carbon atoms by three reactions mentioned above (reactions (2) (3) and (4)); c) diffusion of carbon atoms through Ni particle boundaries and Ni bulk; d) precipitation on the rear side of the Ni particles. The whole process can be illustrated in Figure.14. As the carbon atoms precipitating on the rear side of the metal, the continuous growth of carbon nanofibers can lift the metal particles. This is the reason why we can observe Ni particles on the tips of carbon nanofibers in Figure.12 (d) (e) (f).

Figure.14 [16] Schematic representation of the catalytic growth of a carbon nanofiber (CNF) from a carbon-containing gas.

3. Methods to suppress carbon deposition

Carbon formation can greatly decrease the reforming efficiency and deactivate the whole reaction system by blocking the porous material structures of the anode side in solid oxide fuel cell. Many attempts have been made to overcome carbon deposit for methane steam reforming and great progresses have been
achieved in the recent years. Generally speaking, many measures can be taken to confront the problem, which will be shown in below sections.

### 3.1 Optimization of the reaction system parameters

S. Rakass and co-workers [70] studied the S:C of steam methane reforming using unsupported nickel powder catalysts and they also got similar results. Figure 15 showed that within a quite wide temperature range, a higher steam to carbon would increase the methane conversion rate and a higher production rate of hydrogen.

![Figure 15](image)

**Figure 15** (a) methane conversion as function of CH₄:H₂O molar ratio and temperature  
(b) C formation as function of CH₄:H₂O molar ratio and temperature

Some other researches [71, 72] also suggested that a higher steam to carbon ratio can dramatically decrease the carbon deposition on Ni-based anode material and make the whole system more stable and much more durable for long time service, which has been predicted by thermodynamic calculation shown in the previous section of this paper.

Also, by applying the calculation results from the thermodynamic view, coke favors low temperature and low pressure. So for practical application of solid oxide fuel cell with methane as the fuel, we can set up an optimized condition to suppress carbon deposition and enhance electrochemical reaction.
3.2 Metal elements or rare earth metal oxide addition

Metal element or metal oxide addition is another great and effective way to suppress coking on Ni-based anode materials for methane steam reforming. Alkali metal such as K, Ca, Mg, and noble metal like Ru, Rh, and other metal elements like Co, Cu can be impregnated into the system for the decrease of carbon formation of the system. Metal oxide containing rare earth elements like ceria has also been added into the methane steam reforming system because of its facilitated redox activity. The mechanism of preventing the coke presence for these elements are quite different, which will be presented in the following parts.

3.2.1 Addition of metal oxides (promoters)

A great number of oxides have been proposed as promoters for the catalysts to improve either the activity or the ability to prevent formation of coke. In recent years, researchers have shown growing interest in the effect of rare-earth oxide, especially the application of ceria (CeO₂), which is well known to have a sufficiently high oxygen storage capacity (OSC) to store oxygen under an oxidative atmosphere and release it under a reductive atmosphere[73]. In 2001, Nobuyoshi Nakagawa[74] found that the catalytic activity of Ni-YSZ-CeO₂ anode was higher than that of Ni-YSZ, especially at low temperature. Then, it is reported[75] that for ethane and propane steam reforming, ceria doped Ni/Al₂O₃ showed great reforming activity. The amount of carbon formation decreased with the increase of Ce composition. These improvements are mainly due to the influence of the redox propriety of doped ceria. The addition of ceria provided the oxygen vacancies which can adsorbed surface hydrocarbons (CₙHᵢₓ+Oₓ→nCO+m/2(H₂)+Oₓ₋m). Moreover, the formation of carbon via Boudard reaction can also be reduced because the carbon monoxide can react with the lattice oxygen to produce carbon dioxide, which acts as a depressor to Boudard reaction. Besides the studies on the amount of ceria added into the catalytic system, microstructure modification of Ni and ceria to enhance reforming reactivity has also been discovered. Chengxi Zhang and co-workers[76] fabricated Ni-CeO₂ catalysts for ethanol steam reforming via ball-milling process other than wet-
impregnation method. The process and the stability test results can be briefly illustrated in Figure 16. Small nickel particles are anchored by CeO$_2$ particles forming the core-like morphology and can remain its morphology after test. While, for conventional Ni/CeO$_2$ catalysts, Ni particles are adsorbed on the CeO$_2$ surface randomly and have a coarsening problem after test. TEM images in Figure 17 clearly showed the influence of different fabrication methods of catalyst on the catalyst particle sizes and the amount of carbon deposition after test.

Figure 16[76] Schematic of structures of catalysts prepared by different methods
Figure.17[76] TEM images of the catalysts after stability test, (a) Ni-CeO$_2$ and (b) Ni/CeO$_2$

Carbon deposition on a catalyst is closely related to its surface acidity[77]. Alkaline earth oxides have been widely used as additives or as promoters in catalysts for the reforming reactions to neutralize the acidity of the aluminum oxide support[78, 79], especially for methane dry reforming. It has been found by BM Nagaraja [80] that the addition of 0.5 wt% potassium to catalyst can greatly improve both the activity and stability of the system. A. Carrero[81] and co-workers also indicated that Mg and Ca promoted catalysts favor the formation of defective carbon, which is much easier to be removed during the reforming process. Figure.18 contains three pictures of carbon nanofibers on three kinds of catalysts. It seems that the carbon fibers on CuNi/S sample are much wider than those on Mg and Ca promoted catalysts, which indicates more carbon formation. The following TG analyses confirmed the deduction because a small peak was observed at 588°C for CuNi/S.

However, alkaline earth metal oxides are not suitable for steam reforming because of the risk of hydration of magnesia or calcium oxide[52]. The reaction may result in break-down of the catalyst because it expanses the molecular volume. For fuel cell applications, there are some strict restrictions for material
selections. There are many characteristics of materials to consider, like redox stability, thermal expansion coefficient, sintering ability and so on. Alkaline earth oxides are weak on the match of thermal expansion coefficient with typically used electrolyte and also shows unstable redox stability in reducing atmosphere, which is the service condition as anode material for SOFC use. So despite the wide application in chemistry and chemical engineering, there is still a long way for the application in SOFC field unless a new connection is developed between the fuel cell support and the electrode.

Figure 18 SEM images of used Mg and Ca-modified CuNi/SiO\textsubscript{2} catalysts: (a) CuNi/S, (b) CuNi/Mg\textsubscript{20}S and (c) CuNi/Ca\textsubscript{20}S

3.2.2 Alloyming effect by addition of other metal elements

Ni-Co bimetallic system has long been studied [82-90] on different supports for methane fueled reforming because Co exhibited great activity for the reaction of methane decomposition, which is considered as the rate-determining step for methane reforming [91]. Ni-Co bimetallic catalysts are often prepared by co-precipitating method which using a common aqueous solution containing different amount of nickel nitrate and cobalt nitrate and comes with a calcination and reduction process. Some studies focused on Ni-Co bimetallic catalysts synthesized on traditional oxide support like alumina[89] or alumina modified support [82, 84]. Besides traditional metal oxide support, Lin Chen and his co-workers[83] synthesized Co-Ni bimetallic aerogel catalysts by sol-gel method followed by the supercritical drying process. They took great advantages of the sol-gel catalysts, which exhibited high surface area (about 300 m\textsuperscript{2} g\textsuperscript{-1}) and low bulk density (about 0.04 g ml\textsuperscript{-1}), and studied the effect of Co/Ni ratio on the activity of catalyst. They indicated that the metal particle size is smaller than the “critical size”, leading to a strong coke resistance.
Metal elements like Cu are also great candidates for the decrease of carbon deposition on Ni-based anode materials because of its low cost. Another great advantage of Cu is the high conductivity, which is of great benefit to serve as current collector of SOFC anode. H. Kim[92] and co-workers examined Cu-Ni alloys as anode material for direct oxidation of methane in SOFC at 1073K. Figure.19 showed that the addition of Cu can greatly decrease the carbon formation on Ni-based anode cermet. Eon Woo Park[93] fabricated Cu-Ni-YSZ SOFC anode by electroplating Cu into a porous Ni-YSZ cermet anode and carbon deposited on the anode decreased dramatically at 700°C, which indicated a great function of Cu addition in Ni particles for the decrease of carbon presence. They also found that Cu and Ni can form solid solution with different composition after heat treatment by XRD test shown in Figure.20. While, the power densities of Cu-Ni-YSZ anode-supported single cell in methane and hydrogen were lower than those of the Ni-YSZ. The reason is that Cu is a poor catalyst and the active sites on Ni surfaces were reduced due to the Cu alloying.

Figure.19 Photograph of cermets having 20% metal after reduction in H2 at 1173 K for 3 h and exposure to CH4 at 1073 K for 1.5 h. The photographs are shown for the following metal compositions: a) 100% Cu; b) 90% Cu, 10% Ni; c) 80% Cu, 20% Ni; d) 50% Cu, 50% Ni; e) 100% Ni.
Another great selection to alloy with Ni to limit the carbon deposition on catalyst surface is Sn. Sn-Ni alloy catalysts are widely used in the steam reforming of methane and other hydrocarbons [94-96]. For example[96], Sn-Ni alloy (0.5-1wt% nominal loading of Sn with respect to Ni) was prepared and exhibited improved tolerance to coke formation without compromising much of its electrochemical reactivity.

The SEM image and EDS test result are shown in Figure.21A, showing that Sn is mainly located on the surface layer of the particle. One of the big advantages of low Sn concentration in alloying metal is the tiny influence on the thermal expansion coefficient because the bulk material is still nickel, which can perfectly match to the commonly used electrolytes. Figure.21B is a clear evidence of the crucial role of Sn in preventing coke formation on the Ni catalyst surface. Carbon can be no longer observed by using line scan mode of EDS after Sn was coated on Ni. Figure.22 indicates that the activities of the two anode
materials in the electrochemical oxidation of hydrogen are similar and the addition of tiny amount of Sn did not compromise much of the performance for the SOFC system.

Figure 21A [96] (a) SEM image of a Sn/Ni anode (b) STEM image of a Sn/Ni particle (c) plot of the normalized Sn/Ni ratio measured using EDS as a function of the distance from the bottom of the particle edge
Figure 21B (Color online) (a) SEM of a cross section of Ni anode/electrolyte/cathode assembly after the electrochemical oxidation of isooctane at 1013 K, (b) EDS elemental analysis of the region, outlined in (a), at the electrolyte/anode interface, (c) SEM of a cross section of Sn/Ni anode/electrolyte/cathode assembly after electrochemical oxidation of isooctane at 1013 K, and (d) EDS elemental analysis of the region, outlined in (c) at the electrolyte/Sn/Ni anode interface.

Figure 22 Plot of cell potential and power density as a function of current density for SOFCs with Sn/Ni and Ni anodes. Operating conditions: humidified hydrogen/stagnant air, 1013 K

3.2.3 Addition of noble metal

Noble metals like Ru and Rh are also excellent addition for suppressing carbon formation. Jin Hyeok Jeong [97] added small amount of Ru (wt 1%) on Ni catalysts supported on Al₂O₃ or MgAl₂O₄ cermets and observed the suppression of carbon deposition on the anode. The presence of Ru in a highly dispersed state can also distribute the Ni particles evenly in the system, which decreased the particle size of Ni thus leading to a better coke resistance. Tatsuya Takeguchi et al. [98] applied various kinds of precious metals, which including Ru, Rh, Pd and Pt, to the Ni-YSZ cermet system and studied the electrochemical activity as a SOFC anode and the carbon deposition. They found Ru, Pd, Pt can decrease carbon deposition rate and enhance the electrochemical property, shown in Figure 23. Rh can also promote electrochemical reaction, while the coke seemed to be more severe. However, the price of noble metal is so high that
researchers from all over the world are seeking for alternatives to keep the price of catalyst low, which could benefit the wide use for industry in the future.

![Figure 23](image)

*Figure 23 [98] Current-voltage characteristics in SOFC operation using precious metal-modified Ni-YSZ cermets at 1000°C*

### 3.3 Nickel particle size optimization

For Ni-based anode materials, the particle size of Ni can greatly influence the carbon formation. Researchers have done a lot of work on this problem and progresses have been made so far. KO Christensen[99] and co-workers have discovered that Ni particles which have a smaller crystal size have a higher resistance to coke formation. It is also proposed that there is a carbon thresholds for steam methane reforming on Ni catalyst for particular conditions. Figure.24 showed that in the conditions mentioned, carbon deposition will be totally eliminated if Ni crystal size is less than 10nm.

De Chen[14] studied the relations between the growth rate of carbon nanofibers and the sized Ni crystals, observing the optimum Ni particle size for the growth of carbon is around 34nm, which can be seen in Figure.25.

Actually, the reason why the addition of some metal elements into the Ni catalyst can suppress carbon formation is that the modified metal alloys have a better Ni crystal distribution and smaller Ni...
particle size. Jianguo Zhang [82] focused on the effects of Ni-Co content of the catalyst, attempting to avoid carbon formation on the catalyst. Figure 26 showed the Ni particle distribution chart by adding different amount of Co into the alloy system and Figure 27 showed the carbon formation on the catalyst after 250h test, which indicated that with a smaller size of Ni crystal size, coke can be greatly avoided in this condition.

![Figure 24 Carbon thresholds for steam methane reforming.](image1)

Conditions: total flow rate = 0.009 mol/min, T = 823 K and P = 20 bar.

![Figure 25 [14] Effects of NiO crystal size on the final carbon yield of carbon nanofiber](image2)
4. Conclusions and Prospects
In this problem report, thermodynamic calculations and kinetic approaches of methane steam reforming and related coke formation have been addressed in details. More concerns about coke on Ni-based anode material for SOFC are shown and corresponding solutions are also proposed. Carbon formation on Ni-YSZ anode material for hydrocarbon steam reforming has long been a great challenge for the researchers working in related fields. After decade years of research, significant progress and achievements have been accomplished in predicting the tendency of coke by thermodynamic calculation and studying the mechanism of carbon deposition in different conditions using Ni-YSZ as catalyst for power generation on solid oxide fuel cells. Many typical problems corresponding to catalyst activity or production selectivity can be solved by adjusting catalyst compositions, feed compositions, and reaction conditions. Now researchers are seeking for more paths to decrease the carbon formation during methane steam reforming, like trying new catalyst-synthesis methods or preparing more metal alloying with Ni and significant progresses have been made yet. There also can be more efforts from the view of optimization the working conditions or microstructures of SOFCs. For example, some recent researches reported [100] that by optimizing the oxygen flux, which can be also regarded as current density of the fuel cell, from the cathode side, carbon formation on the anode side can be consumed or even prevented. However, the detailed mechanism is still under discussion. As more studies will be done on varieties of materials, we will get a much more stable-running fuel cell system for a long service time without carbon formation deactivation as a concern.

5. References


